Performance Analysis for Mesh and Mesh-Spectral Archetype Applications

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Abstract

This document outlines a simple method for benchmarking a parallel communication library and for using the results to model the performance of applications developed with that communication library. We use *compositional performance analysis* — decomposing a parallel program into its modular parts and analyzing their respective performances — to gain perspective on the performance of the whole program. This model is useful for predicting parallel program execution times for different types of program archetypes, (e.g., mesh and mesh-spectral) using communication libraries built with different message-passing schemes (e.g., Fortran M and Fortran with MPI) running on different architectures (e.g., IBM SP2 and a network of Pentium personal computers).

1 Introduction

A *parallel programming archetype* [Cha94, CMMM95] is an abstraction that captures the common features of a class of problems with similar computational structure and combines them with a parallelization strategy to produce a pattern of dataflow and communication. Such abstractions are useful in application development, both as a conceptual framework and as a basis for tools and techniques.

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The efficiency of a parallel program can depend a great deal on how its data is decomposed and distributed or on its granularity. This paper describes a simple performance evaluation methodology that includes an analytic model for predicting the performance of parallel and distributed computations developed for multicomputer machines and networked personal computers. This analytic model can be supplemented by a simulation infrastructure for application writers to use when developing parallel programs.

These performance evaluation tools were developed with the following restricted goal in mind: We require accuracy of the analytic model and simulation infrastructure only to the extent that they suggest directions for the programmer to make the appropriate optimizations. This restricted goal sacrifices some accuracy, but makes the tools simpler and easier to use.

A programmer can use these tools to design programs with decomposition and distribution specialized to a given machine configuration. By instantiating a few architecture-based parameters, the model can be employed in the performance analysis of data-parallel applications, guiding process generation, communication, and mapping decisions.

The model is language-independent and machine-independent; it can be applied to help programmers make decisions about performance-affecting parameters as programs are ported across architectures and languages. Furthermore, the model incorporates both platform-specific and application-specific aspects, and it allows programmers to experiment with tradeoffs better than either strictly simulation-based or purely theoretical models. Finally, the model is designed to be simple.

Section 2 presents the model, related work, and our experimental methods. Section 3 and Section 4 describe applications based on the mesh archetype and the mesh-spectral archetype, for use in our performance experiments. Section 5 discusses the experiments, and Section 6 presents conclusions. Source code listings are provided in the Appendices.

2 Performance Model

Archetype-based performance models exploit commonalities in programs to simplify the process of performance analysis. The performance model in this paper, described fully by Rifkin [Rif96], is based on the ideas of extrapolation from observations, asymptotic analysis, scalability analysis, execution profiles, and data fitting, as investigated by Foster [Fos95, Chapter 3].

Since the problem of choosing the data partitioning and distribution to achieve the optimal performance is NP-complete [Rif96], we are more interested in user-guided performance evaluation tools for the refinement of parallel applications than in automatic performance prediction (for example, Fahringer's work with P^3T [Fah96a]). Since our model is likely to be used to supplement a programmer's efforts to develop applications using archetypes, it differs from

efforts to do performance measurement for compiler optimization (as Clement and Quinn do with C^* on multicomputers [CQ93]), and it differs from efforts to estimate performance statically to automate the load balancing of useful work within a program (as with Fahringer's application of P^3T [Fah96b]). Like the BSP model [Val90, GV94], our model decomposes programs into fairly large blocks; our model, however, incorporates the idea of archetypes, gaining ease of use at the expense of greater generality.

Our techniques fit in well with other methodologies for dealing with applications developed for particular architectures (for example, Brinch Hansen's model for programming multicomputer applications [BH93a]). Archetypes frequently represent well-researched patterns or abstractions; for example, the mesh archetype [Mas96] builds on Brinch Hansen's work on parallel cellular automata in the context of multicomputers [BH93b]. In that paper, the computational complexity of parallel cellular automata is derived and shown to be a sufficiently accurate estimator of the performance of a Laplace's equation solver; in this paper, we provide an alternative technique of performance estimation using a combination of benchmarking and analysis that is especially suited to applications developed using archetypes. The mesh-spectral archetype [DM96] extends the parallel cellular automata model, providing row and column operations in addition to grid operations.

2.1 Methodology

A great deal of work has been done both on methods of exploiting design patterns in program development (for example, [Col89] and [GHJV95]) and on methods of solving problems on concurrent processors (for example, [FJL+88] and [BBC+93]). *Archetypes* [Cha94, CMMM95] were developed as design patterns with the single restricted goal of modeling one kind of pattern that is relevant in parallel programming: the pattern of the parallel computation and communication structure.

Methods of exploiting design patterns in program development begin by identifying classes of problems with similar computational structures and creating abstractions that capture the commonality. Combining a problem class's computational structure with a parallelization strategy gives rise to a dataflow pattern and hence a communication structure. It is this combination of computational structure, parallelization strategy, and the implied pattern of dataflow and communication that we capture as a *parallel programming archetype* [Mas98, MC96]. For the remainder of the paper, we use the term "archetype" to refer to a parallel programming archetype.

A key question in the development of a parallel application, especially for a multicomputer or a network of computers, is the issue of data decomposition and distribution. Archetypes directly address the question of which data distributions are compatible with a problem's computational structure. In some cases more than one data distribution is compatible with the computational structure;

in such cases, which one is chosen does not affect program correctness, but it may well affect program performance.

In this paper and related papers ([Rif96, Rif93]) we address the question of how the choice of data distribution affects performance and present a methodology for archetype-based application development, including a phase in which a correct but not necessarily efficient application is refined to improve performance by using an archetype-based performance model.

Our methodology for designing, developing, implementing, and refining an application follows the workflow schedule illustrated in Figure 1. This workflow consists of six major phases: ANALYSIS, APPLICATION, BENCHMARKING, PERFORMANCE MODEL, SIMULATION, and REFINEMENT, each of which we describe in turn.

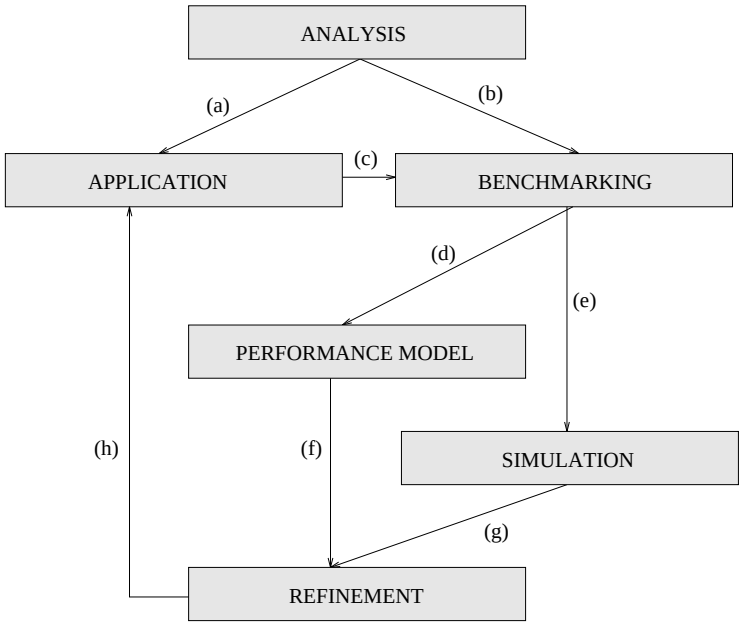


Figure 1: The methodology for using and analyzing the performance of archetypes follows a simple workflow.

Analysis. In the ANALYSIS phase, an appropriate archetype is chosen to help with application development. If more than one archetype could be used, our performance models can suggest which one is more efficient, as is done in Section 5.1. This phase usually starts with a problem description and/or a sequen-

tial program to be parallelized; it ends when the appropriate archetype has been chosen. Two phases of the methodology can then be worked on concurrently: development of the application (path (a) in Figure 1), and benchmarking of computation and communication routines (path (b) in Figure 1).

Application. In the APPLICATION phase, the selected archetype is used to develop an application to solve the specified problem or to parallelize the given sequential program, as follows.

First, the programmer develops an initial archetype-based version of the algorithm. This initial version is structured according to the archetype's pattern and gives an indication of the concurrency to be exploited by the archetype. Essentially, it is produced by adapting the original algorithm or program to fit the archetype pattern and "filling in the blanks" of the archetype with application-specific details. An important feature of this initial archetype-based version of the algorithm is that it can be executed sequentially; if the algorithm is deterministic, it can also be debugged sequentially.

This initial version is then transformed into an equivalent version suitable for efficient execution on the target architecture. The archetype assists in this transformation, either via guidelines to be applied manually or via automated tools. Again, the transformation can optionally be broken down into a sequence of smaller stages, and in some cases intermediate stages can be executed (and debugged) sequentially. A key aspect of this transformation process is that the transformations defined by the archetype preserve semantics and hence correctness.

The programmer then implements the efficient archetype-based version of the algorithm using a language or library suitable for the target architecture. Here again the archetype assists in this process, not only by providing suitable transformations (either manual or automated), but also by providing program skeletons and/or libraries that encapsulate details of the parallel code (for example, process creation and message-passing). A significant aspect of this step is that it is only here that the application developer must choose a particular language or library; the algorithm versions produced in the preceding steps can be expressed in any convenient notation, since the ideas are essentially language-independent.

After this implementation is tested and debugged, its performance can be evaluated and possibly improved via the remaining phases of our methodology.

Benchmarking. BENCHMARKING of archetype communication and computation routines can be performed during or independently of the APPLICATION phase. This phase collects data to be used in performance evaluation via analytic techniques and/or simulation methods.

Our performance model requires two sets of benchmarks: archetype-specific ("communication") benchmarks and application-specific ("computational")

benchmarks. Both sets involve measuring execution times of the relevant routines (from the archetype library for the first set, and from the application for the second) using the target architecture, language, compiler, and library. Computational benchmarks can be done on a single processor; communication benchmarks require N processors, where N is the maximum number of processors the application might use. If the programmer wants to use analysis to help choose an appropriate granularity, communication benchmarks must be done for varying numbers of processors.

Our model uses approximations of higher-level communication routines rather than approximations of low-level measurements such as latency and bandwidth. We do this for two reasons: It is a very simple method for gathering information about the potential performance of a program, and it allows developers to reuse benchmark measurements for applications using the same archetype. Recall the restricted goal: We require accuracy of the analytic model and simulation infrastructure only to the extent that they suggest directions for the programmer to make appropriate optimizations.

Once the relevant routines are benchmarked, the programmer can use the results in the PERFORMANCE MODEL phase (path (d) in Figure 1) as well as in the SIMULATION phase (path (e) in Figure 1). These two phases can be done concurrently if both are desired. However, as our experiments will show, usually the PERFORMANCE MODEL phase is sufficient (without the SIMULATION phase) for predicting program efficiency and for doing the corresponding performance tuning.

Performance Model. The PERFORMANCE MODEL phase consists of two steps:

1. *Analysis* of the program to produce a closed-form equation involving the benchmarked quantities, and

2. *Instantiation* of the equation with the appropriate benchmarked values to give a number representing a prediction of the program's expected running time.

We call the methodology of developing the program concurrently with modeling its performance ADAPT, for Application Development using Analytic Performance Tuning [Rif96].

The *Analysis* segment of ADAPT involves decomposing the given program into a number of subprograms (e.g., initialization, computational loop, and termination) whose running times can be expressed in terms of the benchmark numbers. The finer the grain of decomposition and benchmarking, the more predictive we expect the model equation to be for that program.

The basis for this decompositional approach to performance modeling is a structured induction [Rif96] on the statements of the program being modeled, assuming implicit barriers between any subprograms. For example, for a program

S that consists of program S_1 (which may involve a number of computations and communications) composed in sequence with program S_2 (which also may involve a number of computations and communications), we assume an implicit barrier between S_1 and S_2:

$$S = S_1; S_2$$

For the base case in which S_1 and S_2 each consist of either a single computation, using one or more of the given processors, or a (possibly collective) communication operation also using one or more of the given processors, we can model the expected running time $\mathcal{R}(S)$ of program S as follows: S_2:

$$\mathcal{R}(S) = \mathcal{R}(S_1) + \mathcal{R}(S_2)$$

Since S_1 consists of a single computation or communication, we model $\mathcal{R}(S_1)$ as the maximum of the expected running times of that computation or communication on all of the processors. If $\mathcal{R}_p(S_1)$ is the expected running time of S_1 on processor p, we can model $\mathcal{R}(S_1)$ thus:

$$\mathcal{R}(S_1) = \max_{\forall p} \mathcal{R}_p(S_1)$$

We can model the expected running time of $\mathcal{R}(S_2)$ similarly; as a result, we have:

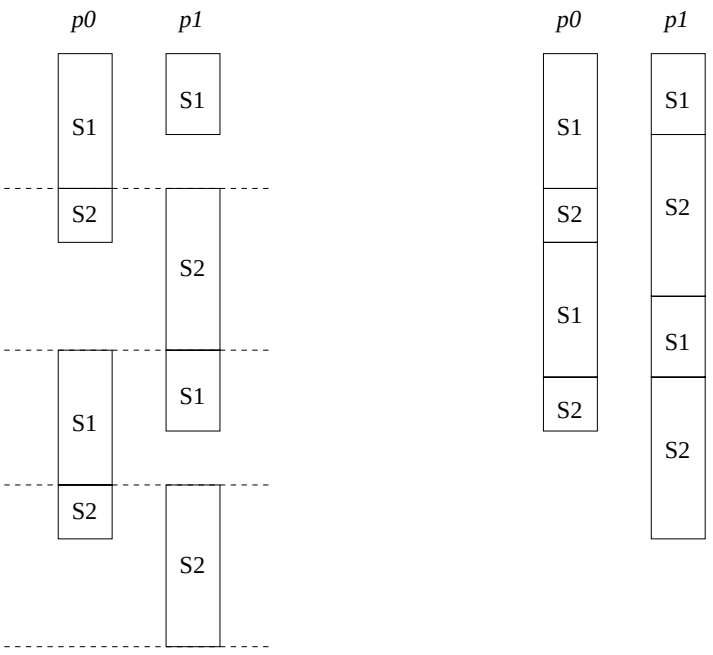
$$\mathcal{R}(S) = \max_{\forall p} \mathcal{R}_p(S_1) + \max_{\forall p} \mathcal{R}_p(S_2)$$

The structured induction thus allows us to compute the expected running time of a large program from the expected running times of its components. For example, having derived a closed-form equation for $\mathcal{R}(S)$, we can use it to compute expected running of a program T that consists of two executions of $\mathcal{R}(S)$ in sequence:

$$\begin{aligned} \mathcal{R}(T) &= \mathcal{R}(S) + \mathcal{R}(S) \\ &= 2 \times \left(\max_{\forall p} \mathcal{R}_p(S_1) + \max_{\forall p} \mathcal{R}_p(S_2) \right) \end{aligned}$$

Part (a) of Figure 2 illustrates how this equation models running time on two processors. Because the model uses implicit barriers, we expect that it will yield conservative or pessimistic performance estimates (i.e., predicted execution times possibly greater than actual execution times), as illustrated in part (b) of the figure. We can derive a similar equation for a program that consists of NSTEPS iterations of S:

$$\begin{aligned} \mathcal{R}(T) &= \left(\sum_{i=1}^{\text{NSTEPS}} \mathcal{R}(S) \right) \\ &= \text{NSTEPS} \times \left(\max_{\forall p} \mathcal{R}_p(S_1) + \max_{\forall p} \mathcal{R}_p(S_2) \right) \end{aligned}$$



(a) Execution time predicted using implicit barriers. (b) Possible actual execution time.

Figure 2: Predicted versus actual execution times for program S_1; S_2; S_1; S_2 on two processors. (a) illustrates how our model predicts execution times for using implicit barriers between program units. (b) illustrates a possible actual execution scenario, if in fact barriers are not needed.

We demonstrate the use of this simple performance model in Sections 3, 4, and 5.

The *Instantiation* segment of ADAPT is simply the "plugging in" of benchmark numbers into the closed-form equations developed during the *Analysis* segment, either manually or via an automated tool.

The PERFORMANCE MODEL phase can (but need not) be done concurrently with the SIMULATION phase. With or without the supplementary simulations, ADAPT can guide the programmer in making decisions about data distributions and granularity during the REFINEMENT phase (path (f) in Figure 1).

Simulation. The SIMULATION of a program consists of writing a simulation program based on the actual application program being modeled. This phase supplements the PERFORMANCE MODEL phase, in cases in which the programmer would like to consider additional factors before making data partitioning and granularity decisions for large program runs.

We call the methodology of developing the program while using the performance model with a simulation architecture ADEPT, for Application Development using Experimental Performance Tuning [Rif96]. Like the performance model, these simulations can help guide a programmer in making decisions about data distribution and granularity during the REFINEMENT phase (path (g) in Figure 1).

Briefly, setting up a simulation works as follows. Normally, each routine being benchmarked in the BENCHMARKING phase is timed repeatedly and the results are combined into an average execution time for the routine. If simulation is to be done, however, rather than simply averaging the results the programmer records their distribution. He or she then writes a program analogous to the application program, with the actual application program statements replaced by the generation of estimated running times based on the distributions observed during benchmarking. Rather than computing the results of the application, the simulation computes the expected running time of the application; this can be done quickly on a single processor as many times as the user desires.

Refinement. In the REFINEMENT phase, choices regarding data distribution and granularity are reconsidered based on expected running times as computed in the PERFORMANCE MODEL phase. Using ADAPT and ADEPT, the programmer can return to the APPLICATION phase (path (h) in Figure 1) to improve the efficiency of the application if necessary. The performance model (and simulation strategy) may suggest a decision between archetypes (Section 5.1), architectures (Section 5.2), or libraries (Section 5.3).

2.2 Experimental Method

We use a small suite of application programs developed using two different archetypes to explore the PERFORMANCE MODEL phase of the methodology described in Section 2.1. This section describes our experimental method.

System specifications. Our experiments were conducted using various combinations of two different archetypes (mesh and mesh-spectral), two different architectures (an IBM SP2 at Argonne National Labs using a straight interconnect, and a network of 166 MHz Pentium personal computers connected by 100Mbps Ethernet), and two different languages/libraries (Fortran M and Fortran with MPI).

Fortran M [FC95] consists of a small set of extensions to Fortran for modular parallel programming. In Fortran M, tasks and channels are represented

explicitly, allowing the design of structured, unstructured, and asynchronous communication patterns for task-parallel programs. In addition, Fortran M gives control over the mapping of tasks to processors. We use the TCP/IP-based implementation of Fortran M for our Fortran-M based programs.

MPI [Mes94, SOHL+96], the Message Passing Interface, is a standard, portable message-passing system that defines the syntax and semantics of a package of library routines useful to a wide range of applications written in Fortran or C. Several free, well-tested, efficient implementations of MPI exist, both for distributed memory multicomputers and networks of personal computers and workstations.

Environment. Experiments were performed on otherwise unloaded computer nodes, with one application process per node, but in an environment in which communications hardware was also supporting other users. Since execution times were consistent across multiple runs, we assume that this sharing of communications hardware did not greatly affect our results.

Measurement of execution times. We measured two kinds of execution times:

- Elapsed "total" time, measured using the Unix `time` command, includes the time required to start the processes.
- Elapsed "process" time, measured by calling the Unix `gettimeofday` system function from within each process, does not include any overhead associated with starting and ending processes.

That is, "total" time is measured from program initiation to program termination, while "process" time is measured from process initiation to process termination. Note that we do not measure elapsed "computational kernel" times, which might show more scalability for our algorithms.

Averaging. Measurements are averaged over several trials, with high and low outliers discarded. Every experiment is done at least twice to verify the consistency of the results.

Presentation of results. We provide tables containing benchmark measurements, and graphs illustrating observed running times versus those computed using the performance model. In the tables, times are rounded to the nearest integer, so very small times are shown are zero. We plot execution times rather than speedups; each plot shows the following:

- *Ideal* time is sequential execution time (on 1 processor) divided by number of processors — that is, time required for a program with ideal speedup.

- *Actual* time is observed time as measured by our experiments.
- *Expected* time is calculated using the appropriate performance model and the results of our benchmark experiments.

The full text of the experimental parallel programs, sequential programs, and benchmark programs are presented in Appendix A and Appendix B.

3 Mesh Applications

In an application based on the mesh archetype [Mas96], data is based on an N-dimensional grid ($N = 1$, 2, or 3), with one or more variables per cell (grid point), and computation consists of some sequence of the following operations:

- Computing, for each cell, new values for one or more variables, based on old values of variables in that cell and nearby cells (for example, neighbors or next-to-neighbors).
- (Optionally) reading in values for a grid variable.
- (Optionally) writing out values for a grid variable.
- (Optionally) computing a global reduction (for example, global maximum or global sum) over the whole grid.

Frequently the compute-new-values and reduction operations are performed repeatedly in a time-step loop. Figure 3 illustrates the basic operation of computing new values in terms of old values, in a two-dimensional grid.

Mesh computations are readily parallelized for distributed-memory architectures using the following approach: The N-dimensional grid is distributed over an N-dimensional grid of processes; computation of new values for grid variables is similarly distributed. A separate (optional) host process is used for reads/writes involving a whole array. Non-grid variables (for example, global constants and reduction variables) are duplicated in each process and their values are kept consistent. This approach is discussed by Massingill [Mas96], including details about how to parallelize sequential code and about how to build an application program from the archetype-provided code template and library. The library includes routines that encapsulate the necessary communication operations (host-to-grid and grid-to-host redistribution, boundary exchange, reductions, and broadcast) and a number of utility routines for index manipulation and other housekeeping. This archetype code (template and library) has been implemented in Fortran M, Fortran with Intel's NX Library, and Fortran with p4 [BL94]. All implementations have essentially the same application programmer interface, so applications developed using one implementation are trivially ported to another.

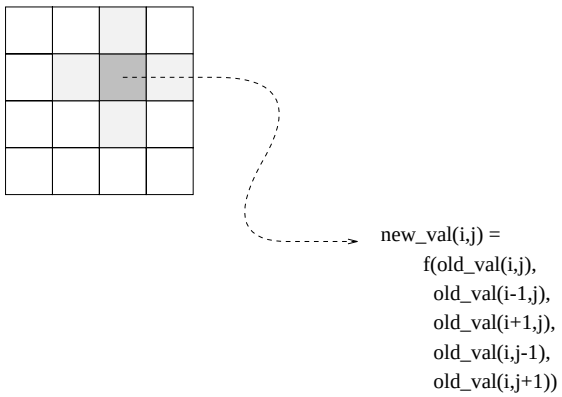


Figure 3: Basic mesh computation.

We note that for the two mesh archetype applications given in Sections 3.1 and 3.2, the total process count includes a host process for performing I/O, which affects performance. There is also a no-host-process version of the mesh archetype, but doing I/O with that version is somewhat more complicated, and in the applications described in this paper we chose programming simplicity over performance where such trade-offs had to be made.

3.1 Heat Diffusion

The heat diffusion application [Mas96] solves the one-dimensional heat diffusion equation:

$$\frac{\partial U}{\partial t} = \frac{\partial^2 U}{\partial x^2}$$

using the approximation:

$$\frac{U(x_i, t_{k+1}) - U(x_i, t_k)}{\Delta t} = \frac{U(x_{i+1}, t_k) - 2U(x_i, t_k) + U(x_{i-1}, t_k)}{\Delta x^2}$$

A sequential program for this computation is straightforward. It maintains two copies of variable U, one for the current time step (`uk`) and one for the next time step (`ukp1`). At each time step, it computes the values of `ukp1` based on the values of `uk`. The two boundary points are handled differently; they maintain a constant value.

An equivalent parallel program using the mesh archetype is similar: Grid-based variables `uk` and `ukp1` are distributed among grid processes. Each local section is surrounded by a "ghost boundary" of width one, to be used to hold

values from neighboring processes. The whole array is initialized in the host process and then copied to the grid processes. (It could also be initialized directly in the grid processes; this approach was chosen for simplicity.) At each time step, the ghost boundaries are updated (by calling the archetype's boundary-exchange routine) before they are used in the grid computation. The special handling for the (global) boundary points is provided by using an archetype library routine to determine which points in each local section are in the interior of the global array. The grid values are then copied back to the host process for printing. The code executed by the host and grid processes has the same high-level structure; both execute the time-step loop, for example. This ensures that proper synchronization is maintained. Both programs appear in Appendix A.1.

Benchmarking. The computational benchmark measures values for the following times: $\mathcal{T}_{\text{overhead}}$ (start and terminate process), $\mathcal{T}_{\text{init}}$ (initialize grid values), $\mathcal{T}_{\text{comp}}$ (calculate new values for all grid points), and $\mathcal{T}_{\text{output}}$ (output results). Results are given in Table 1. Observe that results for this benchmark are independent of the choice of archetype implementation.

Measurement	Time (msecs)
$\mathcal{T}_{\text{overhead}}$	150
$\mathcal{T}_{\text{init}}$	27
$\mathcal{T}_{\text{comp}}$	124
$\mathcal{T}_{\text{output}}$	15

Table 1: Results of computational benchmark for the mesh heat diffusion application, running on a single node of the IBM SP2 using Fortran. Grid size is 640,000 points. Times are in milliseconds.

The communication benchmark measures values for the following times: $\mathcal{T}_{\text{overhead}}$ (start and terminate processes), $\mathcal{T}_{\text{HtoG}}$ (redistribute data, host to grid), $\mathcal{T}_{\text{xintersect}}$ (compute appropriate local indices), $\mathcal{T}_{\text{update\_bdry}}$ (update ghost boundaries by exchanging data with neighboring processes), and $\mathcal{T}_{\text{GtoH}}$ (redistribute data, grid to host). We ran this benchmark on 1, 2, 4, 8, 16, and 32 processors (plus a "host" processor, as described earlier). Results are given in Table 2.

The computational and communication benchmark programs appear in Appendix A.1.

Performance Model. We use our performance model and the program, given in Appendix A.1, to compute estimated running time in terms of the preceding

Measurement	Time (msecs) on n nodes, not including host node					
	$n=1$	$n=2$	$n=4$	$n=8$	$n=16$	$n=32$
$\mathcal{T}_{\text{overhead}}$	8650	9980	14330	16230	24480	68130
$\mathcal{T}_{\text{HtoG}}$	556	649	935	940	991	1048
$\mathcal{T}_{\text{xintersect}}$	0	0	0	0	0	0
$\mathcal{T}_{\text{update\_bdry}}$	0	6	8	9	9	9
$\mathcal{T}_{\text{GtoH}}$	530	533	549	553	516	435

Table 2: Results of communication benchmark for the mesh heat diffusion application, running on the specified number of nodes (plus a "host" node) on the IBM SP2 using Fortran M, without the crossbar switch. Grid size is 640,000 points. Times are in milliseconds.

list of benchmark values and two additional program parameters — NSTEPS (number of loop iterations) and XPROCS (number of grid processes) — as follows. First, a high-level decomposition gives us values for $\mathcal{T}_{\text{elapsed}}$ (total estimated elapsed time) and $\mathcal{T}_{\text{process}}$ (total estimated process time, excluding process-setup overhead):

$$\begin{aligned} \mathcal{T}_{\text{elapsed}} &= \mathcal{T}_{\text{process}} + \mathcal{T}_{\text{overhead}} \\ \mathcal{T}_{\text{process}} &= \mathcal{T}_{\text{startup}} + \mathcal{T}_{\text{computation}} + \mathcal{T}_{\text{finish}} \end{aligned}$$

We can then write down equations for each term on the right-hand side of the above equations based on applying our performance model to the application programs as previously described. For the sequential version, the equations are as follows:

$$\begin{aligned} \mathcal{T}_{\text{startup}} &= \mathcal{T}_{\text{init}} \\ \mathcal{T}_{\text{computation}} &= \text{NSTEPS} \times \mathcal{T}_{\text{comp}} \\ \mathcal{T}_{\text{finish}} &= \mathcal{T}_{\text{output}} \end{aligned}$$

For the parallel version, the equations reflect the division of computation among processes and also the inclusion of communication and housekeeping routines, as follows:

$$\begin{aligned} \mathcal{T}_{\text{startup}} &= \mathcal{T}_{\text{init}} + \mathcal{T}_{\text{HtoG}} + \mathcal{T}_{\text{xintersect}} \\ \mathcal{T}_{\text{computation}} &= \text{NSTEPS} \times \left(\frac{\mathcal{T}_{\text{comp}}}{\text{XPROCS}} + \mathcal{T}_{\text{update\_bdry}} \right) \\ \mathcal{T}_{\text{finish}} &= \mathcal{T}_{\text{GtoH}} + \mathcal{T}_{\text{output}} \end{aligned}$$

Experimental Results. For this experiment we used the following values of the program parameters:

$$\text{NSTEPS} = 2000$$
$$\text{XPROCS} = n$$

where n is the number of grid (non-"host") processors (1, 2, 4, 8, 16, or 32). Table 3 and Figures 4 and 5 compare predicted with observed times. For this experiment, predicted times generally agreed well with observed times, with predicted times being, as we expected, somewhat conservative. Our model also correctly predicts the scalability of the application, validating its utility in helping programmers choose granularity.

	Time (secs) on n nodes, not including host node					
	$n=1$	$n=2$	$n=4$	$n=8$	$n=16$	$n=32$
Expected Elapsed Time	258	147	94	66	59	96
Actual Elapsed Time	237	130	76	54	43	48
Expected Process Time	249	137	79	50	35	27
Actual Process Time	231	123	67	39	24	19

Table 3: Execution times for the mesh heat diffusion application, running on the specified number of nodes (plus a "host" node) on the IBM SP2 using Fortran M, without the crossbar switch. Problem size is 640,000 grid points and 2000 steps. Times are in seconds. See Figures 4 and 5 for corresponding graphs.

3.2 Poisson Solver

This application [Mas96], based on the discussion of the Poisson problem by Van de Velde [VdV94], solve the equation

$$-\frac{\partial^2 U}{\partial x^2} - \frac{\partial^2 U}{\partial y^2} = f(x,y)$$

with Dirichlet boundary condition

$$u(x,y) = g(x,y)$$

using Jacobi iteration; that is, by discretizing the problem domain and applying the following operation to all interior points until convergence is reached:

$$4u_{(i,j)}^{(k+1)} = h^2 f_{i,j} + u_{(i-1,j)}^{(k)} + u_{(i+1,j)}^{(k)} + u_{(i,j-1)}^{(k)} + u_{(i,j+1)}^{(k)}$$

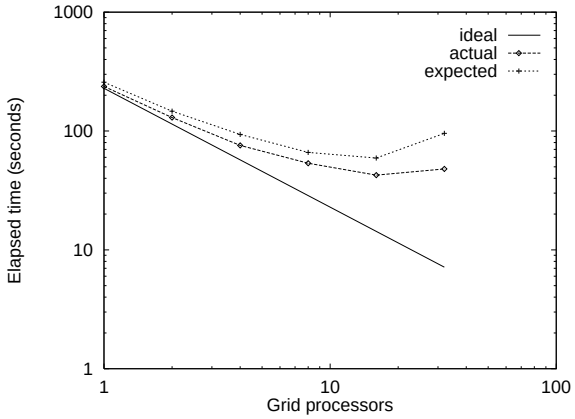


Figure 4: Elapsed times for the mesh heat equation application, running on the specified number of nodes (plus a "host" node) on the IBM SP2 using Fortran M, without the crossbar switch. Problem size is 640,000 grid points and 2000 steps. Times are in seconds. See Table 3 for corresponding table.

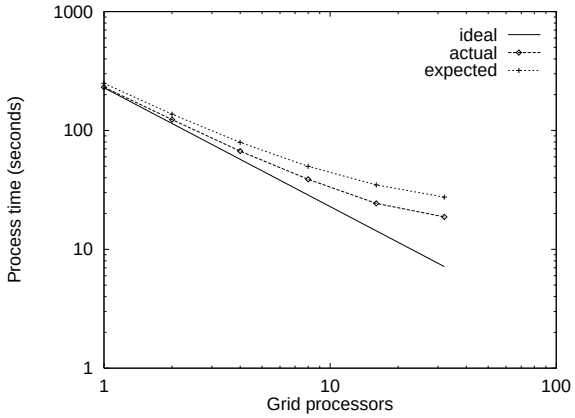


Figure 5: Process times for the mesh heat equation application, running on the specified number of nodes (plus a "host" node) on the IBM SP2 using Fortran M, without the crossbar switch. Problem size is 640,000 grid points and 2000 steps. Times are in seconds. See Table 3 for corresponding table.

Convergence is said to be reached when the maximum of

$$|u_{(i,j)}^{(k+1)} - u_{(i,j)}^{(k)}|$$

falls below a specified tolerance.

A sequential program for this computation maintains two copies of variable u, one for the current iteration (`uk`) and one for the next iteration (`ukp1`). At each iteration, it computes the values of `ukp1` based on the values of `uk`. The boundary points are handled differently; they maintain a constant value. Every `NCHECK` the maximum difference between `uk` and `uk` is computed to check for convergence. At each step, values are copied back from `ukp1` to `uk` (for the sake of simplicity, at a modest cost in performance).

An equivalent parallel program using the mesh archetype is similar: Grid-based variables `uk` and `ukp1` are distributed among grid processes. Each local section is surrounded by a "ghost boundary" of width one, to be used to hold values from neighboring processes. The whole grid is initialized in the host process and then copied to the grid processes. (It could also be initialized directly in the grid processes; this approach was chosen for simplicity.) At each time step, the ghost boundaries are updated (by calling the archetype's boundary-exchange routine) before they are used in the grid computation. The special handling for the (global) boundary points is provided by using archetype library routines to determine which points in the local section are in the interior of the global array. Computing a global maximum for the convergence test is accomplished by computing a local maximum in each grid process and then calling an archetype library routine to find the global maximum. When convergence is reached (or `MAXSTEPS` iterations have been performed), grid values are copied back to the host process for printing. The code executed by the host and grid processes has the same high-level structure; both execute the main loop, for example, including the convergence test. This ensures that proper synchronization is maintained. Both programs appear in Appendix A.2.

Note that this problem can also be solved using the mesh-spectral archetype, as described in Section 4.2. We compare the performances of the two implementations (mesh and mesh-spectral) in Section 5.1.

Benchmarking. The computational benchmark measures values for the following times: $\mathcal{T}_{\text{overhead}}$ (start and terminate process), $\mathcal{T}_{\text{init}}$ (initialize grid values), $\mathcal{T}_{\text{comp}}$ (calculate new values for all grid points), $\mathcal{T}_{\text{check\_converge}}$ (check for convergence), $\mathcal{T}_{\text{copy\_values}}$ (copy new values back to `uk`), and $\mathcal{T}_{\text{output}}$ (output results). Results are given in Table 4. Observe that results for this benchmark are independent of the choice of archetype implementation.

The communication benchmark measures values for the following times: $\mathcal{T}_{\text{overhead}}$ (start and terminate processes), $\mathcal{T}_{\text{iglobal}}$ (index manipulation), $\mathcal{T}_{\text{jglobal}}$ (index manipulation), $\mathcal{T}_{\text{GtoH}}$ (redistribute data, grid to host). $\mathcal{T}_{\text{HtoG}}$ (redistribute data, host to grid), $\mathcal{T}_{\text{merge\_real\_maxabs}}$ (merge local maxima into global

Measurement	Time (msecs)
$\mathcal{T}_{\text{overhead}}$	100
$\mathcal{T}_{\text{init}}$	247
$\mathcal{T}_{\text{comp}}$	430
$\mathcal{T}_{\text{check\_converge}}$	128
$\mathcal{T}_{\text{copy\_values}}$	45
$\mathcal{T}_{\text{output}}$	15

Table 4: Results of computational benchmark for the mesh Poisson solver application, running on a single node of the IBM SP2 using Fortran. Grid size is 800 by 800 points. Times are in milliseconds.

maximum), $\mathcal{T}_{\text{update\_bdry}}$ (update ghost boundaries by exchanging data with neighboring processes), $\mathcal{T}_{\text{xintersect}}$ (index manipulation), and $\mathcal{T}_{\text{yintersect}}$ (index manipulation). We ran this benchmark on 1, 4, 9, 16, 25, and 36 processors (plus a "host" processor, as described earlier). Results are given in Table 5.

	Time (msecs) on n nodes, not including host node					
Measurement	$n=1$	$n=4$	$n=9$	$n=16$	$n=25$	$n=36$
$\mathcal{T}_{\text{overhead}}$	6	8	14	18	33	37
$\mathcal{T}_{\text{iglobal}}$	0	0	0	0	0	0
$\mathcal{T}_{\text{jglobal}}$	0	0	0	0	0	0
$\mathcal{T}_{\text{GtoH}}$	618	630	626	697	667	639
$\mathcal{T}_{\text{HtoG}}$	665	1103	1116	1211	1275	1409
$\mathcal{T}_{\text{merge\_real\_maxabs}}$	7	52	69	83	121	177
$\mathcal{T}_{\text{update\_bdry}}$	0	11	17	18	25	21
$\mathcal{T}_{\text{xintersect}}$	0	0	0	0	0	0
$\mathcal{T}_{\text{yintersect}}$	0	0	0	0	0	0

Table 5: Results of communication benchmark for the mesh Poisson solver application, running on the specified number of nodes (plus a "host" node) on the IBM SP2 using Fortran M, without the crossbar switch. Grid size is 800 by 800 points. Times are in milliseconds.

The computational and communication benchmark programs appear in Ap-

pendix A.2.

Performance Model. We use our performance model and the program, given in Appendix A.2, to compute estimated running time in terms of the preceding list of benchmark values and a few additional program parameters — NSTEPS (number of loop iterations), NCHECK (frequency of convergence checking), and XPROCS and YPROCS (dimensions of process grid, implying a total of XPROCS × YPROCS grid processes) — as follows First, a high-level decomposition gives us values for $\mathcal{T}_{\text{elapsed}}$ (total estimated elapsed time) and $\mathcal{T}_{\text{process}}$ (total estimated process time, excluding process-setup overhead):

$$\begin{aligned}
\mathcal{T}_{\text{elapsed}} &= \mathcal{T}_{\text{process}} + \mathcal{T}_{\text{overhead}} \\
\mathcal{T}_{\text{process}} &= \mathcal{T}_{\text{startup}} + \mathcal{T}_{\text{computation}} + \mathcal{T}_{\text{check}} + \mathcal{T}_{\text{copy}} + \mathcal{T}_{\text{finish}}
\end{aligned}$$

We can then write down equations for each term on the right-hand side of the above equations based on applying our performance model to the application programs as previously described. For the sequential version, the equations are as follows:

$$\begin{aligned}
\mathcal{T}_{\text{startup}} &= \mathcal{T}_{\text{init}} \\
\mathcal{T}_{\text{computation}} &= \text{NSTEPS} \times \mathcal{T}_{\text{comp}} \\
\mathcal{T}_{\text{check}} &= \frac{\text{NSTEPS}}{\text{NCHECK}} \times \mathcal{T}_{\text{check_converge}} \\
\mathcal{T}_{\text{copy}} &= \text{NSTEPS} \times \mathcal{T}_{\text{copy_values}} \\
\mathcal{T}_{\text{finish}} &= \mathcal{T}_{\text{output}}
\end{aligned}$$

For the parallel version, the equations reflect the division of computation among processes and also the inclusion of communication and housekeeping routines, as follows:

$$\begin{aligned}
\mathcal{T}_{\text{startup}} &= \mathcal{T}_{\text{init}} + \mathcal{T}_{\text{HtoG}} + \mathcal{T}_{\text{xintersect}} + \mathcal{T}_{\text{yintersect}} + \mathcal{T}_{\text{iglobal}} + \mathcal{T}_{\text{jglobal}} \\
\mathcal{T}_{\text{computation}} &= \text{NSTEPS} \times \left(\frac{\mathcal{T}_{\text{comp}}}{\text{XPROCS} \times \text{YPROCS}} + \mathcal{T}_{\text{update_bdry}} \right) \\
\mathcal{T}_{\text{check}} &= \frac{\text{NSTEPS}}{\text{NCHECK}} \times \left(\frac{\mathcal{T}_{\text{check_converge}}}{\text{XPROCS} \times \text{YPROCS}} + \mathcal{T}_{\text{merge_real_maxabs}} \right) \\
\mathcal{T}_{\text{copy}} &= \text{NSTEPS} \times \left(\frac{\mathcal{T}_{\text{copy_values}}}{\text{XPROCS} \times \text{YPROCS}} \right) \\
\mathcal{T}_{\text{finish}} &= \mathcal{T}_{\text{GtoH}} + \mathcal{T}_{\text{output}}
\end{aligned}$$

Experimental Results. For this experiment we used the following values of the program parameters:

$$\text{NSTEPS} = 1000$$
$$\text{NCHECK} = 10$$
$$\text{XPROCS} = \text{YPROCS} = \sqrt{n}$$

where n is the number of grid (non-"host") processors (1, 4, 9, 16, 25, or 36). Table 6 and Figures 6 and 7 compare predicted with observed times. For this experiment, predicted times generally agreed fairly well with observed times, with predicted times being, as we expected, somewhat conservative. Our model did less well for this application than for the heat equation application in predicting scalability, but it still came fairly close.

	Time (secs) on n nodes, not including host node					
	$n = 1$	$n = 4$	$n = 9$	$n = 16$	$n = 25$	$n = 36$
Expected Elapsed Time	496	149	94	78	91	91
Actual Elapsed Time	522	148	87	69	58	62
Expected Process Time	490	141	80	59	59	54
Actual Process Time	517	140	73	47	34	32

Table 6: Execution times for the mesh Poisson solver application, running on the specified number of nodes (plus a "host" node) on the IBM SP2 using Fortran M, without the crossbar switch. Problem size is 800 by 800 grid points and 1000 steps. Times are in seconds. See Figures 6 and 7 for corresponding graphs.

4 Mesh-Spectral Applications

In an application written using the mesh archetype [DM96]: Data is based on three-dimensional grids (arrays), with one- and two-dimensional grids considered as special cases of three-dimensional grids; a computation may contain multiple grids of different dimensions. Computation consists of some sequence of the following operations:

- Neighbor operations in which new values are computed for each point in a grid based on values at that point and nearby points.
- Row operations, in which new values are computed for each point in a grid based on values in the same row.

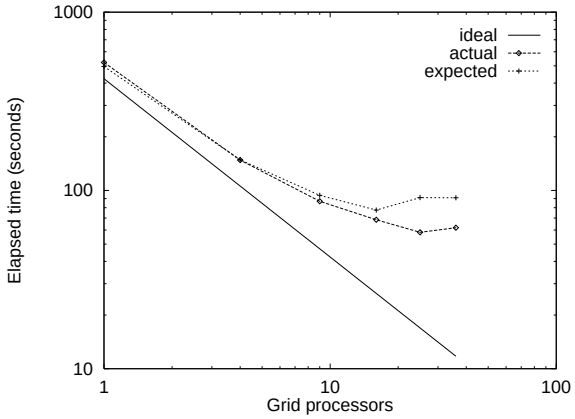


Figure 6: Elapsed times for the mesh Poisson solver application, running on the specified number of nodes (plus a "host" node) on the IBM SP2 using Fortran M, without the crossbar switch. Problem size is 800 by 800 grid points and 1000 steps. Times are in seconds. See Table 6 for corresponding table.

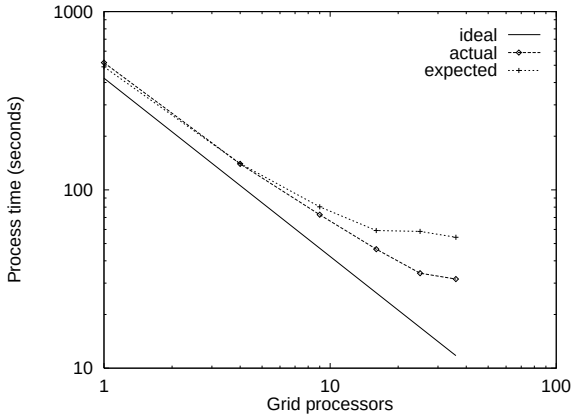


Figure 7: Process times for the mesh Poisson solver application, running on the specified number of nodes (plus a "host" node) on the IBM SP2 using Fortran M, without the crossbar switch. Problem size is 800 by 800 grid points and 1000 steps. Times are in seconds. See Table 6 for corresponding table.

- Column operations, defined analogously.
- Reduction operations over a grid (for example., global maximum).

Figures 8 and 9 illustrate two of these operations (a neighbor operation and a row operation respectively) in a two-dimensional grid.

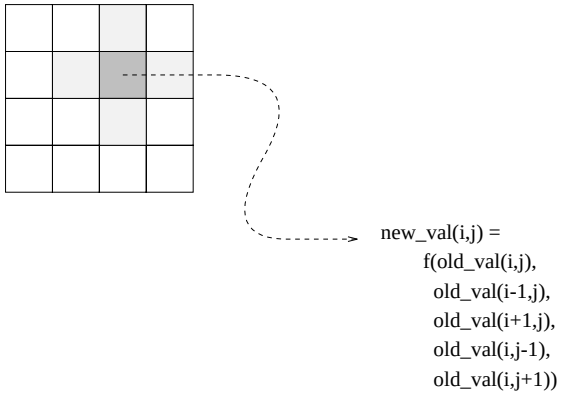


Figure 8: Neighbor operation.

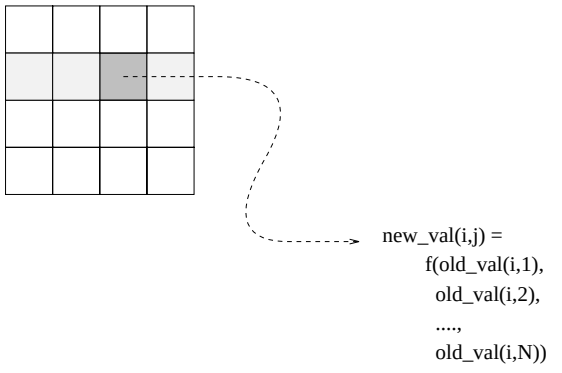


Figure 9: Row operation.

Mesh-spectral computations are readily parallelized using the following approach: The overall structure of the computation is based on the SPMD (Single

Program, Multiple Data) model; that is, it consists of some number N of processes all executing the same program, each on its own data. Each 3-dimensional data grid is distributed over the processes based on a 3-dimensional *process grid* of some or all of the N processes; computation of new values for grid variables is similarly distributed. In the course of a computation, a data grid can be redistributed (that is, the process grid over which it is distributed can be changed); this is usually done when one distribution is convenient for part of the computation and a different distribution is convenient for another part of the computation. Non-grid variables (for example, global constants and reduction variables) are duplicated in each process; their values are kept consistent. This approach is discussed by Massingill and Davis [DM96], including details about how to parallelize sequential code and about how to build an application program from the archetype-provided code template and library. The library includes routines that encapsulate the necessary communication operations (redistribution, boundary exchange, reductions, and broadcast) and a number of utility routines for index manipulation and other housekeeping. This archetype code (template and library) has been implemented in Fortran M and Fortran with MPI. All implementations have essentially the same application programmer interface, so applications developed using one implementation are trivially ported to another.

4.1 Two-dimensional Fast Fourier Transform

This application [DM96] performs a two-dimensional FFT in place. As described in *Numerical Recipes* [PFTV86], computing a two-dimensional FFT in place is accomplished by performing a one-dimensional FFT on each row of a two-dimensional array, and then performing a one-dimensional FFT on each column of the resulting two-dimensional array. Optimality of the 2D FFT depends largely on the choice of algorithm (and implementation) for the 1D FFT.

In our application, the actual FFTs are performed using a sequential subroutine library that allows the computation of FFTs on a set of vectors with a single subroutine call. The sequential version of the application is straightforward (first use the library subroutine to perform 1D FFTs on each row, and then use it to perform 1D FFTs on each column. A parallel version based on the mesh-spectral archetype is not much more complicated: In order to perform the FFT computations using the same sequential subroutine library, the program employs two distributions for the two-dimensional array on which the FFT is to be performed: a distribution by rows (which, for each row, puts all data in a single process, allowing it to be processed with a sequential FFT subroutine), and a distribution by columns (which has the same effect on columns). Data is initially distributed by rows; after the FFT-by-rows is performed, it is redistributed by columns and the FFT-by-columns is performed. It is then redistributed by rows before being written out. The FFT computation (calculation by rows, redistribution, calculation by columns, and then redistribution

again) is repeated several times to reduce the proportion of total application time spent on I/O.

Our 1D FFT code was written by Clive Temperton for the Meteorological Office in England. The code was originally designed for vector machines like the Cray; today, the library is widely available at all supercomputer centers. Note that the details of the one-dimensional FFT implementation are not relevant to the parallelization, and while they affect performance, we use the same one-dimensional FFT in both the sequential and parallel programs. Thus, overall performance could be improved by choosing a faster 1D FFT, without changing the parallel aspects of the code.

We note that [PFTV86] is not the most efficient implementation of an FFT, but it is well-understood and easily implemented using the mesh-spectral archetype; in this paper, we use this algorithm primarily to illustrate the performance model, rather than attempt to achieve the fastest possible FFT (as is the focus of other work, such as [Win78]). Duhamel and Vetterli provide an excellent survey of FFTs [DV90]. A good comparison of the FFT algorithm we use with more efficient ones (such as a split-radix algorithm) on a vanilla workstation is given in [Arn96] (although, with a multicomputer, a simpler butterfly structure might be better for more actual computation [Har96]).

Benchmarking. The computational benchmark measures values for the following times: $\mathcal{T}_{\text{overhead}}$ (start and terminate process), $\mathcal{T}_{\text{read\_fft}}$ (set up grid and read input data), $\mathcal{T}_{\text{init}}$ (initialize for FFT), $\mathcal{T}_{\text{row\_fft}}$ (perform FFTs on rows), $\mathcal{T}_{\text{col\_fft}}$ (perform FFTs on columns), and $\mathcal{T}_{\text{write\_fft}}$ (write output data). Results are given in Table 7. Observe that results for this benchmark are independent of the choice of archetype implementation.

Measurement	Time (msecs)
$\mathcal{T}_{\text{overhead}}$	2800
$\mathcal{T}_{\text{read\_fft}}$	16161
$\mathcal{T}_{\text{init}}$	3
$\mathcal{T}_{\text{row\_fft}}$	2854
$\mathcal{T}_{\text{col\_fft}}$	3335
$\mathcal{T}_{\text{write\_fft}}$	12934

Table 7: Results of computational benchmark for the mesh-spectral 2D FFT application, running on a single node of the IBM SP2 using Fortran. Grid size is 800 by 800 points. Times are in milliseconds.

The communication benchmark measures values for the following times:

$\mathcal{T}_{\text{overhead}}$ (start and terminate processes), $\mathcal{T}_{\text{col\_to\_row}}$ (redistribute data, columns to rows), $\mathcal{T}_{\text{row\_to\_col}}$ (redistribute data, rows to columns), $\mathcal{T}_{\text{data\_widths}}$ (housekeeping), $\mathcal{T}_{\text{local\_pos}}$ (housekeeping), $\mathcal{T}_{\text{set\_mesh}}$ (set up data grid), $\mathcal{T}_{\text{read\_mesh}}$ (perform communication associated with reading data), and $\mathcal{T}_{\text{write\_mesh}}$ (perform communication associated with writing data). We ran this benchmark on 1, 2, 4, 8, 16, and 32 processors. Results are given in Table 8.

	Time (msecs) on n nodes					
Measurement	$n=1$	$n=2$	$n=4$	$n=8$	$n=16$	$n=32$
$\mathcal{T}_{\text{overhead}}$	3930	4430	6030	9400	17130	32180
$\mathcal{T}_{\text{col\_to\_row}}$	3197	1669	660	303	145	61
$\mathcal{T}_{\text{row\_to\_col}}$	3195	1856	1103	1924	1606	1325
$\mathcal{T}_{\text{data\_widths}}$	0	0	0	0	0	0
$\mathcal{T}_{\text{local\_pos}}$	0	0	0	0	0	0
$\mathcal{T}_{\text{set\_mesh}}$	0	0	0	0	0	0
$\mathcal{T}_{\text{read\_mesh}}$	619	435	344	304	287	289
$\mathcal{T}_{\text{write\_mesh}}$	634	423	377	352	350	371

Table 8: Results of communication benchmark for the mesh-spectral 2D FFT application, running on the specified number of nodes on the IBM SP2 using Fortran with MPI, without the crossbar switch. Grid size is 800 by 800 points. Times are in milliseconds.

The computational and communication benchmark programs appear in Appendix B.1.

Performance Model. We use our performance model and the program, given in Appendix B.1, to compute estimated running time in terms of the preceding list of benchmark values and two additional program parameters — NREPEATS (number of times to repeat the FFT) and NPROCS (number of processes) — as follows. First, a high-level decomposition gives us values for $\mathcal{T}_{\text{elapsed}}$ (total estimated elapsed time) and $\mathcal{T}_{\text{process}}$ (total estimated process time, excluding process-setup overhead):

$$\begin{aligned} \mathcal{T}_{\text{elapsed}} &= \mathcal{T}_{\text{process}} + \mathcal{T}_{\text{overhead}} \\ \mathcal{T}_{\text{process}} &= \text{NREPEATS} \times (\mathcal{T}_{\text{startup}} + \mathcal{T}_{\text{computation}} + \mathcal{T}_{\text{finish}}) \end{aligned}$$

We can then write down equations for each term on the right-hand side of the above equations based on applying our performance model to the application

programs as previously described. For the sequential version, the equations are as follows:

$$\begin{aligned} \mathcal{T}_{\text{startup}} &= \mathcal{T}_{\text{read\_fft}} + \mathcal{T}_{\text{init}} \\ \mathcal{T}_{\text{computation}} &= \mathcal{T}_{\text{row\_fft}} + \mathcal{T}_{\text{col\_fft}} \\ \mathcal{T}_{\text{finish}} &= \mathcal{T}_{\text{write\_fft}} \end{aligned}$$

For the parallel version, the equations reflect the division of computation among processes and also the inclusion of communication and housekeeping routines, as follows:

$$\mathcal{T}_{\text{startup}} = \mathcal{T}_{\text{set\_mesh}} + \mathcal{T}_{\text{read\_fft}} + \mathcal{T}_{\text{read\_mesh}} + \mathcal{T}_{\text{init}}$$

$$\begin{aligned} \mathcal{T}_{\text{computation}} = {} & \mathcal{T}_{\text{local\_pos}} + \mathcal{T}_{\text{data\_widths}} + \left(\frac{\mathcal{T}_{\text{row\_fft}}}{\text{NPROCS}} \right) + \mathcal{T}_{\text{row\_to\_col}} + \\ & \mathcal{T}_{\text{local\_pos}} + \mathcal{T}_{\text{data\_widths}} + \left(\frac{\mathcal{T}_{\text{col\_fft}}}{\text{NPROCS}} \right) + \mathcal{T}_{\text{col\_to\_row}} \end{aligned}$$

$$\mathcal{T}_{\text{finish}} = \mathcal{T}_{\text{write\_fft}} + \mathcal{T}_{\text{write\_mesh}}$$

Experimental Results. For this experiment we used the following values of the program parameters:

$$\begin{aligned} \text{NREPEATS} &= 10 \\ \text{NPROCS} &= n \end{aligned}$$

where n is the number of processors (1, 2, 4, 8, 16, or 32). Table 9 and Figures 10 and 11 compare predicted with observed times. For this experiment, predicted times generally agreed well with observed times, with predicted times mostly being, as we expected, somewhat pessimistic. (The exception is the predictions for 4 nodes, which in both cases were optimistic.)

The overall performance of this application is admittedly disappointing. In part this is because the application reads and writes the whole array; including this substantial I/O degrades performance but makes the program slightly more realistic and demonstrates that the performance model is compatible with the archetype's I/O handling. However, it appears that this application simply does not scale very well; for more than a few processors, performance gains obtained by distributing the computation are largely negated by the additional time required for interprocess communication. Possibly this could be overcome by optimizing the archetype library (the current implementation is an unoptimized proof-of-concept version, which could be replaced by an optimized version, thus improving performance of all mesh-spectral applications).

Despite the application's unimpressive performance, however, this experiment validates our model, since predicted execution times were close to actual

execution times. A situation such as this one suggests an additional use for a good performance model — deciding on the basis of the model that a particular parallelization scheme is not likely to be effective without actually coding it up and trying it.

	Time (secs) on n nodes					
	$n = 1$	$n = 2$	$n = 4$	$n = 8$	$n = 16$	$n = 32$
Expected Elapsed Time	160	101	69	69	68	78
Actual Elapsed Time	157	100	80	51	49	60
Expected Process Time	156	96	63	60	51	45
Actual Process Time	153	95	73	41	32	29

Table 9: Execution times for the mesh-spectral 2D FFT application, running on the specified number of nodes on the IBM SP2 using Fortran with MPI, without the crossbar switch. Problem size is 800 by 800 points and 10 repetitions. Times are in seconds. See Figures 10 and 11 for corresponding graphs.

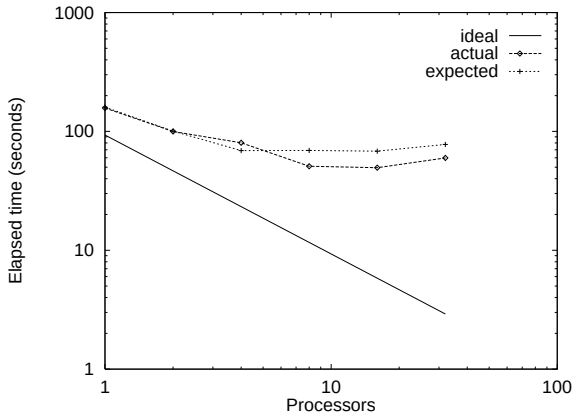


Figure 10: Elapsed times for the mesh-spectral 2D FFT application. running on the specified number of nodes on the IBM SP2 using Fortran with MPI, without the crossbar switch. Problem size is 800 by 800 points and 10 repetitions. See Table 9 for corresponding table.

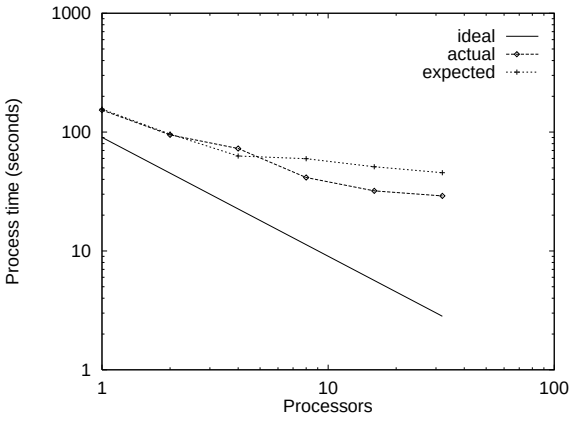


Figure 11: Process times for the mesh-spectral 2D FFT application. running on the specified number of nodes on the IBM SP2 using Fortran with MPI, without the crossbar switch. Problem size is 800 by 800 points and 10 repetitions. See Table 9 for corresponding table.

4.2 Poisson Solver

This application is another implementation, using the mesh-spectral archetype this time, of the Poisson solver described in Section 3.2, with one additional feature: Values for stepsize (`H`) and convergence tolerance (`TOL`) are to be read at runtime from standard input or an input file. Both sequential and parallel versions are very similar to those described in Section 3.2, except that the parallel version uses the mesh-spectral archetype library rather than the mesh archetype library, and both versions read in stepsize and tolerance. (The parallel version performs this read in the archetype's designated I/O process and then uses `broadcast` to copy their values to the other processes.) We compare the performance of the mesh-spectral implementation to that of the mesh implementation in Section 5.1.

Benchmarking. The computational benchmark measures values for the following times: $\mathcal{T}_{\text{overhead}}$ (start and terminate process), $\mathcal{T}_{\text{read\_const}}$ (read constants), $\mathcal{T}_{\text{init}}$ (initialize grid values), $\mathcal{T}_{\text{comp}}$ (calculate new values for all grid points), $\mathcal{T}_{\text{check\_converge}}$ (check for convergence), $\mathcal{T}_{\text{copy\_values}}$ (copy new values back to `uk`), and $\mathcal{T}_{\text{output}}$ (output results). Results are given in Table 10. Observe that results for this benchmark are independent of the choice of archetype implementation.

The communication benchmark measures values for the following times:

Measurement	Time (msecs)
$\mathcal{T}_{\text{overhead}}$	100
$\mathcal{T}_{\text{read\_const}}$	15
$\mathcal{T}_{\text{init}}$	222
$\mathcal{T}_{\text{comp}}$	427
$\mathcal{T}_{\text{check\_converge}}$	134
$\mathcal{T}_{\text{copy\_values}}$	62
$\mathcal{T}_{\text{output}}$	15

Table 10: Results of computational benchmark for the mesh-spectral Poisson solver application, running on a single node of the IBM SP2 using Fortran. Grid size is 800 by 800 points. Times are in milliseconds.

$\mathcal{T}_{\text{overhead}}$ (start and terminate processes), $\mathcal{T}_{\text{set\_mesh}}$ (set up grid), $\mathcal{T}_{\text{blk\_to\_one}}$ (redistribute data, block distribution to all-in-one), $\mathcal{T}_{\text{one\_to\_blk}}$ (redistribute data, all-in-one to block distribution), $\mathcal{T}_{\text{bdry\_exchg}}$ (update ghost boundaries by exchanging data with neighboring processes), $\mathcal{T}_{\text{bcast}}$ (broadcast constants), $\mathcal{T}_{\text{global\_max\_dp}}$ (compute global maximum from local maxima), and housekeeping routines (mostly for manipulating global and local indices) $\mathcal{T}_{\text{data\_bounds}}$, $\mathcal{T}_{\text{intersect}}$, $\mathcal{T}_{\text{local\_pos}}$, $\mathcal{T}_{\text{local\_to\_global}}$, $\mathcal{T}_{\text{pack}}$, and $\mathcal{T}_{\text{unpack}}$. We ran this benchmark on 1, 4, 9, 16, 25, and 36 processors. Results are given in Table 11.

The computational and communication benchmark programs appear in Appendix B.2.

Performance Model. We use our performance model and the program, given in Appendix B.2, to compute estimated running time in terms of the preceding list of benchmark values and a few additional program parameters — NSTEPS (number of loop iterations), NCHECK (frequency of convergence checking), and NXPROCS and NYPROCS (dimensions of process grid, implying a total of NXPROCS $\times$ NYPROCS processes) — as follows. First, a high-level decomposition gives us values for $\mathcal{T}_{\text{elapsed}}$ (total estimated elapsed time) and $\mathcal{T}_{\text{process}}$ (total estimated process time, excluding process-setup overhead):

$$\begin{aligned}\mathcal{T}_{\text{elapsed}} &= \mathcal{T}_{\text{process}} + \mathcal{T}_{\text{overhead}} \\ \mathcal{T}_{\text{process}} &= \mathcal{T}_{\text{startup}} + \mathcal{T}_{\text{computation}} + \mathcal{T}_{\text{check}} + \mathcal{T}_{\text{copy}} + \mathcal{T}_{\text{finish}}\end{aligned}$$

We can then write down equations for each term on the right-hand side of the above equations based on applying our performance model to the application programs as previously described. For the sequential version, the equations are

Measurement	Time (msecs) on n nodes					
	$n=1$	$n=4$	$n=9$	$n=16$	$n=25$	$n=36$
$\mathcal{T}_{\text{overhead}}$	3850	9630	15950	27380	48330	86150
$\mathcal{T}_{\text{set\_mesh}}$	0	0	0	0	0	0
$\mathcal{T}_{\text{blk\_to\_one}}$	2928	1957	1365	1219	954	1241
$\mathcal{T}_{\text{one\_to\_blk}}$	2951	2474	2051	2026	2222	1792
$\mathcal{T}_{\text{bdry\_exchg}}$	0	11	13	14	16	20
$\mathcal{T}_{\text{bcast}}$	0	4	14	35	75	145
$\mathcal{T}_{\text{data\_bounds}}$	0	0	0	0	0	0
$\mathcal{T}_{\text{global\_max\_dp}}$	0	12	25	53	96	171
$\mathcal{T}_{\text{intersect}}$	0	0	0	0	0	0
$\mathcal{T}_{\text{local\_pos}}$	0	0	0	0	0	0
$\mathcal{T}_{\text{local\_to\_global}}$	0	0	0	0	0	0
$\mathcal{T}_{\text{pack}}$	0	0	0	0	0	0
$\mathcal{T}_{\text{unpack}}$	0	0	0	0	0	0

Table 11: Results of communication benchmark for the mesh-spectral Poisson solver application, running on the specified number of nodes on the IBM SP2 using Fortran M, without the crossbar switch. Grid size is 800 by 800 points. Times are in milliseconds.

as follows:

$$\begin{aligned}
\mathcal{T}_{\text{startup}} &= \mathcal{T}_{\text{read_const}} + \mathcal{T}_{\text{init}} \\
\mathcal{T}_{\text{computation}} &= \text{NSTEPS} \times \mathcal{T}_{\text{comp}} \\
\mathcal{T}_{\text{check}} &= \frac{\text{NSTEPS}}{\text{NCHECK}} \times \mathcal{T}_{\text{check_converge}} \\
\mathcal{T}_{\text{copy}} &= \text{NSTEPS} \times \mathcal{T}_{\text{copy_values}} \\
\mathcal{T}_{\text{finish}} &= \mathcal{T}_{\text{output}}
\end{aligned}$$

For the parallel version, the equations reflect the division of computation among processes and also the inclusion of communication and housekeeping routines, as follows:

$$\begin{aligned}
\mathcal{T}_{\text{startup}} = {} & \mathcal{T}_{\text{local_pos}} + \mathcal{T}_{\text{read_const}} + \mathcal{T}_{\text{bcast}} + \mathcal{T}_{\text{set_mesh}} + \mathcal{T}_{\text{local_pos}} + \\
& \mathcal{T}_{\text{init}} + \mathcal{T}_{\text{one_to_blk}} + \mathcal{T}_{\text{local_pos}}
\end{aligned}$$

$$
\begin{aligned}
\mathcal{T}_{\text{computation}} &= (\ \mathcal{T}_{\text{pack}} \times\ 3\ ) + (\ \mathcal{T}_{\text{unpack}} \times\ 3\ ) + \\
&\quad \mathcal{T}_{\text{data\_bounds}} + \mathcal{T}_{\text{intersect}} + \mathcal{T}_{\text{local\_to\_global}} + \\
&\quad \text{NSTEPS} \times\ (\ \frac{\mathcal{T}_{\text{comp}}}{\text{XPROCS} \times\ \text{YPROCS}} + \mathcal{T}_{\text{bdry\_exchg}}\ ) \\
\mathcal{T}_{\text{check}} &= \frac{\text{NSTEPS}}{\text{NCHECK}} \times\ (\ \frac{\mathcal{T}_{\text{check\_converge}}}{\text{XPROCS} \times\ \text{YPROCS}} + \mathcal{T}_{\text{global\_max\_dp}}\ ) \\
\mathcal{T}_{\text{copy}} &= \text{NSTEPS} \times\ (\ \frac{\mathcal{T}_{\text{copy\_values}}}{\text{NXPROCS} \times\ \text{NYPROCS}}\ ) \\
\mathcal{T}_{\text{finish}} &= \mathcal{T}_{\text{output}}
\end{aligned}
$$

Experimental Results. For this experiment we used the following values of the program parameters:

$$
\begin{aligned}
\text{NSTEPS} &= 1000 \\
\text{NCHECK} &= 10 \\
\text{NXPROCS} &= \text{NYPROCS} = \sqrt{n}
\end{aligned}
$$

where n is the number of processors (1, 4, 9, 16, 25, or 36). Table 12 and Figures 12 and 13 compare predicted with observed times. For this experiment, predicted times agreed well with observed times. Surprisingly, several predictions were slightly optimistic, but overall the agreement was quite good for this application. Our model also correctly predicts the scalability of the application, validating its utility in helping programmers choose granularity.

	Time (secs) on n nodes					
	$n=1$	$n=4$	$n=9$	$n=16$	$n=25$	$n=36$
Expected Elapsed Time	512	152	91	81	98	142
Actual Elapsed Time	521	151	91	78	95	130
Expected Process Time	508	142	75	54	49	55
Actual Process Time	516	143	75	54	55	63

Table 12: Execution times for the mesh-spectral Poisson solver application, running on the specified number of nodes on the IBM SP2 using Fortran M, without the crossbar switch. Problem size is 800 by 800 points and 1000 steps. Times are in seconds. See Figures 12 and 13 for corresponding graphs.

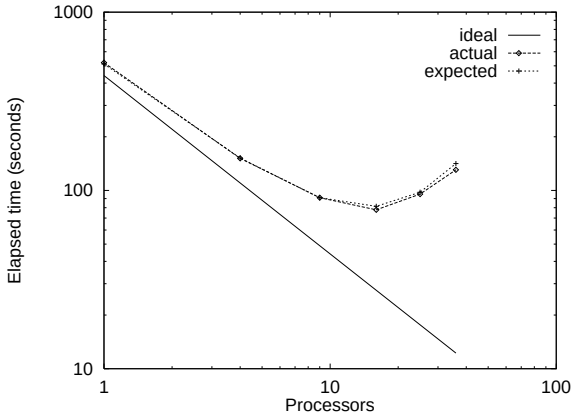


Figure 12: Elapsed times for the mesh-spectral Poisson solver application, running on the specified number of nodes on the IBM SP2 using Fortran M, without the crossbar switch. Problem size is 800 by 800 points and 1000 steps. Times are in seconds. See Table 12 for corresponding table.

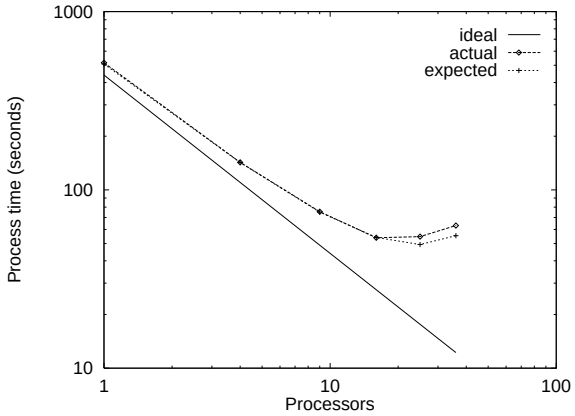


Figure 13: Process times for the mesh-spectral Poisson solver application, running on the specified number of nodes on the IBM SP2 using Fortran M, without the crossbar switch. Problem size is 800 by 800 points and 1000 steps. Times are in seconds. See Table 12 for corresponding table.

5 Evaluating the Performance Model

In this section, we evaluate the utility of our performance model. Through selected experiments, we show that our performance analysis works well when applied to different archetypes (Section 5.1), to different architectures (Section 5.2), and to different communication libraries (Section 5.3).

In addition, we show that our performance model can be used to choose between different data distributions (Section 5.4), and that our performance model can be used to simulate actual program executions to predict expected running times (Section 5.5).

5.1 Performance Analysis Across Archetypes

In this section, we demonstrate that our performance analysis works well when used to compare running times for the same application developed using different archetypes. For this experiment, we employ two versions of the Poisson solver application (described in Sections 3.2 and 4.2), both implemented in Fortran M and running on an IBM SP2, but one using the mesh archetype and one the mesh-spectral archetype.

Benchmarking. The computational and communication benchmark programs for this application appear in Appendix A.2 and Appendix B.2 for the mesh and mesh-spectral versions, respectively. Results of the computational and communication benchmarks for the mesh version of the application, executed using the target archetype implementation and architecture, appear in Tables 4 and 5, respectively. Results of the computational and communication benchmarks for the mesh-spectral version of the application, executed using the target archetype implementation and architecture, appear in Tables 10 and 11, respectively.

Performance Models. Our performance model for the mesh Poisson solver application is given in Section 3.2, based on the program in Appendix A.2. Our performance model for the mesh-spectral Poisson solver application is given in Section 4.2, based on the program in Appendix B.2.

Experimental Results. For this experiment we used the following values of the program parameters:

$$\text{NSTEPS} = 1000$$
$$\text{NCHECK} = 10$$

For the mesh version, we used

$$\text{XPROCS} = \text{YPROCS} = \sqrt{n}$$

where n is the number of grid (non-"host") processors (1, 4, 9, 16, 25, or 36). For the mesh-spectral version, we used

$$\text{NXPROCS} = \text{NYPROCS} = \sqrt{n}$$

where n is the number of processors (1, 4, 9, 16, 25, or 36). Table 13 and Figure 14 compare elapsed times (predicted and observed) for the two programs. Table 14 and Figure 15 compare process times (predicted and observed) for the two programs. These results have been discussed previously (in Sections 3.2 and 4.2); note again that for both versions of the application the model's predictions about execution times and scaling are generally good. The model also correctly predicts that overall the mesh-spectral version of the application performs better.

	Time (secs) on n nodes, not including host node					
	$n = 1$	$n = 4$	$n = 9$	$n = 16$	$n = 25$	$n = 36$
Mesh-Spectral Expected Elapsed Time	512	152	91	81	98	142
Mesh-Spectral Actual Elapsed Time	521	151	91	78	95	130
Mesh Expected Elapsed Time	496	149	94	78	91	91
Mesh Actual Elapsed Time	522	148	87	69	58	62

Table 13: Elapsed times for the mesh and mesh-spectral Poisson solver applications, running on the specified number of nodes (plus a "host" node for the mesh version) on the IBM SP2 using Fortran M, without the crossbar switch. Problem size is 800 by 800 grid points and 1000 steps. Times are in seconds. See Figure 14 for corresponding graph.

5.2 Performance Analysis Across Architectures

In this section, we demonstrate that our performance analysis works well when used to compare running times for the same application developed using the same archetype, executing on different target machines (with portability as an automatic consequence of using a portable archetype implementation). For this experiment, we employ the mesh-spectral Poisson solver application (described in Section 4.2), implemented in Fortran with MPI, running on an IBM SP2 and

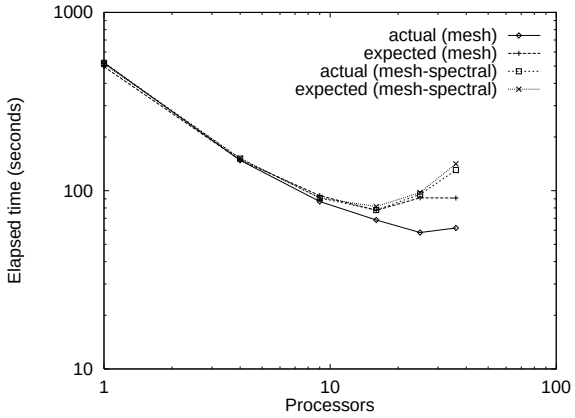


Figure 14: Elapsed times for the mesh and mesh-spectral Poisson solver applications, running on the specified number of nodes (plus a "host" node for the mesh version) on the IBM SP2 using Fortran M, without the crossbar switch. Problem size is 800 by 800 grid points and 1000 steps. Times are in seconds. See Table 13 for corresponding table.

	Time (secs) on n nodes, not including host node					
	$n = 1$	$n = 4$	$n = 9$	$n = 16$	$n = 25$	$n = 36$
Mesh-Spectral Expected Process Time	508	142	75	54	49	55
Mesh-Spectral Actual Process Time	516	143	75	54	55	63
Mesh Expected Process Time	490	141	80	59	59	54
Mesh Actual Process Time	517	140	73	47	34	32

Table 14: Process times for the mesh and mesh-spectral Poisson solver applications, running on the specified number of nodes (plus a "host" node for the mesh version) on the IBM SP2 using Fortran M, without the crossbar switch. Problem size is 800 by 800 grid points and 1000 steps. Times are in seconds. See Figure 15 for corresponding graph.

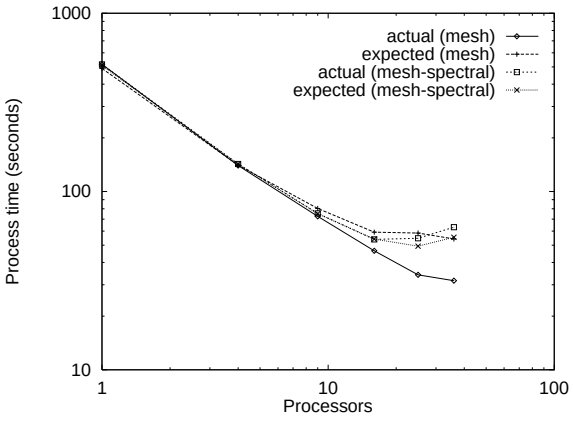


Figure 15: Process times for the mesh and mesh-spectral Poisson solver applications, running on the specified number of nodes (plus a "host" node for the mesh version) on the IBM SP2 using Fortran M, without the crossbar switch. Problem size is 800 by 800 grid points and 1000 steps. Times are in seconds. See Table 14 for corresponding table.

on a network of 166 MHz Pentium personal computers connected by 100 Mbps Ethernet.

Benchmarking. The computational and communication benchmark programs for this application appear in Appendix B.2. Applying our performance analysis for a particular implementation and architecture requires results from executing both benchmarks on an appropriate system. For the SP2, we can reuse the computational benchmark results shown in Table 10, since the target architecture is the same. We must, however, rerun the communication benchmark using the MPI-based archetype implementation. As before, we ran this benchmark on 1, 4, 9, 16, 25, and 36 processors; results are given in Table 15. For the network of Pentiums, we must rerun both computational and communication benchmarks. Results of running the computational benchmark on one Pentium processor appear in Table 16. Due to a bug in the MPI implementation installed on our target network, we were unable to make use of more than 9 processors, so we ran the communication benchmark for 1, 2, 4, 6, 8, and 9 processors. Results are given in Table 17.

Performance Model. Our performance model for this application is given in Section 4.2, based on the program in Appendix B.2, and is applicable to both

Measurement	Time (msecs) on n nodes					
	$n = 1$	$n = 4$	$n = 9$	$n = 16$	$n = 25$	$n = 36$
$\mathcal{T}_{\text{overhead}}$	3930	6030	10280	17130	26400	39130
$\mathcal{T}_{\text{set\_mesh}}$	0	0	0	0	0	0
$\mathcal{T}_{\text{blk\_to\_one}}$	3218	2235	1374	1276	1172	1026
$\mathcal{T}_{\text{one\_to\_blk}}$	3243	1977	1829	1666	1750	1698
$\mathcal{T}_{\text{bdry\_exchg}}$	0	4	4	4	4	5
$\mathcal{T}_{\text{bcast}}$	0	0	1	1	2	3
$\mathcal{T}_{\text{data\_bounds}}$	0	0	0	0	0	0
$\mathcal{T}_{\text{global\_max\_dp}}$	0	1	1	2	3	4
$\mathcal{T}_{\text{intersect}}$	0	0	0	0	0	0
$\mathcal{T}_{\text{local\_pos}}$	0	0	0	0	0	0
$\mathcal{T}_{\text{local\_to\_global}}$	0	0	0	0	0	0
$\mathcal{T}_{\text{pack}}$	0	0	0	0	0	0
$\mathcal{T}_{\text{unpack}}$	0	0	0	0	0	0

Table 15: Results of communication benchmark for the mesh-spectral Poisson solver application, running on the specified number of nodes on the IBM SP2 using Fortran with MPI, without the crossbar switch. Grid size is 800 by 800 points. Times are in milliseconds.

Measurement	Time (msecs)
$\mathcal{T}_{\text{overhead}}$	150
$\mathcal{T}_{\text{read\_const}}$	5
$\mathcal{T}_{\text{init}}$	271
$\mathcal{T}_{\text{comp}}$	941
$\mathcal{T}_{\text{check\_converge}}$	265
$\mathcal{T}_{\text{copy\_values}}$	244
$\mathcal{T}_{\text{output}}$	40

Table 16: Results of computational benchmark for the mesh-spectral Poisson solver application, running on a single 166 MHz Pentium using Fortran. Grid size is 800 by 800 points. Times are in milliseconds.

Measurement	Time (msecs) on n nodes					
	$n=1$	$n=2$	$n=4$	$n=6$	$n=8$	$n=9$
$\mathcal{T}_{\text{overhead}}$	3000	7530	9930	14830	18000	18150
$\mathcal{T}_{\text{set\_mesh}}$	0	0	0	0	0	0
$\mathcal{T}_{\text{blk\_to\_one}}$	3957	3805	3307	2310	2243	2133
$\mathcal{T}_{\text{one\_to\_blk}}$	4115	3738	4563	4961	5230	5134
$\mathcal{T}_{\text{bdry\_exchg}}$	0	11	15	19	209	296
$\mathcal{T}_{\text{bcast}}$	0	0	2	3	5	5
$\mathcal{T}_{\text{data\_bounds}}$	0	0	0	0	0	0
$\mathcal{T}_{\text{global\_max\_dp}}$	0	2	4	6	9	12
$\mathcal{T}_{\text{intersect}}$	0	0	0	0	0	0
$\mathcal{T}_{\text{local\_pos}}$	0	0	0	0	0	0
$\mathcal{T}_{\text{local\_to\_global}}$	0	0	0	0	0	0
$\mathcal{T}_{\text{pack}}$	0	0	0	0	0	0
$\mathcal{T}_{\text{unpack}}$	0	0	0	0	0	0

Table 17: Results of communication benchmark for the mesh-spectral Poisson solver application, running on the specified number of nodes on a network of 166 MHz Pentiums using Fortran with MPI, communicating over 100 Mbps Ethernet. Grid size is 800 by 800 points. Times are in milliseconds.

architectures.

Experimental Results. For this experiment we used the following values of the program parameters:

$$\text{NSTEPS} = 1000$$
$$\text{NCHECK} = 10$$

On the SP2, we used

$$\text{NXPROCS} = \text{NYPROCS} = \sqrt{n}$$

where n is the number of processors (1, 4, 9, 16, 25, or 36). On the network of Pentiums, we used the following values of (NXPROCS, NYPROCS): (1,1), (1,2), (2,2), (2,3), (2,4), and (3,3), corresponding to 1, 2, 4, 8, and 9 processors. Table 18 and Figure 16 compare elapsed times (predicted and observed) for the two architectures (network of Pentiums and IBM SP2). Table 19 and Figure 17 compare process times (predicted and observed) for the two architectures. For this experiment, predicted times agreed well with observed times for both architectures. Surprisingly, many predicted times for the network of Pentiums

were optimistic, though not extremely so. For both architectures, our model predicts the scalability of the application pretty well, and it correctly predicts the expected performance difference between the two architectures.

	Time (secs) on n nodes				
	$n = 1$	$n = 2$	$n = 4$	$n = 6$	$n = 8$
SP2 Expected Elapsed Time	513	–	140	–	–
SP2 Actual Elapsed Time	520	–	142	–	–
Pentium Expected Elapsed Time	1222	632	337	243	387
Pentium Actual Elapsed Time	1308	712	362	288	342

	Time (secs) on n nodes			
	$n = 9$	$n = 16$	$n = 25$	$n = 36$
SP2 Expected Elapsed Time	74	56	54	61
SP2 Actual Elapsed Time	75	52	52	56
Pentium Expected Elapsed Time	457	–	–	–
Pentium Actual Elapsed Time	379	–	–	–

Table 18: Elapsed times for the mesh-spectral Poisson solver application implemented in Fortran with MPI, running on the specified number of nodes on the IBM SP2 (without the crossbar switch) and a network of 166 MHz Pentiums (communicating over 100 Mbps Ethernet). Problem size is 800 by 800 grid points and 1000 steps. Times are in seconds. See Figure 16 for corresponding graph.

5.3 Performance Analysis Across Libraries

In this section, we demonstrate that our performance analysis works well when used to compare running times for the same application developed using the same archetype for the same target machine, using different communication libraries (i.e., different archetype implementations). For this experiment, we employ the mesh-spectral Poisson solver application (described in Section 4.2), comparing a Fortran M implementation running on an IBM SP2 with an MPI implementation also running on an IBM SP2.

Benchmarking. The computational and communication benchmark programs appear in Appendix B.2. As in Section 5.2, applying our performance

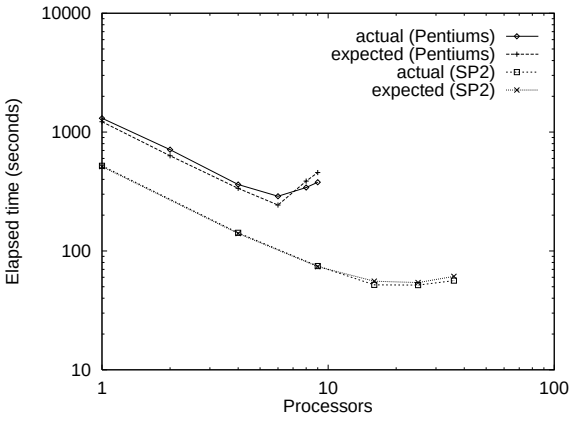


Figure 16: Elapsed times for the mesh-spectral Poisson solver application implemented in Fortran with MPI, running on the specified number of nodes on the IBM SP2 (without the crossbar switch) and a network of 166 MHz Pentiums (communicating over 100 Mbps Ethernet). Problem size is 800 by 800 grid points and 1000 steps. Times are in seconds. See Table 18 for corresponding table.

analysis for a particular implementation requires results from executing both benchmarks on appropriate system. Since here we are comparing different archetype implementations on the same target architecture, we can use the same computational benchmark results for both, namely the ones presented in Table 10. For the communication benchmark, we need results from executing versions based on both the Fortran M and MPI archetype implementations, presented respectively in Tables 11 and 15.

Performance Model. Our performance model for this application is given in Section 4.2, based on the program in Appendix B.2, and is applicable to both implementations.

Experimental Results. For this experiment we used the following values of the program parameters:

$$\text{NSTEPS} = 1000$$
$$\text{NCHECK} = 10$$
$$\text{NXPROCS} = \text{NYPROCS} = \sqrt{n}$$

	Time (secs) on n nodes				
	$n = 1$	$n = 2$	$n = 4$	$n = 6$	$n = 8$
SP2 Expected Process Time	509	–	134	–	–
SP2 Actual Process Time	516	–	135	–	–
Pentium Expected Process Time	1219	625	327	229	370
Pentium Actual Process Time	1305	632	354	276	328

	Time (secs) on n nodes			
	$n = 9$	$n = 16$	$n = 25$	$n = 36$
SP2 Expected Process Time	64	38	28	22
SP2 Actual Process Time	64	39	27	24
Pentium Expected Process Time	439	–	–	–
Pentium Actual Process Time	363	–	–	–

Table 19: Process times for the mesh-spectral Poisson solver application implemented in Fortran with MPI, running on the specified number of nodes on the IBM SP2 (without the crossbar switch) and a network of 166 MHz Pentiums (communicating over 100 Mbps Ethernet). Problem size is 800 by 800 grid points and 1000 steps. Times are in seconds. See Figure 17 for corresponding graph.

where n is the number of processors (1, 4, 9, 16, 25, or 36). Table 20 and Figure 18 compare elapsed times (predicted and observed) for the two implementations. Table 21 and Figure 19 compare process times (predicted and observed) for the two implementations. These results have been discussed previously (in Section 4.2 for the Fortran M implementation and Section 5.2 for the MPI implementation); note again that for both implementations the model's predictions about execution times and scaling are generally good. The model also correctly predicts that the MPI implementation performs better than the Fortran M implementation, suggesting that it could help programmers decide between archetype implementations without trying both.

5.4 Performance Analysis and Data Distributions

In this section, we show that our performance model can be used to predict how performance is affected by data distribution and thus help the programmer to choose an efficient data distribution. For our experiment, we employ the mesh-spectral Poisson solver application (described in Section 4.2), implemented in

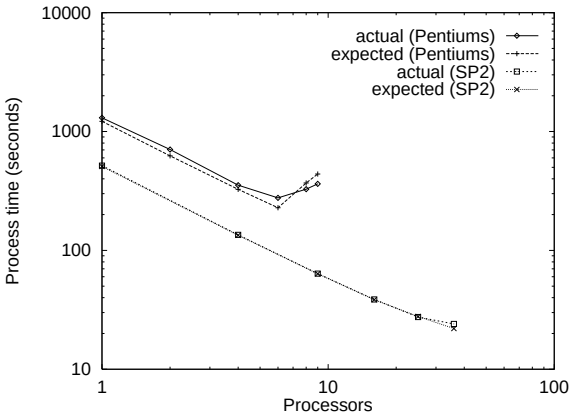


Figure 17: Process times for the mesh-spectral Poisson solver application implemented in Fortran with MPI, running on the specified number of nodes on the IBM SP2 (without the crossbar switch) and a network of 166 MHz Pentiums (communicating over 100 Mbps Ethernet). Problem size is 800 by 800 grid points and 1000 steps. Times are in seconds. See Table 19 for corresponding table.

	Time (secs) on n nodes					
	$n=1$	$n=4$	$n=9$	$n=16$	$n=25$	$n=36$
Fortran M Expected Elapsed Time	512	152	91	81	98	142
Fortran M Actual Elapsed Time	521	151	91	78	95	130
MPI Expected Elapsed Time	513	140	74	57	54	61
MPI Actual Elapsed Time	520	142	75	52	52	56

Table 20: Elapsed times for the mesh-spectral Poisson solver application, Fortran M and MPI implementations, running on the specified number of nodes on the IBM SP2, without the crossbar switch. Problem size is 800 by 800 grid points and 1000 steps. Times are in seconds. See Figure 18 for corresponding graph.

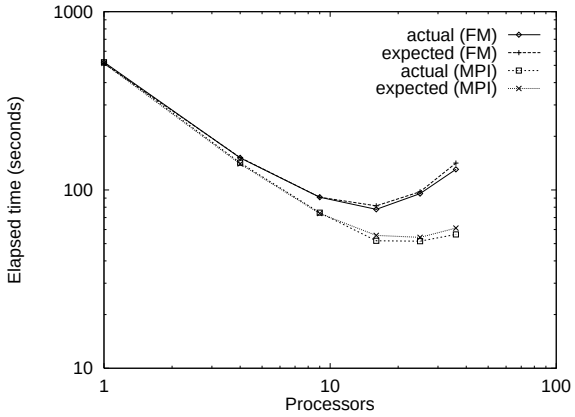


Figure 18: Elapsed times for the mesh-spectral Poisson solver application, Fortran M and MPI implementations, running on the specified number of nodes on the IBM SP2, without the crossbar switch. Problem size is 800 by 800 grid points and 1000 steps. Times are in seconds. See Table 20 for corresponding table.

	Time (secs) on n nodes					
	$n = 1$	$n = 4$	$n = 9$	$n = 16$	$n = 25$	$n = 36$
Fortran M Expected Process Time	508	142	75	54	49	55
Fortran M Actual Process Time	516	143	75	54	55	63
MPI Expected Process Time	509	134	64	39	28	22
MPI Actual Process Time	516	135	64	39	27	24

Table 21: Process times for the mesh-spectral Poisson solver application, Fortran M and MPI implementations, running on the specified number of nodes on the IBM SP2, without the crossbar switch. Problem size is 800 by 800 grid points and 1000 steps. Times are in seconds. See Figure 19 for corresponding graph.

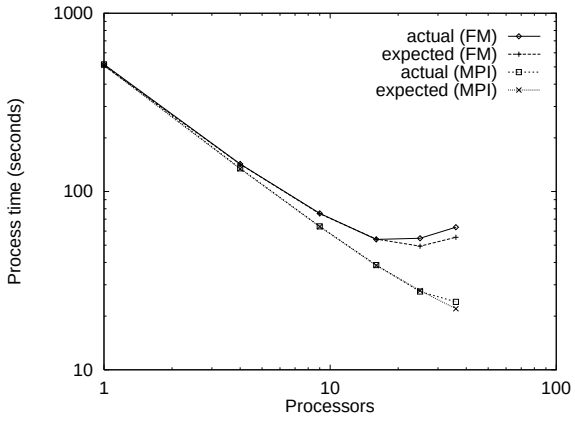


Figure 19: Process times for the mesh-spectral Poisson solver application, Fortran M and MPI implementations, running on the specified number of nodes on the IBM SP2, without the crossbar switch. Problem size is 800 by 800 grid points and 1000 steps. Times are in seconds. See Table 21 for corresponding table.

Fortran with MPI and running on an IBM SP2.

Benchmarking. The computational and communication benchmark programs appear in Appendix B.2. Different choices of NXPROCS and NYPROCS (the dimensions of the process grid) imply different data distributions; for example, if NXPROCS $= 1$, data is distributed by columns. To model the effect of varying the data distribution in this way, we can reuse the computational benchmark results in Table 10, but we must rerun the communication benchmark for each choice of (NXPROCS, NYPROCS). We ran the communication benchmark for the following configurations of (NXPROCS, NYPROCS): (1,16), (2,8), (4,4), (8,2), and (16,1). Results are given in Table 22.

Performance Model. Our performance model for this application is given in Section 4.2, based on the program in Appendix B.2, and is applicable to all data distributions (parameterized by NXPROCS and NYPROCS).

Experimental Results. For this experiment we used the following values of the program parameters:

$$\text{NSTEPS} = 1000$$
$$\text{NCHECK} = 10$$

(NXPROCS, NYPROCS)	(1, 16)	(2, 8)	(4, 4)	(8, 2)	(16, 1)
$\mathcal{T}_{\text{set\_mesh}}$	0	0	0	0	0
$\mathcal{T}_{\text{blk\_to\_one}}$	868	1454	1276	1315	1428
$\mathcal{T}_{\text{one\_to\_blk}}$	1326	1714	1666	1669	1629
$\mathcal{T}_{\text{bdry\_exchg}}$	4	4	4	4	6
$\mathcal{T}_{\text{bcast}}$	1	1	1	1	1
$\mathcal{T}_{\text{data\_bounds}}$	0	0	0	0	0
$\mathcal{T}_{\text{global\_max\_dp}}$	2	2	2	2	2
$\mathcal{T}_{\text{intersect}}$	0	0	0	0	0
$\mathcal{T}_{\text{local\_pos}}$	0	0	0	0	0
$\mathcal{T}_{\text{local\_to\_global}}$	0	0	0	0	0
$\mathcal{T}_{\text{pack}}$	0	0	0	0	0
$\mathcal{T}_{\text{unpack}}$	0	0	0	0	0

Table 22: Results of communication benchmark for the mesh-spectral Poisson solver application, running with the specified data distributions on the IBM SP2 using Fortran and MPI, without the crossbar switch. Grid size is 800 by 800 points. Times are in milliseconds.

and NXPROCS and NYPROCS as described earlier. Table 23 compares predicted with observed times. Again, predicted times agree well overall with actual times. Somewhat surprisingly, the model also predicts that for this application the choice of data distribution has little effect on execution time; nevertheless, this is borne out by observed execution times, suggesting that the model's predictions can indeed help guide the programmer's choice of data distribution.

5.5 Performance Analysis and Simulation

In this section, we show that our performance model can be used to simulate the actual program executions. For our experiment, we employ the mesh-spectral Poisson solver application (described in Section 4.2), implemented in Fortran M, running on the IBM SP2.

Benchmarking. The computational and communication benchmark programs appear in Appendix B.2. For this experiment, we need not only the average results presented Tables 10 and 11 but also, for each measurement, the maximum and minimum of the values used to compute the average. These values are shown in Tables 24 and 25. For each measurement, the simulation generates a uniform distribution using these minimum and maximum values.

(NXPROCS, NYPROCS)	(1, 16)	(2, 8)	(4, 4)	(8, 2)	(16, 1)
Expected Process Time	38	39	39	39	41
Actual Process Time	38	38	39	39	41
Expected Elapsed Time	55	56	55	56	58
Actual Elapsed Time	52	52	52	57	57

Table 23: Execution times for the mesh-spectral Poisson solver application, running with the specified data distributions on the IBM SP2 using Fortran and MPI, without the crossbar switch. Problem size is 800 by 800 points and 1000 steps. Times are in seconds.

Measurement	Min, max times (msecs)
$\mathcal{T}_{\text{overhead}}$	100, 100
$\mathcal{T}_{\text{read\_const}}$	11, 24
$\mathcal{T}_{\text{init}}$	222, 223
$\mathcal{T}_{\text{comp}}$	426, 431
$\mathcal{T}_{\text{check\_converge}}$	133, 138
$\mathcal{T}_{\text{copy\_values}}$	60, 66
$\mathcal{T}_{\text{output}}$	15, 16

Table 24: Results of computational benchmark for the mesh-spectral Poisson solver application, running on a single node of the IBM SP2 using Fortran. Grid size is 800 by 800 points. Times are in milliseconds.

Performance Model. Our simulation is based on the performance model given in Section 4.2, and on the program in Appendix B.2.

Experimental Results. For this experiment we used the following values of the program parameters:

$$\text{NSTEPS} = 1000$$
$$\text{NCHECK} = 10$$
$$\text{NXPROCS} = \text{NYPROCS} = \sqrt{n}$$

Measurement	Min, max times (msecs) on n nodes		
	$n = 1$	$n = 4$	$n = 9$
$\mathcal{T}_{\text{overhead}}$	3300, 5000	7800, 11600	14500, 18300
$\mathcal{T}_{\text{set\_mesh}}$	0, 0	0, 0	0, 0
$\mathcal{T}_{\text{blk\_to\_one}}$	2856, 3006	1916, 2011	1335, 1392
$\mathcal{T}_{\text{one\_to\_blk}}$	2886, 3021	2363, 2603	2016, 2085
$\mathcal{T}_{\text{bdry\_exchg}}$	0, 0	11, 11	13, 13
$\mathcal{T}_{\text{bcast}}$	0, 0	4, 4	14, 14
$\mathcal{T}_{\text{data\_bounds}}$	0, 0	0, 0	0, 0
$\mathcal{T}_{\text{global\_max\_dp}}$	0, 0	12, 12	25, 25
$\mathcal{T}_{\text{intersect}}$	0, 0	0, 0	0, 0
$\mathcal{T}_{\text{local\_pos}}$	0, 0	0, 0	0, 0
$\mathcal{T}_{\text{local\_to\_global}}$	0, 0	0, 0	0, 0
$\mathcal{T}_{\text{pack}}$	0, 0	0, 0	0, 0
$\mathcal{T}_{\text{unpack}}$	0, 0	0, 0	0, 0

Measurement	Min, max times (msecs) on n nodes		
	$n = 16$	$n = 25$	$n = 36$
$\mathcal{T}_{\text{overhead}}$	22000, 40100	41100, 61300	78100, 101900
$\mathcal{T}_{\text{set\_mesh}}$	0, 0	0, 0	0, 0
$\mathcal{T}_{\text{blk\_to\_one}}$	1183, 1243	155, 1238	1082, 1689
$\mathcal{T}_{\text{one\_to\_blk}}$	1951, 2080	2053, 2677	2166, 2212
$\mathcal{T}_{\text{bdry\_exchg}}$	13, 14	16, 17	20, 21
$\mathcal{T}_{\text{bcast}}$	35, 36	74, 76	138, 149
$\mathcal{T}_{\text{data\_bounds}}$	0, 0	0, 0	0, 0
$\mathcal{T}_{\text{global\_max\_dp}}$	53, 55	95, 97	163, 176
$\mathcal{T}_{\text{intersect}}$	0, 0	0, 0	0, 0
$\mathcal{T}_{\text{local\_pos}}$	0, 0	0, 0	0, 0
$\mathcal{T}_{\text{local\_to\_global}}$	0, 0	0, 0	0, 0
$\mathcal{T}_{\text{pack}}$	0, 0	0, 0	0, 0
$\mathcal{T}_{\text{unpack}}$	0, 0	0, 0	0, 0

Table 25: Results of communication benchmark for the mesh-spectral Poisson solver application, running on the specified number of nodes on the IBM SP2 using Fortran M, without the crossbar switch. Grid size is 800 by 800 points. Times are in milliseconds.

where n is the number of processors (1, 4, 9, 16, 25, or 36). Table 26 and Figures 20 and 21 compare predicted, simulated, and actual execution times. These results indicate that our simulation helps us as developers to predict the performance times about as accurately as the performance model. Although before this experiment we surmised that analysis using closed-form equations would be most useful for calculating worst-case performance, and simulation would be most useful for estimating average-case performance, the nature of this application is such that both techniques are useful for estimating actual performance.

	Time (secs) on n nodes					
	$n = 1$	$n = 4$	$n = 9$	$n = 16$	$n = 25$	$n = 36$
Expected Elapsed Time	512	152	91	81	98	142
Simulated Elapsed Time	533	142	90	75	100	140
Actual Elapsed Time	521	151	91	78	95	130
Expected Process Time	508	142	75	54	49	55
Simulated Process Time	521	138	73	50	45	69
Actual Process Time	516	143	75	54	55	63

Table 26: Elapsed times for the mesh-spectral Poisson solver application, running on the specified number of nodes on the IBM SP2, without the crossbar switch, using Fortran M. Problem size is 800 by 800 grid points and 1000 steps. Times are in seconds. See Figures 20 and 21 for corresponding graphs.

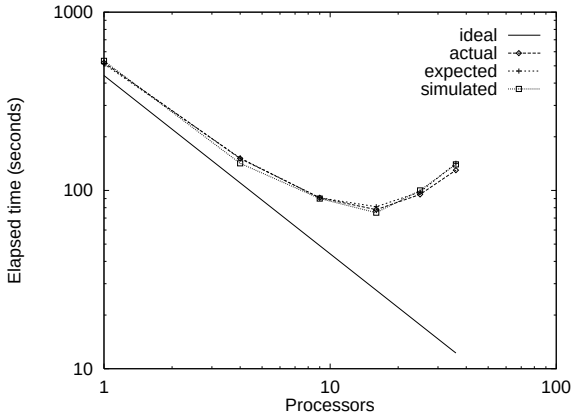


Figure 20: Elapsed times for the mesh-spectral Poisson solver application, running on the specified number of nodes on the IBM SP2, without the crossbar switch, using Fortran M. Problem size is 800 by 800 grid points and 1000 steps. Times are in seconds. See Table 26 for corresponding table.

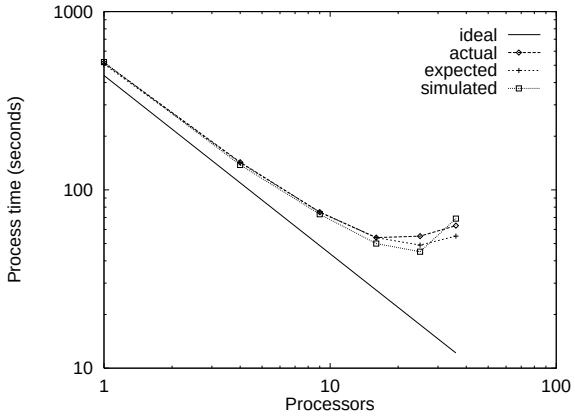


Figure 21: Process times for the mesh-spectral Poisson solver application, running on the specified number of nodes on the IBM SP2, without the crossbar switch, using Fortran M. Problem size is 800 by 800 grid points and 1000 steps. Times are in seconds. See Table 26 for corresponding table.

6 Conclusions

Our experimental results in Section 5 confirm that execution times as predicated by our model are reasonably close to observed execution times[1] More important, experiments designed to test our model's ability to predict how various "tuning choices" affect execution time gave encouraging results: The tuning choices that gave the best predicted times also gave the best observed times, though in some cases the differences were slight.

The goal of our performance evaluation methodology was to estimate program execution time with sufficient accuracy to guide programmers in making tuning decisions, and to do this in a way that can be incorporated into application development relatively easily. Based on the experiments described in Section 5, we believe that we have met that goal. We conclude that the model, though simple, can be of practical value in application development. Future work could investigate (i) a wider range of archetypes and (ii) the applicability of the methodology to shared-memory architectures.

How well does the model predict performance? In some cases, actual and expected times agree consistently, especially when computation is more than half of the overall running time, and when a finer grain of benchmarking is used.

How useful is the model for making decisions? As demonstrated in Section 5, the model can help programmers choose between different data partitioning and granularity strategies. We conclude that the model, though simple, can be of use to an application developer.

Future Work: Problem Solving Environments. The performance tools we have described in this paper — including the methodology encapsulated by the workflow in Figure 1, the analytic models, and the accompanying simulation techniques — can be nicely managed when bundled with a Problem Solving Environment (PSE). According to Gallopoluous et al. [GHR94], PSEs provide "a framework that is all things to all people: they solve simple or complex problems, support rapid prototyping or detailed analysis, and can be used in introductory education or at the frontiers of science." As demonstrated by Cheng and Fox [CF96], integrating parallel programming paradigms in a software environment (in their example, programming the CM5 using the visualization software AVS)

[1] In most cases, predicted times are, as expected, conservative compared to observed times. Due to time constraints, we did not pursue the question of why in a few cases predicted times were optimistic. One possible explanation is that our assumptions about repeatability were not as valid as we thought: For example, we assumed that execution times on the IBM SP2 would not be affected by other users of the machine, since we had exclusive control of the particular nodes we were using; this assumption ignores possible contention for machine-wide communication resources and so might be invalid.

enables application developers to become more productive through useful provided tools.

PSEs represent a way to package a computational solution to a problem with the set of tools and methodologies. Employing these tools and methodologies, a scientist can formulate a problem, solve the problem, optimize the solution through refinement, and analyze the results. The PSE provides a user-friendly environment that is natural to the problem domain; for example, the PSE for Air Quality Models [DC97] provides an integrated user interface for defining, solving, and evaluating smog models. This PSE is integrated with the $3D + T + M^k$ archetype; this suggests that integrating it with the mesh and mesh-spectral archetypes would yield similar benefits. Additionally, the integration of the performance model with the problem solving environment further helps an application developer use an archetype.

This suggests another path for future work as well. The performance model and tools presented in this paper could be applied to other archetypes as well, including the one-deep divide and conquer archetype [MC96], which is a pattern that solves divide and conquer programs while only taking the recursion to a single depth. In addition, the performance analysis work done for the aforementioned air quality models [DM97] could be applied to the framework presented in this paper.

Future Work: Shared-Memory Architectures. Most of our experiments with archetype-based application development have targeted distributed-memory architectures. A major advantage of an archetype-based approach to developing applications for such archetypes is that a parallel programming archetype can specifically address one of the things that makes such applications difficult to develop, namely the distribution of data. This advantage could be equally useful for a shared-memory architecture for which data locality is crucial to performance — i.e., a shared-memory architecture that is most effectively used by treating it as a distributed-memory architecture. It would be relatively easy to port existing archetype implementations that use message-passing to such a machine, after which some of the experiments described in this and other papers on archetypes [CMMM95, MC96] could be repeated.

Whether an archetype-based approach has similar benefits when the target architecture supports a shared-memory model without performance penalties is a more difficult question. Massingill [Mas98] describes an archetype-based approach to application development one of whose stages can be converted in a straightforward way to a program for a shared-memory architecture, but again the experimental work focuses on the later stages of the process, whereby the original algorithm becomes a program for a distributed-memory architecture. Future work could experiment with using this process to develop practical applications for shared-memory architectures.

Future Work: Task-Parallel Problems. The performance model in this paper was used to evaluate different data partitions and distributions in SPMD programs written using archetypes. Future work could extend to evaluating the model's utility in analyzing different decompositions and mappings of task-parallel programs as well.

Future Work: Event-Oriented Problems. The overall goal of any distributed resource management system is the efficient matching of resource providers and requestors. Using events as our solutions' communication substrate, we can develop distributed control announce-listen algorithms that are both scalable and fault-tolerant [Sch96]. The announce-listen paradigm is used at the messaging layer to assist in resource location, reservation, and scheduling [RRDC97]. We have implemented this messaging facility in Java as *global events*.

Java Beans provide *local events* as a mechanism by which a component informs other components that something interesting has happened. These events can be thought of as active messages; for example, a button is pressed at a source, and channeled through an event listener, to trigger a method in an event observer automatically. An event propagates from an *event source* through an *event notifier* to one or more *event observers* that respond to the events as they arrive. The notifier routes the event to the observers using a control list, and observers can ask the notifier to be added or removed from this list without notifying the event source.

We have developed a global event structuring mechanism [CRS98] that is identical to the local event model of Java Beans, except that instead of Java Beans' referencing an object within a single Java Virtual Machine, we use a global name for the object, employing the Web's URL convention. Furthermore, because the components of the global event system are distributed, multicast can be used for efficient group communication, instead of Java Beans' local event point-to-point casting.

Using global events, an event is *announced* by a source object in one virtual machine, and notifiers for that event in other virtual machines anywhere on the Internet *listen* for the event and forward it to the appropriate (distributed) observers. Unlike the group communication in *virtual synchrony* [BvR94], it is not necessary for the event sources to know at any point who the event observers will be. Our global event model is useful not only to distribute events and the objects that use them, but also to compose event notifiers, to filter using predicates, and to provide security using access control lists at the event notifier level.

There are several advantages to using global events and soft state. The announce-listen paradigm is fault-resilient [Sch96]; that is, if a resource provider goes away, the system adapts dynamically to continue to meet the requests of the consumers. Furthermore, systems constructed using global events and multicast

are compositional and scalable; providers and consumers can add or remove themselves at any point dynamically. Unfortunately, such systems also have the potential for oscillation; that is, if state changes faster than the communication updates, then soft state may give a bad estimate of the current system state.

We are currently investigating the tradeoffs between soft state and hard invariants, between pushing and pulling resource requests and responses, and between a hierarchy of middlemen and a flat requestor-provider structure. The performance tools we have described in this paper — including the methodology encapsulated by the workflow in Figure 1, the analytic models, and the accompanying simulation techniques — can be used in conjunction with distributed programs communicating using events as the messaging facility, and this is an exciting area worthy of future exploration.

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A Mesh Programs

This appendix contains source code listings of the sequential applications, parallel applications, computational benchmark programs, and communication benchmark programs based on the mesh archetype and referenced in this paper. For more information about the archetype and its library routines, refer to [Mas96]. In reading these programs, observe that:

- PARAMETER values containing underscores (e.g., the definition of `NX` in the heat diffusion program) are intended to be replaced with numeric values by a preprocessor.
- INCLUDE files `mesh_uparms.h`, `mesh_parms.h`, and `mesh_common.h` (not shown) contain archetype constants and PARAMETERS; see [Mas96] for details.
- Routine `mytime` (not shown) samples wall-clock time; routine `mytimediff` (not shown) computes the difference in milliseconds between two such samples.

A.1 Heat Diffusion

Sequential Application Program.

```
C--------------------------------------------------------------------
C
C       program heat
C
C       explicitly solves the 1-D diffusion equation
C
C       make-time parameters:
C               NX = problem size
C               NSTEPS = number of time steps
C
C--------------------------------------------------------------------

        program heat

        implicit none
        integer NX
        parameter (NX=_NX_)
        integer NSTEPS
        parameter (NSTEPS=_NSTEPS_)

        integer IUNIT,OUNIT
        parameter (IUNIT=11,OUNIT=12)
        character*(*) OUTNAME
        parameter (OUTNAME='seq_heat.OUT')

        real uk(1:NX), ukp1(1:NX)
        integer istarts, istartms, istops, istopms, itimediff
        real dx, dt
        integer i, icnt, k

        call mytime(istarts, istartms)
```

```
        dx = 1.0/NX
        dt = 0.5*dx*dx

C       initialize
        print*, 'NX = ', NX
        print*, 'NSTEPS = ', NSTEPS
        open (unit=OUNIT, file=OUTNAME, status='unknown',
     -          access='sequential', form='formatted')
        do i=2,NX-1
           uk(i)=0.0
        enddo
        uk(1)=1.0
        uk(NX)=1.0

C       time step loop
        do k=1,NSTEPS
            do i=2,NX-1
                ukp1(i)=uk(i)+(dt/(dx*dx))*(uk(i+1)-2*uk(i)+uk(i-1))
            enddo
            do i=2,NX-1
                uk(i)=ukp1(i)
            enddo
C           write (OUNIT,*) 'timestep ', k
C           write (OUNIT, 25) (uk(I),I=1,NX)
C25         format(4X,E15.5)
        enddo
        write (OUNIT,*) 'timestep ', NSTEPS
        icnt=min(5,NSTEPS/2)
        do i=1,icnt
                write (OUNIT,'(4X,I8,E15.5)') i, uk(i)
        enddo
        do i=NX-icnt+1,NX
                write (OUNIT,'(4X,I8,E15.5)') i, uk(i)
        enddo

        close(unit=OUNIT)
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'sequential time:  ', itimediff
        end

C-----------------------------------------------------------------------
```

Parallel Application Program.

```
C-----------------------------------------------------------------------
C
C       program heat
C
C       explicitly solves the 1-D diffusion equation
C
C       make-time parameters:
C               NX = problem size
C               XPROCS = number of grid processes
C               NSTEPS = number of time steps
C
C-----------------------------------------------------------------------

        subroutine hostmain

        include 'mesh_uparms.h'
        include 'mesh_parms.h'
        include 'mesh_common.h'
```

```
C       moved to archetype file mesh_uparms.h
C       integer NX
C       parameter (NX=_NX_)
        integer NSTEPS
        parameter (NSTEPS=_NSTEPS_)

        integer IUNIT,OUNIT
        parameter (IUNIT=11,OUNIT=12)
        character*(*) OUTNAME1, OUTNAME2
        parameter (OUTNAME1='par_heat_', OUTNAME2='.OUT')

        real uk(1:NX)
        integer istarts, istartms, istops, istopms, itimediff
        real dx, dt
        integer i, icnt
        character*80 outname
        character*4 cbuff
        integer cblen

        call mytime(istarts, istartms)

        dx = 1.0/NX
        dt = 0.5*dx*dx

C       initialize

        print*, 'NX = ', NX
        print*, 'XPROCS = ', XPROCS
        print*, 'NSTEPS = ', NSTEPS

C       build output filename
        if (XPROCS .le. 9) then
                write (cbuff, '(3i1.1)') XPROCS
                cblen=1
        else
                write (cbuff, '(3i2.2)') XPROCS
                cblen=2
        endif
        outname = OUTNAME1 // cbuff(1:cblen) // OUTNAME2

        open (unit=OUNIT, file=outname, status='unknown',
     -          access='sequential', form='formatted')
        do i=2,NX-1
           uk(i)=0.0
        enddo
        uk(1)=1.0
        uk(NX)=1.0
        call mesh_HtoG_host(uk)


C       time step loop
        do k=1,NSTEPS
C           call mesh_GtoH_host(uk)
C           write (OUNIT,*) 'timestep ', k
C           write (OUNIT, 25) (uk(I),I=1,NX)
C25         format(4X,E15.5)
        enddo
        call mesh_GtoH_host(uk)
        write (OUNIT,*) 'timestep ', NSTEPS
        icnt=min(5,NSTEPS/2)
        do i=1,icnt
                write (OUNIT,'(4X,I8,E15.5)') i, uk(i)
        enddo
        do i=NX-icnt+1,NX
```

```
               write (OUNIT,'(4X,I8,E15.5)') i, uk(i)
            enddo

            close(unit=OUNIT)
            call mytime(istops, istopms)
            call mytimediff(istarts, istartms, istops, istopms,
     $           itimediff)
            print*, 'host:  ', itimediff
            end

C-----------------------------------------------------------------------

            subroutine gridmain

            include 'mesh_uparms.h'
            include 'mesh_parms.h'
            include 'mesh_common.h'

C           moved to archetype file mesh_uparms.h
C           integer NX
C           parameter (NX=_NX_)
            integer NSTEPS
            parameter (NSTEPS=_NSTEPS_)

            real uk(IXLO:IXHI),ukp1(IXLO:IXHI)
            integer istarts, istartms, istops, istopms, itimediff
            logical iempty
            integer istart, iend
            integer i, k
            real dx, dt

            call mytime(istarts, istartms)

            dx = 1.0/NX
            dt = 0.5*dx*dx

C           initialize
            call mesh_HtoG_grid(uk)
            call xintersect(2,NX-1,istart,iend,iempty)

C           time step loop
            do k=1,NSTEPS
                call mesh_update_bdry(uk)
                do i=istart,iend
                    ukp1(i)=uk(i)+(dt/(dx*dx))*(uk(i+1)-2*uk(i)+uk(i-1))
                enddo
                do i=istart,iend
                    uk(i)=ukp1(i)
                enddo
C               call mesh_GtoH_grid(uk)
            enddo
            call mesh_GtoH_grid(uk)

            call mytime(istops, istopms)
            call mytimediff(istarts, istartms, istops, istopms,
     $           itimediff)
            print*, 'process ', iprocx, ': ', itimediff

            end

C-----------------------------------------------------------------------
```

Computational Benchmark Program.

```
C-----------------------------------------------------------------------
C
C       benchmark version
C
C       make-time parameters:
C               NX = problem size
C               NSTEPS = number of time steps
C
C       may also need to adjust loops bounded by klim
C
C-----------------------------------------------------------------------

        program heat
C
C       explicitly solves the 1-D diffusion equation
C
        implicit none
        integer NX
        parameter (NX=_NX_)
        integer NSTEPS
        parameter (NSTEPS=_NSTEPS_)

        integer IUNIT,OUNIT
        parameter (IUNIT=11,OUNIT=12)
        character*(*) OUTNAME1, OUTNAME2
        parameter (OUTNAME1='bench_heat', OUTNAME2='.OUT')

        real uk(1:NX), ukp1(1:NX)
        integer istarts, istartms, istops, istopms, itimediff
        real dx, dt
        integer k, klim, i, icnt
        character*80 outname
        character*4 cbuff
        integer cblen

        dx = 1.0/NX
        dt = 0.5*dx*dx

        print*, 'NX = ', NX
        print*, 'NSTEPS = ', NSTEPS

C-------benchmark initialization
        call mytime(istarts, istartms)
        klim = 10000
        do k = 1, klim
C       initialize
                do i= 2,NX-1
                uk(I)=0.0
                enddo
                uk(1)=1.0
                uk(NX)=1.0
        enddo
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'initialization:  ', klim, itimediff,
     $          dble(itimediff)/dble(klim)

C-------benchmark time step
        call mytime(istarts, istartms)
C       time step loop
        klim = 10000
        do k = 1, klim
```

```
C       do k=1,NSTEPS
            do i=2,NX-1
                ukp1(i)=uk(i)+(dt/(dx*dx))*(uk(i+1)-2*uk(i)+uk(i-1))
            enddo
            do i=2,NX-1
                uk(i)=ukp1(i)
            enddo
C           print*, 'timestep ', k
C           print 25,(uk(I),I=1,NX)
C25         format(4X,E15.5)
C       enddo
        enddo
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'computation:  ', klim, itimediff,
     $          dble(itimediff)/dble(klim)

c-------benchmark output operation
        call mytime(istarts, istartms)
        klim = 10
        do k = 1, klim
c               build output filename (dummy version)
                write (cbuff, '(3i1.1)') 0
                cblen=1
                outname = OUTNAME1 // OUTNAME2
c               open and write
                open (unit=OUNIT, file=outname, status='unknown',
     -                  access='sequential', form='formatted')
                write (OUNIT,*) 'timestep ', NSTEPS
                icnt = min(5,NSTEPS/2)
                do i=1,icnt
                write (OUNIT,'(4X,I8,E15.5)') i, uk(i)
                enddo
                do i=NX-icnt+1,NX
                write (OUNIT,'(4X,I8,E15.5)') i, uk(i)
                enddo
                close(unit=OUNIT)
        enddo
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'output:  ', klim, itimediff,
     $          dble(itimediff)/dble(klim)

        end
C--------------------------------------------------------------------------
```

Communication Benchmark Program.

```
C--------------------------------------------------------------------------
C
C       program bench_mesh
C       written by adam rifkin, adam@cs.caltech.edu, 1996
C       modified by berna massingill
C
C       calculates times for the archetype library routines
C
C       make-time parameters:
C               NX = problem size
C               XPROCS = number of grid processes
C               NTIMES = number of times to execute comm. routines
C
C       may also need to adjust loops bounded by klim
```

```
C
C--------------------------------------------------------------------

        subroutine hostmain

        include 'mesh_uparms.h'
        include 'mesh_parms.h'
        include 'mesh_common.h'

C       moved to archetype file mesh_uparms.h
C       integer NX
C       parameter (NX=_NX_)
        integer NTIMES
        parameter (NTIMES=_NTIMES_)

        real uk(1:NX)
        integer istarts, istartms, istops, istopms, itimediff

        print*, 'NX= ', NX
        print*, 'XPROCS= ', XPROCS
        print*, 'NTIMES= ', NTIMES

C------ benchmark mesh_GtoH_host

        call mytime(istarts, istartms)
        klim = NTIMES
        do k=1,klim
                call mesh_GtoH_host(uk)
        enddo
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'mesh_GtoH_host:  ', klim, itimediff,
     $          dble(itimediff)/dble(klim)

C------ benchmark mesh_HtoG_host

        call mytime(istarts, istartms)
        klim = NTIMES
        do k=1,klim
                call mesh_HtoG_host(uk)
        enddo
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'mesh_HtoG_host:  ', klim, itimediff,
     $          dble(itimediff)/dble(klim)
        end

C--------------------------------------------------------------------

        subroutine gridmain

        include 'mesh_uparms.h'
        include 'mesh_parms.h'
        include 'mesh_common.h'

C       moved to archetype file mesh_uparms.h
C       integer NX
C       parameter (NX=_NX_)
        integer NTIMES
        parameter (NTIMES=_NTIMES_)

        real uk(IXLO:IXHI),ukp1(IXLO:IXHI)
        integer istarts, istartms, istops, istopms, itimediff
```

```
C------ benchmark mesh_GtoH_grid

        call mytime(istarts, istartms)
        klim = NTIMES
        do k=1,klim
                call mesh_GtoH_grid(uk)
        enddo
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'mesh_GtoH_grid process ', iprocx, ':  ', klim,
     $          itimediff,
     $          dble(itimediff)/dble(klim)

C------ benchmark mesh_HtoG_grid

        call mytime(istarts, istartms)
        klim = NTIMES
        do k=1,klim
                call mesh_HtoG_grid(uk)
        enddo
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'mesh_HtoG_grid process ', iprocx, ':  ', klim,
     $          itimediff,
     $          dble(itimediff)/dble(klim)

C------ benchmark mesh_update_bdry

        call mytime(istarts, istartms)
        klim = NTIMES
        do k=1,klim
                call mesh_update_bdry(uk)
        enddo
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'mesh_update_bdry process ', iprocx, ':  ', klim,
     $          itimediff,
     $          dble(itimediff)/dble(klim)

C------ benchmark xintersect

        call mytime(istarts, istartms)
        klim = 1000000
        do k=1,klim
                call xintersect(2,NX-1,ibegin,iend,iempty)
        enddo
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'xintersect process ', iprocx, ':  ', klim,
     $          itimediff,
     $          dble(itimediff)/dble(klim)

        end

C--------------------------------------------------------------------------
```

A.2 Poisson Solver

Sequential Application Program.

```
C-----------------------------------------------------------------------
C
C       program poisson
C
C       uses Jacobi relaxation to solve the Poisson equation
C
C       make-time parameters:
C               NX, NY = problem size
C               MAXSTEPS = maximum number of iterations
C
C-----------------------------------------------------------------------

        program poisson

        integer NX
        integer NY
        parameter (NX=_NX_)
        parameter (NY=_NY_)

        real H
        parameter (H=0.05)
C       how often to check for convergence
        integer NCHECK
        parameter (NCHECK=10)
C       convergence criterion
        real TOL
        parameter (TOL=0.00001)
C       maximum number of steps
        integer MAXSTEPS
        parameter (MAXSTEPS=_MAXSTEPS_)

C       file units, names
        integer IUNIT,OUNIT
        parameter (IUNIT=11,OUNIT=12)
        character*(*) OUTNAME
        parameter (OUTNAME='seq_poisson.OUT')

        external F
        external G
        real uk(1:NX,1:NY), ukp1(1:NX,1:NY)
        real diff, diffmax
        integer istarts, istartms, istops, istopms, itimediff

C       initialize
        call mytime(istarts, istartms)
        print*, 'NX = ', NX
        print*, 'NY = ', NY
        print*, 'NCHECK = ', NCHECK
        open (unit=OUNIT, file=OUTNAME, status='unknown',
     -          access='sequential', form='formatted')
C       interior points
        do j = 2, NY-1
        do i = 2, NX-1
                uk(i,j) = F(i,j,NX,NY,H)
        enddo
        enddo
C       boundary points
        do j = 1, NY
                uk(1,j) = G(1,j,NX,NY,H)
                uk(NX,j) = G(NX,j,NX,NY,H)
        enddo
```

```
        do i = 2, NX-1
                uk(i,1) = G(i,1,NX,NY,H)
                uk(i,NY) = G(i,NY,NX,NY,H)
        enddo

C       loop until convergence
        diffmax = TOL + 1.0

        do k=1,MAXSTEPS

C       compute new values
        do j = 2, NY-1
        do i = 2, NX-1
                ukp1(i,j) = 0.25*(H*H*F(i,j,NX,NY,H)
     -                  + uk(i-1,j) + uk(i,j-1)
     -                  + uk(i+1,j) + uk(i,j+1) )
        enddo
        enddo
C       every NCHECK-th step, recompute convergence test
        if (mod(k,NCHECK) .eq. 0) then
                diffmax = 0.0
                do j = 2, NY-1
                do i = 2, NX-1
                        diff = abs(ukp1(i,j) - uk(i,j))
                        if (diff .gt. diffmax) diffmax = diff
                enddo
                enddo
        endif
C       copy new values to old values
        do j = 2, NY-1
        do i = 2, NX-1
                uk(i,j) = ukp1(i,j)
        enddo
        enddo

C       check for convergence
        if (diffmax .le. TOL) go to 1000

        enddo

C       print results
1000    continue
        write (OUNIT,*) 'NX, NY = ', NX, NY
        write (OUNIT,*) 'H = ', H
        write (OUNIT,*) 'tolerance = ', TOL
        write (OUNIT,*) 'NCHECK = ', NCHECK
        call Fprint(OUNIT)
        call Gprint(OUNIT)

        if (diffmax .le. TOL) then
                write (OUNIT,*) 'convergence occurred in ', k, ' steps'
                print*, 'steps  = ', k
        else
                write (OUNIT,*) 'no convergence in ', MAXSTEPS,
     -                  ' steps; ', 'max. difference ', diffmax
                print*, 'steps  = ', MAXSTEPS
        endif

c       do i = 1, NX
c               if (NX .gt. 10) write (OUNIT,*) ' '
c               write (OUNIT,9999) (uk(i,j), j = 1, NY)
        do i = 1, NX, NX/5
                do j = 1, NY, NY/5
                        write (OUNIT,9998) i, j, uk(i,j)
                enddo
```

```
                write (OUNIT,9998) i, NY, uk(i,NY)
                write (OUNIT,*) ' '
        enddo
        do j = 1, NY, NY/5
                write (OUNIT,9998) NX, j, uk(NX,j)
        enddo
        write (OUNIT,9998) NX, NY, uk(NX,NY)
9998    format(2i10,f8.4)
9999    format(6F8.4)

        close(unit=OUNIT)
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'sequential time:  ', itimediff
        end

C-----------------------------------------------------------------------

        real function F(i,j,nx,ny,h)
        integer i, j, nx, ny
        real h

        F = 0.0
        end

        subroutine Fprint(ounit)
        integer ounit
        write (ounit,*) 'F(i,j) = 0.0'
        end

C-----------------------------------------------------------------------

        real function G(i,j,nx,ny,h)
        integer i, j, nx, ny
        real h

        G = (i+j)*h
        end

        subroutine Gprint(ounit)
        integer ounit
        write (ounit,*) 'G(i,j) = (i+j)*H'
        end

C-----------------------------------------------------------------------
```

Parallel Application Program.

```
C-----------------------------------------------------------------------
C
C       program poisson
C
C       uses Jacobi relaxation to solve the Poisson equation
C
C       make-time parameters:
C               NX, NY = problem size
C               XPROCS, YPROCS = number of grid processes
C               MAXSTEPS = maximum number of iterations
C
C-----------------------------------------------------------------------

C       integer NX
C       integer NY
```

```
C       parameter (NX=_NX_)
C       parameter (NY=_NY_)

C-----------------------------------------------------------------------

        subroutine hostmain

        include 'mesh_uparms.h'
        include 'mesh_parms.h'
        include 'mesh_common.h'

        real H
        parameter (H=0.05)
C       how often to check for convergence
        integer NCHECK
        parameter (NCHECK=10)
C       convergence criterion
        real TOL
        parameter (TOL=0.00001)
C       maximum number of steps
        integer MAXSTEPS
        parameter (MAXSTEPS=_MAXSTEPS_)

C       file units, names
        integer IUNIT,OUNIT
        parameter (IUNIT=11,OUNIT=12)
        character*(*) OUTNAME1, OUTNAME2
        parameter (OUTNAME1='par_poisson_', OUTNAME2='.OUT')

        external F
        external G
        real uk(1:NX,1:NY)
        real difflocal, diffmax
        integer istarts, istartms, istops, istopms, itimediff
        character*80 outname
        character*4 cbuff1,cbuff2
        integer cblen1, cblen2

C       initialize
        call mytime(istarts, istartms)
        print*, 'NX = ', NX
        print*, 'NY = ', NY
        print*, 'XPROCS = ', XPROCS
        print*, 'YPROCS = ', YPROCS
        print*, 'NCHECK = ', NCHECK

C       build output filename
        if (XPROCS .le. 9) then
                write (cbuff1, '(3i1.1)') XPROCS
                cblen1=1
        else
                write (cbuff1, '(3i2.2)') XPROCS
                cblen1=2
        endif
        if (YPROCS .le. 9) then
                write (cbuff2, '(3i1.1)') YPROCS
                cblen2=1
        else
                write (cbuff2, '(3i2.2)') YPROCS
                cblen2=2
        endif
        outname = OUTNAME1 // cbuff1(1:cblen1) // '_'
     -          // cbuff2(1:cblen2) // OUTNAME2

        open (unit=OUNIT, file=outname, status='unknown',
```

```
     -          access='sequential', form='formatted')
C       interior points
        do j = 2, NY-1
        do i = 2, NX-1
                uk(i,j) = F(i,j,NX,NY,H)
        enddo
        enddo
C       boundary points
        do j = 1, NY
                uk(1,j) = G(1,j,NX,NY,H)
                uk(NX,j) = G(NX,j,NX,NY,H)
        enddo
        do i = 2, NX-1
                uk(i,1) = G(i,1,NX,NY,H)
                uk(i,NY) = G(i,NY,NX,NY,H)
        enddo
C       move to grid
        call mesh_HtoG_host(uk)

C       loop until convergence
        diffmax = TOL + 1.0

        do k=1,MAXSTEPS

C       compute new values
C       (computation in grid only)
C       every NCHECK-th step, recompute convergence test
        if (mod(k,NCHECK) .eq. 0) then
C               (computation in grid only)
                call mesh_merge_real_maxabs(1, difflocal, diffmax)
        endif
C       copy new values to old values
C       (computation in grid only)

C       check for convergence
        if (diffmax .le. TOL) go to 1000

        enddo

C       print results
1000    continue
        call mesh_GtoH_host(uk)
        write (OUNIT,*) 'NX, NY = ', NX, NY
        write (OUNIT,*) 'H = ', H
        write (OUNIT,*) 'tolerance = ', TOL
        write (OUNIT,*) 'NCHECK = ', NCHECK
        call Fprint(OUNIT)
        call Gprint(OUNIT)

        if (diffmax .le. TOL) then
                write (OUNIT,*) 'convergence occurred in ', k, ' steps'
                print*, 'steps  = ', k
        else
                write (OUNIT,*) 'no convergence in ', MAXSTEPS,
     -                  ' steps; ', 'max. difference ', diffmax
                print*, 'steps  = ', MAXSTEPS
        endif

c       do i = 1, NX
c               if (NX .gt. 10) write (OUNIT,*) ' '
c               write (OUNIT,9999) (uk(i,j), j = 1, NY)
        do i = 1, NX, NX/5
                do j = 1, NY, NY/5
                        write (OUNIT,9998) i, j, uk(i,j)
                enddo
```

```
                write (OUNIT,9998) i, NY, uk(i,NY)
                write (OUNIT,*) ' '
        enddo
        do j = 1, NY, NY/5
                write (OUNIT,9998) NX, j, uk(NX,j)
        enddo
        write (OUNIT,9998) NX, NY, uk(NX,NY)
9998    format(2i10,f8.4)
9999    format(6F8.4)

        close(unit=OUNIT)
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'host:  ', itimediff
        end

C-----------------------------------------------------------------------

        subroutine gridmain

        include 'mesh_uparms.h'
        include 'mesh_parms.h'
        include 'mesh_common.h'

        real H
        parameter (H=0.05)
C       how often to check for convergence
        integer NCHECK
        parameter (NCHECK=10)
C       convergence criterion
        real TOL
        parameter (TOL=0.00001)
C       maximum number of steps
        integer MAXSTEPS
        parameter (MAXSTEPS=_MAXSTEPS_)

        external F
        external G
        real uk(IXLO:IXHI,IYLO:IYHI), ukp1(1:NXlsize,1:NYlsize)
        real diff, difflocal, diffmax
        logical iempty, jempty
        integer istarts, istartms, istops, istopms, itimediff

C       initialize
        call mytime(istarts, istartms)
C       (initialization in host only)
        call mesh_HtoG_grid(uk)

C       compute loop bounds
        call xintersect(2, NX-1, istart, iend, iempty)
        call yintersect(2, NY-1, jstart, jend, jempty)
C       compute starting global indices (of local section)
        call iglobal(iprocx, istart, istartg)
        call jglobal(iprocy, jstart, jstartg)
C       compute offsets (global index = offset + local index)
        igoffset = istartg - istart
        jgoffset = jstartg - jstart

C       loop until convergence
        diffmax = TOL + 1.0

        do k=1,MAXSTEPS

C       refresh ghost boundaries
```

```
        call mesh_update_bdry(uk)
C       compute new values
        do j = jstart, jend
        do i = istart, iend
                ukp1(i,j) = 0.25*(H*H*F(igoffset+i,jgoffset+j,NX,NY,H)
     -                  + uk(i-1,j) + uk(i,j-1)
     -                  + uk(i+1,j) + uk(i,j+1) )
        enddo
        enddo
C       every NCHECK-th step, recompute convergence test
        if (mod(k,NCHECK) .eq. 0) then
                difflocal = 0.0
                do j = jstart, jend
                do i = istart, iend
                        diff = abs(ukp1(i,j) - uk(i,j))
                        if (diff .gt. difflocal) difflocal = diff
                enddo
                enddo
                call mesh_merge_real_maxabs(1, difflocal, diffmax)
        endif
C       copy new values to old values
        do j = jstart, jend
        do i = istart, iend
                uk(i,j) = ukp1(i,j)
        enddo
        enddo

C       check for convergence
        if (diffmax .le. TOL) go to 1000

        enddo

C       print results
1000    continue
C       (printing in host only)
        call mesh_GtoH_grid(uk)

        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'process ', iprocx, ':  ', itimediff
        end

C-----------------------------------------------------------------------

        real function F(i,j,nx,ny,h)
        integer i, j, nx, ny
        real h

        F = 0.0
        end

        subroutine Fprint(ounit)
        integer ounit
        write (ounit,*) 'F(i,j) = 0.0'
        end

C-----------------------------------------------------------------------

        real function G(i,j,nx,ny,h)
        integer i, j, nx, ny
        real h

        G = (i+j)*h
        end
```

```
        subroutine Gprint(ounit)
        integer ounit
        write (ounit,*) 'G(i,j) = (i+j)*H'
        end

C-----------------------------------------------------------------------
```

Computational Benchmark Program.

```
C-----------------------------------------------------------------------
C
C       benchmark version
C
C       make-time parameters:
C               NX, NY = problem size
C               XPROCS, YPROCS = number of grid processes
C               MAXSTEPS = maximum number of iterations
C
C       may also need to adjust loops bounded by klim
C
C-----------------------------------------------------------------------

        program poisson
C
C       uses Jacobi relaxation to solve the Poisson equation
C
        integer NX
        integer NY
        parameter (NX=_NX_)
        parameter (NY=_NY_)

        real H
        parameter (H=0.05)
C       how often to check for convergence
        integer NCHECK
        parameter (NCHECK=10)
C       convergence criterion
        real TOL
        parameter (TOL=0.00001)
C       maximum number of steps
        integer MAXSTEPS
        parameter (MAXSTEPS=_MAXSTEPS_)

C       file units, names
        integer IUNIT,OUNIT
        parameter (IUNIT=11,OUNIT=12)
        character*(*) OUTNAME1, OUTNAME2
        parameter (OUTNAME1='bench_poisson', OUTNAME2='.OUT')

        external F
        external G
        real uk(1:NX,1:NY), ukp1(1:NX,1:NY)
        real diff, diffmax
        integer istarts, istartms, istops, istopms, itimediff
        character*80 outname
        character*4 cbuff1,cbuff2
        integer cblen1, cblen2

        print*, 'NX = ', NX
        print*, 'NY = ', NY

C-------benchmark initialization
        call mytime(istarts, istartms)
```

```
        klim = 1000
        do k=1,klim
C       initialize
C               interior points
                do j = 2, NY-1
                do i = 2, NX-1
                        uk(i,j) = F(i,j,NX,NY,H)
                enddo
                enddo
C               boundary points
                do j = 1, NY
                        uk(1,j) = G(1,j,NX,NY,H)
                        uk(NX,j) = G(NX,j,NX,NY,H)
                enddo
                do i = 2, NX-1
                        uk(i,1) = G(i,1,NX,NY,H)
                        uk(i,NY) = G(i,NY,NX,NY,H)
                enddo
        enddo
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'initialization:  ', klim, itimediff,
     $          dble(itimediff)/dble(klim)

C       loop until convergence
c       diffmax = TOL + 1.0

c       do k=1,MAXSTEPS

C-------benchmark computation
        igoffset=0
        jgoffset=0
        call mytime(istarts, istartms)
        klim = 1000
        do k=1,klim
C       compute new values
                do j = 2, NY-1
                do i = 2, NX-1
                ukp1(i,j) = 0.25*(H*H*F(igoffset+i,jgoffset+j,NX,NY,H)
     -                  + uk(i-1,j) + uk(i,j-1)
     -                  + uk(i+1,j) + uk(i,j+1) )
                enddo
                enddo
        enddo
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'computation:  ', klim, itimediff,
     $          dble(itimediff)/dble(klim)

C       every NCHECK-th step, recompute convergence test
c       if (mod(k,NCHECK) .eq. 0) then
C-------benchmark convergence test
        call mytime(istarts, istartms)
        klim = 1000
        do k=1,klim
                diffmax = 0.0
                do j = 2, NY-1
                do i = 2, NX-1
                        diff = abs(ukp1(i,j) - uk(i,j))
                        if (diff .gt. diffmax) diffmax = diff
                enddo
                enddo
        enddo
```

```
         call mytime(istops, istopms)
         call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
         print*, 'convergence test:  ', klim, itimediff,
     $          dble(itimediff)/dble(klim)

c        endif

C-------benchmark copy
         call mytime(istarts, istartms)
         klim = 1000
         do k=1,klim
C                copy new values to old values
                 do j = 2, NY-1
                 do i = 2, NX-1
                         uk(i,j) = ukp1(i,j)
                 enddo
                 enddo
         enddo
         call mytime(istops, istopms)
         call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
         print*, 'copy:  ', klim, itimediff,
     $          dble(itimediff)/dble(klim)

C        check for convergence
c        if (diffmax .le. TOL) go to 1000

c        enddo

C-------benchmark output
         call mytime(istarts, istartms)
         klim = 100
         do k=1,klim
C                build output filename (dummy version)
                 write (cbuff1, '(3i1.1)') 0
                 cblen1=1
                 write (cbuff2, '(3i1.1)') 0
                 cblen2=1
                 outname = OUTNAME1 // OUTNAME2
c                open and write
                 open (unit=OUNIT, file=outname, status='unknown',
     -                   access='sequential', form='formatted')
                 write (OUNIT,*) 'NX, NY = ', NX, NY
                 write (OUNIT,*) 'H = ', H
                 write (OUNIT,*) 'tolerance = ', TOL
                 write (OUNIT,*) 'NCHECK = ', NCHECK
                 call Fprint(OUNIT)
                 call Gprint(OUNIT)

                 if (diffmax .le. TOL) then
                         write (OUNIT,*)
     -                           'convergence occurred in ', k, ' steps'
c                        print*, 'steps  = ', k
                 else
                         write (OUNIT,*) 'no convergence in ', MAXSTEPS,
     -                           ' steps; ', 'max. difference ', diffmax
c                        print*, 'steps  = ', MAXSTEPS
                 endif

c                do i = 1, NX
c                        if (NX .gt. 10) write (OUNIT,*) ' '
c                        write (OUNIT,9999) (uk(i,j), j = 1, NY)
                 do i = 1, NX, NX/5
                         do j = 1, NY, NY/5
```

```
                                write (OUNIT,9998) i, j, uk(i,j)
                        enddo
                        write (OUNIT,9998) i, NY, uk(i,NY)
                        write (OUNIT,*) ' '
                enddo
                do j = 1, NY, NY/5
                        write (OUNIT,9998) NX, j, uk(NX,j)
                enddo
                write (OUNIT,9998) NX, NY, uk(NX,NY)
9998            format(2i10,f8.4)
9999            format(6F8.4)

                close(unit=OUNIT)
        enddo
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'output:  ', klim, itimediff,
     $          dble(itimediff)/dble(klim)

        end

C--------------------------------------------------------------------------

        real function F(i,j,nx,ny,h)
        integer i, j, nx, ny
        real h

        F = 0.0
        end

        subroutine Fprint(ounit)
        integer ounit
        write (ounit,*) 'F(i,j) = 0.0'
        end

C--------------------------------------------------------------------------

        real function G(i,j,nx,ny,h)
        integer i, j, nx, ny
        real h

        G = (i+j)*h
        end

        subroutine Gprint(ounit)
        integer ounit
        write (ounit,*) 'G(i,j) = (i+j)*H'
        end

C--------------------------------------------------------------------------
```

Communication Benchmark Program.

```
C--------------------------------------------------------------------------
C
C       program bench_mesh
C       written by adam rifkin, adam@cs.caltech.edu, 1996
C       modified by berna massingill
C
C       calculates times for the archetype library routines
C
C       make-time parameters:
C               NX, NY = problem size
```

```
C               XPROCS, YPROCS = number of grid processes
C               NTIMES = number of times to execute comm. routines
C
C       may also need to adjust loops bounded by klim
C
C-----------------------------------------------------------------------

        subroutine hostmain

        include 'mesh_uparms.h'
        include 'mesh_parms.h'
        include 'mesh_common.h'

        integer NTIMES
        parameter (NTIMES=_NTIMES_)

        real uk(1:NX,1:NY)
        real difflocal, diffmax
        integer istarts, istartms, istops, istopms, itimediff

        print*, 'NX= ', NX
        print*, 'NY= ', NY
        print*, 'XPROCS= ', XPROCS
        print*, 'YPROCS= ', YPROCS
        print*, 'NTIMES= ', NTIMES

C------ benchmark mesh_GtoH_host

        call mytime(istarts, istartms)
        klim = NTIMES
        do k=1,klim
                call mesh_GtoH_host(uk)
        enddo
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'mesh_GtoH_host:  ', klim, itimediff,
     $          dble(itimediff)/dble(klim)

C------ benchmark mesh_HtoG_host

        call mytime(istarts, istartms)
        klim = NTIMES
        do k=1,klim
                call mesh_HtoG_host(uk)
        enddo
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'mesh_HtoG_host:  ', klim, itimediff,
     $          dble(itimediff)/dble(klim)

C------ benchmark mesh_merge_real_maxabs

        call mytime(istarts, istartms)
        klim = NTIMES
        do k=1,klim
                call mesh_merge_real_maxabs(1, difflocal, diffmax)
        enddo
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'mesh_merge_real_maxabs host:  ', klim, itimediff,
     $          dble(itimediff)/dble(klim)
```

```
        end

C-----------------------------------------------------------------------

        subroutine gridmain

        include 'mesh_uparms.h'
        include 'mesh_parms.h'
        include 'mesh_common.h'

        integer NTIMES
        parameter (NTIMES=_NTIMES_)

        real uk(IXLO:IXHI,IYLO:IYHI)
        real difflocal, diffmax
        logical iempty, jempty
        integer istarts, istartms, istops, istopms, itimediff

C------ benchmark mesh_GtoH_grid

        call mytime(istarts, istartms)
        klim = NTIMES
        do k=1,klim
                call mesh_GtoH_grid(uk)
        enddo
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'mesh_GtoH_grid process ', iprocx, iprocy, ':  ', klim,
     $          itimediff,
     $          dble(itimediff)/dble(klim)

C------ benchmark mesh_HtoG_grid

        call mytime(istarts, istartms)
        klim = NTIMES
        do k=1,klim
                call mesh_HtoG_grid(uk)
        enddo
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'mesh_HtoG_grid process ', iprocx, iprocy, ':  ', klim,
     $          itimediff,
     $          dble(itimediff)/dble(klim)

C------ benchmark mesh_merge_real_maxabs

        call mytime(istarts, istartms)
        klim = NTIMES
        do k=1,klim
                call mesh_merge_real_maxabs(1, difflocal, diffmax)
        enddo
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'mesh_merge_real_maxabs process ', iprocx, iprocy,
     $          ':  ', klim,
     $          itimediff,
     $          dble(itimediff)/dble(klim)

C------ benchmark mesh_update_bdry

        call mytime(istarts, istartms)
        klim = NTIMES
```

```
        do k=1,klim
                call mesh_update_bdry(uk)
        enddo
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'mesh_update_bdry process ', iprocx, iprocy,
     $          ':  ', klim,
     $          itimediff,
     $          dble(itimediff)/dble(klim)

C------ benchmark xintersect

        call mytime(istarts, istartms)
        klim = 100000
        do k=1,klim
                call xintersect(2,NX-1,i1,i2,iempty)
        enddo
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'xintersect process ', iprocx, iprocy, ':  ', klim,
     $          itimediff,
     $          dble(itimediff)/dble(klim)

C------ benchmark yintersect

        call mytime(istarts, istartms)
        klim = 100000
        do k=1,klim
                call yintersect(2,NY-1,j1,j2,jempty)
        enddo
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'yintersect process ', iprocx, iprocy, ':  ', klim,
     $          itimediff,
     $          dble(itimediff)/dble(klim)

C------ benchmark iglobal

        call mytime(istarts, istartms)
        klim = 100000
        do k=1,klim
                call iglobal(iprocx,1,i1)
        enddo
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'iglobal process ', iprocx, iprocy, ':  ', klim,
     $          itimediff,
     $          dble(itimediff)/dble(klim)

C------ benchmark jglobal

        call mytime(istarts, istartms)
        klim = 100000
        do k=1,klim
                call jglobal(iprocy,1,j1)
        enddo
        call mytime(istops, istopms)
        call mytimediff(istarts, istartms, istops, istopms,
     $          itimediff)
        print*, 'jglobal process ', iprocx, iprocy, ':  ', klim,
     $          itimediff,
```

```
     $          dble(itimediff)/dble(klim)
        end

C--------------------------------------------------------------------
```

B Mesh-Spectral Programs

This appendix contains source code listings of the sequential applications, parallel applications, computational benchmark programs, and communication benchmark programs based on the mesh-spectral archetype and referenced in this paper. For more information about the archetype and its library routines, refer to [DM96]. In reading these programs, observe that:

- INCLUDE files `arch_uparms.h` and `arch_parms.h` (not shown) contain archetype constants and PARAMETERS; see [DM96] for details. Other INCLUDE files not shown (for example, `par_fft_header.h` and `par_fft_wrapper.h` in the parallel 2D FFT program) are generated by the archetype's utility program for generating header files; see [DM96] for details and examples.
- Routine `mytime` (not shown) samples wall-clock time; routine `mytimediff` (not shown) computes the difference in milliseconds between two such samples.

B.1 Two-dimensional Fast Fourier Transform

Sequential Application Program.

```
c--------------------------------------------------------------------------
c
c     example of mesh/spectral archetype
c
c     2D FFT
c
c     make-time parameters:
c         NX, NY = dimensions of grid
c
c--------------------------------------------------------------------------

c--------------------------------------------------------------------------
c
c     main program
c
c--------------------------------------------------------------------------

      program main
      implicit none
c     include 'arch_uparms.h'
c     include 'arch_parms.h'
c     include 'seq_fft_header.h'

c     processors (MAXPROCS)
c     call spawn(procs)
c     end

c--------------------------------------------------------------------------
```

```
c
c     process-main program
c
c-----------------------------------------------------------------------

c     subroutine procmain()
c     implicit none
c     include 'arch_uparms.h'
c     include 'arch_parms.h'
      include 'seq_fft_header.h'

      integer nrepeats
      parameter (nrepeats=10)

      integer IUNIT,OUNIT
      parameter (IUNIT=11,OUNIT=12)
      character*(*) FFT_IN
      parameter (FFT_IN='fft.IN')
      character*(*) FFT_OUT
      parameter (FFT_OUT='seq_fft.OUT')

c     external readproc, writeproc
c     integer procnum, procxyz(3), datasize(3)
      integer istarts, istartms, istops, istopms, itimediff

c
c     arguments for cfft99:
c         cfft99(a,work,trigs,ifax,inc,jump,n,lot,isign)
c
c         a contains input/output of FFT (a set of vectors)
c         work is a work array
c         trigs, ifax contain constants for cfft99 (generated by
c             subroutine cftfax)
c         inc is stride between vector elements
c         jump is between successive vectors
c         n is size of each vector
c         lot is how many vectors
c         isign indicates forward/inverse transform
c
      integer ifaxnx(13), ifaxny(13)
      real trigsnx(2*nx_dg1), trigsny(2*ny_dg1)
      integer inc, jump, n, lot, m

c     local section of distributed grid -- type is really complex,
c         declared double precision for compatibility with archetype
c     double precision arr(lclsize_dg1)
c     complex work(lclsize_dg1)
      double precision arr(nx_dg1*ny_dg1)
      complex work(nx_dg1*ny_dg1)

      call mytime(istarts, istartms)

c     call local_pos(procxyz,procnum,-1)
c     if (procnum.eq.IOPROC) then
c         print*, 'procs = ', procs
          print*, 'nx_dg1 = ', nx_dg1
          print*, 'ny_dg1 = ', ny_dg1
          print*, 'nrepeats = ', nrepeats
c     endif

      do m = 1, nrepeats
c
c     set up grid and read input data; open output file
c
c     call wrapper(id_dg1,id_row,DOUBLEPRECISION_T,arr,SETMESH)
```

```
c     if (procnum.eq.IOPROC) then
          open(unit=IUNIT, file=FFT_IN, form='unformatted')
c     endif
c     call read_mesh(readproc, id_dg1, IUNIT, arr)
      call readproc(0, IUNIT, 1,1,1, 1,nx_dg1,1,ny_dg1,1,1,
     -     nx_dg1,ny_dg1,1, arr)
c     if (procnum.eq.IOPROC) then
          close(IUNIT)
c     endif

c
c     initialize for fft
c
      call cftfax(nx_dg1, ifaxnx, trigsnx)
      call cftfax(ny_dg1, ifaxny, trigsny)

c
c     do fft by rows
c
c     call local_pos(procxyz,procnum,id_dg1)
c     call data_widths(procxyz,.false.,datasize,id_dg1)
c     inc = datasize(1)
      inc = nx_dg1
      jump = 1
      n = ny_dg1
c     lot = datasize(1)
      lot = nx_dg1
      call cfft99(arr, work, trigsny, ifaxny, inc, jump, n, lot, -1)

c
c     redistribute data
c
c     call wrapper(id_dg1,id_col,DOUBLEPRECISION_T,arr,REDISTRIBUTEDATA)

c-----benchmark fft by columns
c
c     do fft by columns
c
c     call local_pos(procxyz,procnum,id_dg1)
c     call data_widths(procxyz,.false.,datasize,id_dg1)
      inc = 1
      jump = nx_dg1
      n = nx_dg1
c     lot = datasize(2)
      lot = ny_dg1
      call cfft99(arr, work, trigsnx, ifaxnx, inc, jump, n, lot, -1)

c
c     redistribute data
c
c     call wrapper(id_dg1,id_row,DOUBLEPRECISION_T,arr,REDISTRIBUTEDATA)

c
c     write output data
c
c     if (procnum.eq.IOPROC) then
          open(unit=OUNIT, file=FFT_OUT, form='unformatted')
c     endif
c     call write_mesh(writeproc, id_dg1, OUNIT, arr)
      call writeproc(0, OUNIT, 1,1,1, 1,nx_dg1,1,ny_dg1,1,1,
     -     nx_dg1,ny_dg1,1, arr)
c     if (procnum.eq.IOPROC) then
          close(OUNIT)
c     endif
```

```
c     end of 'do m = 1, nrepeats' loop
      enddo

      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'sequential time:  ', itimediff

c     return
      end

c-----------------------------------------------------------------------
c
c     subroutine for reading input data (one local section at
c         a time)
c
c-----------------------------------------------------------------------

      subroutine readproc(ignum, iunit, ipx, ipy, ipz, ixlo, ixhi,
     -     iylo, iyhi, izlo, izhi, nxlcl, nylcl, nzlcl, rarr)
      implicit none

      integer ignum, iunit, x, y,z
      integer ipx, ipy, ipz
      integer ixlo, ixhi, iylo, iyhi, izlo, izhi
      integer nxlcl, nylcl, nzlcl

      complex rarr(ixlo:ixhi, iylo:iyhi, izlo:izhi)

      do x=1,nxlcl
         do y=1,nylcl
            do z=1,nzlcl
               read(iunit, end=10) rarr(x, y, z)
            enddo
         enddo
      enddo
 10   return
      end

c-----------------------------------------------------------------------
c
c     subroutine for writing input data (one local section at
c         a time)
c
c-----------------------------------------------------------------------

      subroutine writeproc(ignum, ounit, ipx, ipy, ipz, ixlo, ixhi,
     -     iylo, iyhi, izlo, izhi, nxlcl, nylcl, nzlcl, warr)
      implicit none

      integer ignum, ounit
      integer ipx, ipy, ipz, x, y, z
      integer ixlo, ixhi, iylo, iyhi, izlo, izhi
      integer nxlcl, nylcl, nzlcl

      complex warr(ixlo:ixhi, iylo:iyhi, izlo:izhi)

      do x=1,nxlcl
         do y=1,nylcl
            do z=1,nzlcl
               write(ounit) warr(x, y, z)
            enddo
         enddo
      enddo
      return
      end
```

```
c-----------------------------------------------------------------------
c
c     automatically-generated wrapper program to pack arrays
c         and call set_mesh or redistribute_data
c
c-----------------------------------------------------------------------

c     include 'seq_fft_wrap.h'

c-----------------------------------------------------------------------
```

Parallel Application Program.

```
c-----------------------------------------------------------------------
c
c     example of mesh/spectral archetype
c
c     2D FFT
c
c     make-time parameters:
c         NX, NY = dimensions of grid
c         NPROCS = number of processes
c
c-----------------------------------------------------------------------

c-----------------------------------------------------------------------
c
c     main program
c
c-----------------------------------------------------------------------

      program main
      implicit none
      include 'arch_uparms.h'
      include 'arch_parms.h'
      include 'par_fft_header.h'

      processors (MAXPROCS)
      call spawn(procs)
      end

c-----------------------------------------------------------------------
c
c     process-main program
c
c-----------------------------------------------------------------------

      subroutine procmain()
      implicit none
      include 'arch_uparms.h'
      include 'arch_parms.h'
      include 'par_fft_header.h'

      integer nrepeats
      parameter (nrepeats=10)

      integer IUNIT,OUNIT
      parameter (IUNIT=11,OUNIT=12)
      character*(*) FFT_IN
      parameter (FFT_IN='fft.IN')
      character*(*) FFT_OUT1,FFT_OUT2
      parameter (FFT_OUT1='par_fft_',FFT_OUT2='.OUT')
```

```
      external readproc, writeproc
      integer procnum, procxyz(3), datasize(3)
      integer istarts, istartms, istops, istopms, itimediff

c
c     arguments for cfft99:
c         cfft99(a,work,trigs,ifax,inc,jump,n,lot,isign)
c
c         a contains input/output of FFT (a set of vectors)
c         work is a work array
c         trigs, ifax contain constants for cfft99 (generated by
c             subroutine cftfax)
c         inc is stride between vector elements
c         jump is between successive vectors
c         n is size of each vector
c         lot is how many vectors
c         isign indicates forward/inverse transform
c
      integer ifaxnx(13), ifaxny(13)
      real trigsnx(2*nx_dg1), trigsny(2*ny_dg1)
      integer inc, jump, n, lot, m

c     local section of distributed grid -- type is really complex,
c         declared double precision for compatibility with archetype
      double precision arr(lclsize_dg1)
      complex work(lclsize_dg1)

      character*80 fft_out
      character*4 cbuff1
      integer cblen1

      call mytime(istarts, istartms)

      call local_pos(procxyz,procnum,-1)
      if (procnum.eq.IOPROC) then
          print*, 'procs = ', procs
          print*, 'nx_dg1 = ', nx_dg1
          print*, 'ny_dg1 = ', ny_dg1
          print*, 'nrepeats = ', nrepeats
      endif

      do m = 1, nrepeats
c
c     set up grid and read input data
c
      call wrapper(id_dg1,id_row,DOUBLEPRECISION_T,arr,SETMESH)
      if (procnum.eq.IOPROC) then
          open(unit=IUNIT, file=FFT_IN, form='unformatted')
      endif
      call read_mesh(readproc, id_dg1, IUNIT, arr)
      if (procnum.eq.IOPROC) then
          close(IUNIT)
      endif

c
c     initialize for fft
c
      call cftfax(nx_dg1, ifaxnx, trigsnx)
      call cftfax(ny_dg1, ifaxny, trigsny)

c
c     do fft by rows
c
      call local_pos(procxyz,procnum,id_dg1)
      call data_widths(procxyz,.false.,datasize,id_dg1)
```

```
      inc = datasize(1)
      jump = 1
      n = ny_dg1
      lot = datasize(1)
      call cfft99(arr, work, trigsny, ifaxny, inc, jump, n, lot, -1)

c
c     redistribute data
c
      call wrapper(id_dg1,id_col,DOUBLEPRECISION_T,arr,REDISTRIBUTEDATA)

c
c     do fft by columns
c
      call local_pos(procxyz,procnum,id_dg1)
      call data_widths(procxyz,.false.,datasize,id_dg1)
      inc = 1
      jump = nx_dg1
      n = nx_dg1
      lot = datasize(2)
      call cfft99(arr, work, trigsnx, ifaxnx, inc, jump, n, lot, -1)

c
c     redistribute data
c
      call wrapper(id_dg1,id_row,DOUBLEPRECISION_T,arr,REDISTRIBUTEDATA)

c
c     write output data
c
      if (procnum.eq.IOPROC) then
c         build output filename
          if (procs .le. 9) then
              write (cbuff1, '(3i1.1)') procs
              cblen1=1
          else
              write (cbuff1, '(3i2.2)') procs
              cblen1=2
          endif
          fft_out = FFT_OUT1 // cbuff1(1:cblen1) // FFT_OUT2
          open(unit=OUNIT, file=fft_out, form='unformatted')
      endif
      call write_mesh(writeproc, id_dg1, OUNIT, arr)
      if (procnum.eq.IOPROC) then
          close(OUNIT)
      endif

c     end of 'do m = 1, nrepeats' loop
      enddo

      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'process ', procnum, ':  ', itimediff

      return
      end

c-----------------------------------------------------------------------
c
c     subroutine for reading input data (one local section at
c         a time)
c
c-----------------------------------------------------------------------

      subroutine readproc(ignum, iunit, ipx, ipy, ipz, ixlo, ixhi,
```

```
     -     iylo, iyhi, izlo, izhi, nxlcl, nylcl, nzlcl, rarr)
      implicit none

      integer ignum, iunit, x, y,z
      integer ipx, ipy, ipz
      integer ixlo, ixhi, iylo, iyhi, izlo, izhi
      integer nxlcl, nylcl, nzlcl

      complex rarr(ixlo:ixhi, iylo:iyhi, izlo:izhi)

      do x=1,nxlcl
         do y=1,nylcl
            do z=1,nzlcl
               read(iunit, end=10) rarr(x, y, z)
            enddo
         enddo
      enddo
 10   return
      end

c--------------------------------------------------------------------------
c
c     subroutine for writing input data (one local section at
c         a time)
c
c--------------------------------------------------------------------------

      subroutine writeproc(ignum, ounit, ipx, ipy, ipz, ixlo, ixhi,
     -     iylo, iyhi, izlo, izhi, nxlcl, nylcl, nzlcl, warr)
      implicit none

      integer ignum, ounit
      integer ipx, ipy, ipz, x, y, z
      integer ixlo, ixhi, iylo, iyhi, izlo, izhi
      integer nxlcl, nylcl, nzlcl

      complex warr(ixlo:ixhi, iylo:iyhi, izlo:izhi)

      do x=1,nxlcl
         do y=1,nylcl
            do z=1,nzlcl
               write(ounit) warr(x, y, z)
            enddo
         enddo
      enddo
      return
      end

c--------------------------------------------------------------------------
c
c     automatically-generated wrapper program to pack arrays
c         and call set_mesh or redistribute_data
c
c--------------------------------------------------------------------------

      include 'par_fft_wrap.h'

c--------------------------------------------------------------------------
```

Computational Benchmark Program.

```
c--------------------------------------------------------------------------
c
c     example of mesh/spectral archetype
```

```
c
c     2D FFT
c
c     benchmark version
c
c     make-time parameters:
c         NX, NY = dimensions of grid
c
c     may need to adjust loops bounded by klim
c
c-----------------------------------------------------------------------

c-----------------------------------------------------------------------
c
c     main program
c
c-----------------------------------------------------------------------

      program main
      implicit none
c     include 'arch_uparms.h'
c     include 'arch_parms.h'
c     include 'bench_fft_header.h'

c     processors (MAXPROCS)
c     call spawn(procs)
c     end

c-----------------------------------------------------------------------
c
c     process-main program
c
c-----------------------------------------------------------------------

c     subroutine procmain()
c     implicit none
c     include 'arch_uparms.h'
c     include 'arch_parms.h'
      include 'bench_fft_header.h'

c     integer nrepeats
c     parameter (nrepeats=10)

      integer IUNIT,OUNIT
      parameter (IUNIT=11,OUNIT=12)
      character*(*) FFT_IN
      parameter (FFT_IN='fft.IN')
      character*(*) FFT_OUT1,FFT_OUT2
      parameter (FFT_OUT1='bench_fft',FFT_OUT2='.OUT')

c     external readproc, writeproc
c     integer procnum, procxyz(3), datasize(3)
      integer istarts, istartms, istops, istopms, itimediff, k, klim

c
c     arguments for cfft99:
c         cfft99(a,work,trigs,ifax,inc,jump,n,lot,isign)
c
c         a contains input/output of FFT (a set of vectors)
c         work is a work array
c         trigs, ifax contain constants for cfft99 (generated by
c             subroutine cftfax)
c         inc is stride between vector elements
c         jump is between successive vectors
c         n is size of each vector
```

```
c         lot is how many vectors
c         isign indicates forward/inverse transform
c
      integer ifaxnx(13), ifaxny(13)
      real trigsnx(2*nx_dg1), trigsny(2*ny_dg1)
      integer inc, jump, n, lot

c     local section of distributed grid -- type is really complex,
c         declared double precision for compatibility with archetype
c     double precision arr(lclsize_dg1)
c     complex work(lclsize_dg1)
      double precision arr(nx_dg1*ny_dg1)
      complex work(nx_dg1*ny_dg1)

      character*80 fft_out
      character*4 cbuff1
      integer cblen1

c     call local_pos(procxyz,procnum,-1)
c     if (procnum.eq.IOPROC) then
c         print*, 'procs = ', procs
          print*, 'nx_dg1 = ', nx_dg1
          print*, 'ny_dg1 = ', ny_dg1
c         print*, 'nrepeats = ', nrepeats
c     endif

c     do m = 1, nrepeats
c
c-----benchmark initializations
c
c     set up grid and read input data
c
      call mytime(istarts, istartms)
      klim = 10
      do k=1,klim
c         if (procnum.eq.IOPROC) then
              open(unit=IUNIT, file=FFT_IN, form='unformatted')
c         endif
c         call read_mesh(readproc, id_dg1, IUNIT, arr)
          call readproc(0, IUNIT, 1,1,1, 1,nx_dg1,1,ny_dg1,1,1,
     -         nx_dg1,ny_dg1,1, arr)
c         if (procnum.eq.IOPROC) then
              close(IUNIT)
c         endif
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'reading input file: ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

c
c     initialize for fft
c
      call mytime(istarts, istartms)
      klim = 1000
      do k=1,klim
          call cftfax(nx_dg1, ifaxnx, trigsnx)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'initialization x: ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

      call mytime(istarts, istartms)
      klim = 1000
```

```
      do k=1,klim
          call cftfax(ny_dg1, ifaxny, trigsny)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'initialization y: ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

c-----benchmark fft by rows
c
c     do fft by rows
c
      call mytime(istarts, istartms)
      klim = 50
      do k=1,klim
c         call local_pos(procxyz,procnum,id_dg1)
c         call data_widths(procxyz,.false.,datasize,id_dg1)
c         inc = datasize(1)
          inc = nx_dg1
          jump = 1
          n = ny_dg1
c         lot = datasize(1)
          lot = nx_dg1
          call cfft99(arr, work, trigsny, ifaxny, inc, jump, n, lot, -1)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'fft by rows: ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

c
c     redistribute data
c
c     call wrapper(id_dg1,id_col,DOUBLEPRECISION_T,arr,REDISTRIBUTEDATA)

c-----benchmark fft by columns
c
c     do fft by columns
c
      call mytime(istarts, istartms)
      klim = 50
      do k=1,klim
c         call local_pos(procxyz,procnum,id_dg1)
c         call data_widths(procxyz,.false.,datasize,id_dg1)
          inc = 1
          jump = nx_dg1
          n = nx_dg1
c         lot = datasize(2)
          lot = ny_dg1
          call cfft99(arr, work, trigsnx, ifaxnx, inc, jump, n, lot, -1)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'fft by column: ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

c
c     redistribute data
c
c     call wrapper(id_dg1,id_row,DOUBLEPRECISION_T,arr,REDISTRIBUTEDATA)

c-----benchmark output
c
c     write output data
c
```

```
      call mytime(istarts, istartms)
      klim = 10
      do k=1,klim
c         if (procnum.eq.IOPROC) then
c             build output filename (dummy version)
              write (cbuff1, '(3i1.1)') 0
              cblen1=1
              fft_out = FFT_OUT1 // FFT_OUT2
              open(unit=OUNIT, file=fft_out, form='unformatted')
c         endif
c         call write_mesh(writeproc, id_dg1, OUNIT, arr)
          call writeproc(0, OUNIT, 1,1,1, 1,nx_dg1,1,ny_dg1,1,1,
     -         nx_dg1,ny_dg1,1, arr)
c         if (procnum.eq.IOPROC) then
              close(OUNIT)
c         endif
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'writing output file: ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

c     end of 'do m = 1, nrepeats' loop
c     enddo

c     return
      end

c-----------------------------------------------------------------------
c
c     subroutine for reading input data (one local section at
c         a time)
c
c-----------------------------------------------------------------------

      subroutine readproc(ignum, iunit, ipx, ipy, ipz, ixlo, ixhi,
     -     iylo, iyhi, izlo, izhi, nxlcl, nylcl, nzlcl, rarr)
      implicit none

      integer ignum, iunit, x, y,z
      integer ipx, ipy, ipz
      integer ixlo, ixhi, iylo, iyhi, izlo, izhi
      integer nxlcl, nylcl, nzlcl

      complex rarr(ixlo:ixhi, iylo:iyhi, izlo:izhi)

      do x=1,nxlcl
         do y=1,nylcl
            do z=1,nzlcl
               read(iunit, end=10) rarr(x, y, z)
            enddo
         enddo
      enddo
 10   return
      end

c-----------------------------------------------------------------------
c
c     subroutine for writing input data (one local section at
c         a time)
c
c-----------------------------------------------------------------------

      subroutine writeproc(ignum, ounit, ipx, ipy, ipz, ixlo, ixhi,
     -     iylo, iyhi, izlo, izhi, nxlcl, nylcl, nzlcl, warr)
```

```
      implicit none

      integer ignum, ounit
      integer ipx, ipy, ipz, x, y, z
      integer ixlo, ixhi, iylo, iyhi, izlo, izhi
      integer nxlcl, nylcl, nzlcl

      complex warr(ixlo:ixhi, iylo:iyhi, izlo:izhi)

      do x=1,nxlcl
         do y=1,nylcl
            do z=1,nzlcl
               write(ounit) warr(x, y, z)
            enddo
         enddo
      enddo
      return
      end

c--------------------------------------------------------------------------
c
c     automatically-generated wrapper program to pack arrays
c         and call set_mesh or redistribute_data
c
c--------------------------------------------------------------------------

c     include 'bench_fft_wrap.h'

c--------------------------------------------------------------------------
```

Communication Benchmark Program.

```
C--------------------------------------------------------------------------
C
C       program bench_mesh_spectral
C       written by adam rifkin, adam@cs.caltech.edu, 1996
C       modified by berna massingill
C
C       calculates times for the archetype library routines
C
C       make-time parameters:
C           NX, NY = dimensions of grid
C           NPROCS = number of processes
C           NXPROCS, NYPROCS = dimensions of process grid
C
C       may also need to adjust loops bounded by klim
C
C--------------------------------------------------------------------------

      program main
      implicit none
      include 'arch_uparms.h'
      include 'arch_parms.h'
      include 'bench_mesh_spectral_header.h'

      processors (MAXPROCS)
      call spawn(procs)
      end

C--------------------------------------------------------------------------

      subroutine procmain()
      implicit none
      include 'arch_uparms.h'
```

```
      include 'arch_parms.h'
      include 'bench_mesh_spectral_header.h'

c     number of times to do communication operations
      integer NTIMES
      parameter (NTIMES=10)
c     sizes of data for broadcast operation
      integer NIC, NRC, NDPC
      parameter (NIC=2)
      parameter (NRC=2)
      parameter (NDPC=2)

      integer IUNIT,OUNIT
      parameter (IUNIT=11,OUNIT=12)

      integer procnum, procxyz(3), datasize(3)
      integer low(3), high(3)
      integer glbstart(3), glbend(3)
      integer lclstart(3), lclend(3)
      integer locals(3), globals(3)
      integer k, itemp1, itemp2, itemp3
      logical iempty(3)
      integer iconst(NIC)
      integer rconst(NRC)
      integer dconst(NDPC)
      double precision difflocal, diffmax
      integer locmaxin, locmaxout
      double precision data(lclsize_dg1)
      integer istarts, istartms, istops, istopms, itimediff, klim, k
      external readproc, writeproc

      call local_pos(procxyz,procnum,-1)
      if (procnum.eq.IOPROC) then
          print*, 'procs = ', procs
          print*, 'data sizes:'
          print*, 'nx_dg1 = ', nx_dg1
          print*, 'ny_dg1 = ', ny_dg1
          print*, 'broadcast sizes:'
          print*, 'NIC = ', NIC
          print*, 'NRC = ', NRC
          print*, 'NDPC = ', NDPC
      endif

C---- benchmark wrapper SETMESH

      call mytime(istarts, istartms)
      klim = 100000
      do k=1,klim
        call wrapper(id_dg1,id_blk,DOUBLEPRECISION_T,data,SETMESH)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'SETMESH ', procnum, ':  ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

C---- benchmark local_pos

      call mytime(istarts, istartms)
      klim = 100000
      do k=1,klim
        call local_pos(procxyz,procnum,id_dg1)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'local_pos ', procnum, ':  ', klim, itimediff,
```

```
     $    dble(itimediff)/dble(klim)

C---- benchmark data_widths

      call mytime(istarts, istartms)
      klim = 100000
      do k=1,klim
        call data_widths(procxyz,.false.,datasize,id_dg1)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'data_widths ', procnum, ':  ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

C---- benchmark wrapper REDISTRIBUTEDATA (one to blk)

      call mytime(istarts, istartms)
      klim = NTIMES
      do k=1,klim
        call wrapper(id_dg1,id_one,DOUBLEPRECISION_T,data,SETMESH)
        call wrapper(id_dg1,id_blk,DOUBLEPRECISION_T,data,
     $      REDISTRIBUTEDATA)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'SETMESH/REDISTRIBUTEDATA (one to blk) ',
     $    procnum, ':  ', klim, itimediff, dble(itimediff)/dble(klim)

C---- benchmark wrapper REDISTRIBUTEDATA (blk to one)

      call mytime(istarts, istartms)
      klim = NTIMES
      do k=1,klim
        call wrapper(id_dg1,id_blk,DOUBLEPRECISION_T,data,SETMESH)
        call wrapper(id_dg1,id_one,DOUBLEPRECISION_T,data,
     $      REDISTRIBUTEDATA)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'SETMESH/REDISTRIBUTEDATA (blk to one) ',
     $    procnum, ':  ', klim, itimediff, dble(itimediff)/dble(klim)

C---- benchmark wrapper REDISTRIBUTEDATA (row to col)

      call mytime(istarts, istartms)
      klim = NTIMES
      do k=1,klim
        call wrapper(id_dg1,id_row,DOUBLEPRECISION_T,data,SETMESH)
        call wrapper(id_dg1,id_col,DOUBLEPRECISION_T,data,
     $      REDISTRIBUTEDATA)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'SETMESH/REDISTRIBUTEDATA (row to col) ',
     $    procnum, ':  ', klim, itimediff, dble(itimediff)/dble(klim)

C---- benchmark wrapper REDISTRIBUTEDATA (col to row)

      call mytime(istarts, istartms)
      klim = NTIMES
      do k=1,klim
        call wrapper(id_dg1,id_col,DOUBLEPRECISION_T,data,SETMESH)
        call wrapper(id_dg1,id_row,DOUBLEPRECISION_T,data,
     $      REDISTRIBUTEDATA)
      enddo
```

```
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'SETMESH/REDISTRIBUTEDATA (col to row) ',
     $    procnum, ':  ', klim, itimediff, dble(itimediff)/dble(klim)

C---- benchmark broadcast

      call mytime(istarts, istartms)
      klim = NTIMES
      do k=1,klim
        call broadcast(NIC,NRC,NDPC,iconst,rconst,dconst,-1)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'broadcast ', procnum, ':  ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

C---- benchmark data_bounds

      call wrapper(id_dg1,id_blk,DOUBLEPRECISION_T,data,SETMESH)
      call local_pos(procxyz,procnum,id_dg1)
      call mytime(istarts, istartms)
      klim = 100000
      do k=1,klim
        call data_bounds(procxyz, low, high, id_dg1)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'data_bounds ', procnum, ':  ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

C---- benchmark pack3

      call mytime(istarts, istartms)
      klim = 1000000
      do k=1,klim
        call pack3(2,2,1,glbstart)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'pack3 ', procnum, ':  ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

C------ benchmark unpack3

      call mytime(istarts, istartms)
      klim = 1000000
      do k=1,klim
        call unpack3(itemp1,itemp2,itemp3,glbstart)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'unpack3 ', procnum, ':  ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

C---- benchmark intersect

      call wrapper(id_dg1,id_blk,DOUBLEPRECISION_T,data,SETMESH)
      call local_pos(procxyz,procnum,id_dg1)
      call pack3(2,2,1,glbstart)
      call pack3(nx_dg1-1,ny_dg1-1,1,glbend)
      call mytime(istarts, istartms)
      klim = 1000000
      do k=1,klim
          call intersect(procxyz,glbstart,glbend,lclstart,lclend,
```

```
     $          iempty,id_dg1)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'intersect ', procnum, ':  ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

C---- benchmark local_to_global

      call wrapper(id_dg1,id_blk,DOUBLEPRECISION_T,data,SETMESH)
      call local_pos(procxyz,procnum,id_dg1)
      call pack3(1,1,1,locals)
      call mytime(istarts, istartms)
      klim = 1000000
      do k=1,klim
          call local_to_global(procxyz,locals,globals,id_dg1)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'local_to_global ', procnum, ':  ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

C---- benchmark boundary_exchange

      call mytime(istarts, istartms)
      klim = NTIMES
      do k=1,klim
        call boundary_exchange(data,id_dg1)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'boundary_exchange (no wrap) ', procnum, ':  ',
     $    klim, itimediff, dble(itimediff)/dble(klim)

C---- benchmark global_max_dp

      call mytime(istarts, istartms)
      klim = NTIMES
      do k=1,klim
        call global_max_dp(difflocal,locmaxin,diffmax,locmaxout,id_dg1)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'global_max_dp ', procnum, ':  ', klim, itimediff,
     $    dble(itimediff)/dble(klim)


C---- benchmark read_mesh (no actual I/O -- benchmarked elsewhere)

      call mytime(istarts, istartms)
      klim = NTIMES
      do k=1,klim
        call wrapper(id_dg1,id_row,DOUBLEPRECISION_T,data,SETMESH)
c       if (procnum.eq.IOPROC) then
c           open(unit=IUNIT, file=fft_in, form='unformatted')
c       endif
        call read_mesh(readproc, id_dg1, IUNIT, data)
c       if (procnum.eq.IOPROC) then
c           close(unit=IUNIT)
c       endif
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'read_mesh (dummy) ', procnum, ':  ', klim, itimediff,
     $    dble(itimediff)/dble(klim)
```

```
C---- benchmark write_mesh (no actual I/O -- benchmarked elsewhere)

      call mytime(istarts, istartms)
      klim = NTIMES
      do k=1,klim
        call wrapper(id_dg1,id_row,DOUBLEPRECISION_T,data,SETMESH)
c       if (procnum.eq.IOPROC) then
c           open(unit=OUNIT, file=fft_out, form='unformatted')
c       endif
        call write_mesh(writeproc, id_dg1, OUNIT, data)
c       if (procnum.eq.IOPROC) then
c           close(unit=OUNIT)
c       endif
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'write_mesh (dummy) ', procnum, ':  ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

      end

c-----------------------------------------------------------------------
c
c
c     dummy subroutine for reading input data (one local section at
c         a time)
c
c-----------------------------------------------------------------------

      subroutine readproc(ignum, iunit, ipx, ipy, ipz, ixlo, ixhi,
     -     iylo, iyhi, izlo, izhi, nxlcl, nylcl, nzlcl, rarr)
      implicit none

      integer ignum, iunit, x, y,z
      integer ipx, ipy, ipz
      integer ixlo, ixhi, iylo, iyhi, izlo, izhi
      integer nxlcl, nylcl, nzlcl

      complex rarr(ixlo:ixhi, iylo:iyhi, izlo:izhi)

c     do x=1,nxlcl
c        do y=1,nylcl
c           do z=1,nzlcl
c              read(iunit, end=10) rarr(x, y, z)
c           enddo
c        enddo
c     enddo
10    return
      end

c-----------------------------------------------------------------------
c
c     dummy subroutine for writing input data (one local section at
c         a time)
c
c-----------------------------------------------------------------------

      subroutine writeproc(ignum, ounit, ipx, ipy, ipz, ixlo, ixhi,
     -     iylo, iyhi, izlo, izhi, nxlcl, nylcl, nzlcl, warr)
      implicit none

      integer ignum, ounit
      integer ipx, ipy, ipz, x, y, z
      integer ixlo, ixhi, iylo, iyhi, izlo, izhi
```

```
      integer nxlcl, nylcl, nzlcl

      complex warr(ixlo:ixhi, iylo:iyhi, izlo:izhi)

c     do x=1,nxlcl
c        do y=1,nylcl
c           do z=1,nzlcl
c              write(ounit) warr(x, y, z)
c           enddo
c        enddo
c     enddo
      return
      end


C-----------------------------------------------------------------------

      include 'bench_mesh_spectral_wrap.h'

C-----------------------------------------------------------------------
```

B.2 Poisson Solver

Sequential Application Program.

```
c-----------------------------------------------------------------------
c
c     example of mesh/spectral archetype
c
c     Poisson solver
c
c     make-time parameters:
c         NX, NY = dimensions of grid
c
c-----------------------------------------------------------------------

c-----------------------------------------------------------------------
c
c     main program
c
c-----------------------------------------------------------------------

      program main
      implicit none
c     include 'arch_uparms.h'
c     include 'arch_parms.h'
c     include 'seq_poisson_header.h'

c     call procmain()
c     end

c-----------------------------------------------------------------------
c
c     process-main program
c
c-----------------------------------------------------------------------

c     subroutine procmain()
c     implicit none
c     include 'arch_uparms.h'
c     include 'arch_parms.h'
      include 'seq_poisson_header.h'
```

```
      integer IUNIT,OUNIT
      parameter (IUNIT=11,OUNIT=12)
      character*(*) P_IN
      parameter (P_IN='poisson.IN')
      character*(*) P_OUT
      parameter (P_OUT='seq_poisson.OUT')

c     integer procnum, idummy(3)
c     integer procnum_one, procxyz_one(3)
c     integer procnum_blk, procxyz_blk(3)
c     integer low(3), high(3)
c     double precision uk(lclsize_dg1)
c     double precision ukp1(lclsize_dg1)
      double precision uk(nx_dg1*ny_dg1)
      double precision ukp1(nx_dg1*ny_dg1)
      double precision F, G
      external F, G
      double precision diffmax
      integer nsteps
      integer istarts, istartms, istops, istopms, itimediff

      call mytime(istarts, istartms)

c
c     read and broadcast constants
c
c     call local_pos(idummy,procnum,-1)
c     if (procnum .eq. IOPROC) then
c         print*, 'procs = ', procs
          print*, 'nx_dg1 = ', nx_dg1
          print*, 'ny_dg1 = ', ny_dg1
c         print*, 'nprocx_blk = ', nprocx_blk
c         print*, 'nprocy_blk = ', nprocy_blk
          open(unit=IUNIT, file=P_IN, access='sequential',
     $         status='old', form='formatted')
          read(IUNIT, *) H
          read(IUNIT, *) TOL
          read(IUNIT, *) NCHECK
          read(IUNIT, *) MAXSTEPS
          close(unit=IUNIT)
c     endif
c     call broadcast(NIC,NRC,NDPC,iconst,rconst,dconst,-1)

c
c     set up grid (undistributed)
c
c     call wrapper(id_dg1,id_one,DOUBLEPRECISION_T,uk,SETMESH)
c     call local_pos(procxyz_one,procnum_one,id_dg1)

c
c     initialize undistributed grid
c
c     if (procnum_one .eq. 1) then
          call initgrid(nx_dg1, ny_dg1, uk)
c     endif

c
c     distribute
c
c     call wrapper(id_dg1,id_blk,DOUBLEPRECISION_T,uk,REDISTRIBUTEDATA)
c     call local_pos(procxyz_blk,procnum_blk,id_dg1)

c
c     perform computation
c
```

```
c     call data_bounds(procxyz_blk, low, high, id_dg1)
c     call computegrid(low(1),high(1),low(2),high(2),uk,ukp1,
c    -    diffmax,nsteps)
      call computegrid(1,nx_dg1,1,ny_dg1,uk,ukp1,diffmax,nsteps)

c
c     redistribute to collect all data in one process again
c
c     call wrapper(id_dg1,id_one,DOUBLEPRECISION_T,uk,REDISTRIBUTEDATA)

c
c     print results
c
c     if (procnum_one .eq. 1) then
          open(unit=OUNIT, file=P_OUT, access='sequential',
     $         status='unknown', form='formatted')
          write (OUNIT,*) 'NX, NY = ', nx_dg1, ny_dg1
          write (OUNIT,*) 'H = ', H
          write (OUNIT,*) 'tolerance = ', TOL
          call Fprint(OUNIT)
          call Gprint(OUNIT)

          if (diffmax .le. TOL) then
              write (OUNIT,*) 'convergence occurred in ',
     -            nsteps, ' steps'
              print*, 'steps = ', nsteps
          else
              write (OUNIT,*) 'no convergence in ', MAXSTEPS,
     -            ' steps; ', 'max. difference ', diffmax
              print*, 'steps = ', MAXSTEPS
          endif
          call printgrid(nx_dg1, ny_dg1, uk, OUNIT)
          close(unit=OUNIT)
c     endif

      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'sequential time:  ', itimediff

c     return
      end

c-----------------------------------------------------------------------
c
c     initialize grid
c
c-----------------------------------------------------------------------

      subroutine initgrid(nx, ny, uk)
      implicit none
c     include 'arch_uparms.h'
c     include 'arch_parms.h'
      include 'seq_poisson_header.h'

      integer nx, ny
      double precision uk(nx, ny)

      double precision F, G
      external F, G
      integer i, j

c
c     interior points
c
      do i = 2, nx-1
```

```
      do j = 2, ny-1
          uk(i,j) = F(i,j,nx,ny,H)
      enddo
      enddo
c
c     boundary points
c
      do j = 1, ny
          uk(1,j) = G(1,j,nx,ny,H)
          uk(nx,j) = G(nx,j,nx,ny,H)
      enddo
      do i = 2, nx-1
          uk(i,1) = G(i,1,nx,ny,H)
          uk(i,ny) = G(i,ny,nx,ny,H)
      enddo
      end

c---------------------------------------------------------------------
c
c     print grid data
c
c---------------------------------------------------------------------

      subroutine printgrid(nx, ny, uk, ounit)
      implicit none
c     include 'arch_uparms.h'
c     include 'arch_parms.h'
      include 'seq_poisson_header.h'

      integer nx, ny
      double precision uk(nx, ny)
      integer ounit

      integer i, j

c     do i = 1, nx
c         if (nx .gt. 10) write (ounit,*) ' '
c         write (ounit,9999) (uk(i,j), j = 1, ny)
c     enddo
9999  format(10F8.4)
      do i = 1, nx, nx/5
          write (ounit,9999) (uk(i,j), j = 1, ny, ny/5), uk(i,ny)
      enddo
      write (ounit,9999) (uk(nx,j), j = 1, ny, ny/5), uk(nx,ny)

      end

c---------------------------------------------------------------------
c
c     do grid computation
c
c---------------------------------------------------------------------

      subroutine computegrid(ixlo,ixhi,iylo,iyhi,uk,ukp1,diffmax,nsteps)

      implicit none
c     include 'arch_uparms.h'
c     include 'arch_parms.h'
      include 'seq_poisson_header.h'

      integer ixlo,ixhi,iylo,iyhi
      double precision uk(ixlo:ixhi,iylo:iyhi)
      double precision ukp1(ixlo:ixhi,iylo:iyhi)
      double precision diffmax
      integer nsteps
```

```
      double precision F, G
      external F, G
      double precision diff, difflocal
c     integer glbstart(3), glbend(3)
c     integer lclstart(3), lclend(3)
c     integer ipxyz(3), iproc
      integer istart, iend, jstart, jend, kstart, kend
c     integer locmaxin(3), locmaxout(3)
c     logical iempty(3)
      integer i, j, k
c     integer glblcl(3)
c     integer istartg, jstartg, kstartg
c     integer igoffset, jgoffset

c     compute loop bounds
c     call local_pos(ipxyz,iproc,id_dg1)
c     call pack3(2,2,1,glbstart)
c     call pack3(nx_dg1-1,ny_dg1-1,1,glbend)
c     call intersect(ipxyz,glbstart,glbend,lclstart,lclend,iempty,
c    -    id_dg1)
c     call unpack3(istart,jstart,kstart,lclstart)
c     call unpack3(iend,jend,kend,lclend)
c     compute starting global indices (of local section)
c     call local_to_global(ipxyz,lclstart,glblcl,id_dg1)
c     call unpack3(istartg,jstartg,kstartg,glblcl)
c     compute offsets (global index = offset + local index)
c     igoffset = istartg - istart
c     jgoffset = jstartg - jstart

      istart=2
      jstart=2
      kstart=1
      iend=nx_dg1-1
      jend=ny_dg1-1
      kend=1
c     igoffset=0
c     jgoffset=0

c     loop until convergence
      diffmax = TOL + 1.0

      do k = 1,MAXSTEPS

c         refresh ghost boundaries
c         call boundary_exchange(uk,id_dg1)

c         compute new values

          do i = istart, iend
          do j = jstart, jend
c             ukp1(i,j) = 0.25*(H*H*F(igoffset+i,jgoffset+j,
c    -                  nx_dg1,ny_dg1,H)
c    -            + uk(i-1,j) + uk(i,j-1)
c    -            + uk(i+1,j) + uk(i,j+1) )
              ukp1(i,j) = 0.25*(H*H*F(i,j,nx_dg1,ny_dg1,H)
     -            + uk(i-1,j) + uk(i,j-1)
     -            + uk(i+1,j) + uk(i,j+1) )
          enddo
          enddo

c         every NCHECK-th step, recompute convergence test
          if (mod(k,NCHECK) .eq. 0) then
c             difflocal = 0.0
              diffmax = 0.0
```

```
              do i = istart, iend
              do j = jstart, jend
                  diff = abs(ukp1(i,j) - uk(i,j))
c                 if (diff .gt. difflocal) difflocal = diff
                  if (diff .gt. diffmax) diffmax = diff
              enddo
              enddo
c             call global_max_dp(difflocal,locmaxin,diffmax,locmaxout,
c    -            id_dg1)
          endif

c         copy new values to old values
          do i = istart, iend
          do j = jstart, jend
              uk(i,j) = ukp1(i,j)
          enddo
          enddo

c         check for convergence
          nsteps = k
          if (diffmax .le. TOL) go to 1000

      enddo

1000  return
      end

c--------------------------------------------------------------------------
c
c     functions for Poisson equation
c
c--------------------------------------------------------------------------

      double precision function F(i,j,nx,ny,h)
      implicit none
      integer i, j, nx, ny
      double precision h

      F = 0.0
      end

c--------------------------------------------------------------------------

      subroutine Fprint(ounit)
      integer ounit
      implicit none
      write (ounit,*) 'F(i,j) = 0.0'
      end

c--------------------------------------------------------------------------

      double precision function G(i,j,nx,ny,h)
      implicit none
      integer i, j, nx, ny
      double precision h

      G = (i+j)*h
      end

c--------------------------------------------------------------------------

      subroutine Gprint(ounit)
      integer ounit
      implicit none
      write (ounit,*) 'G(i,j) = (i+j)*H'
```

```
      end

c-----------------------------------------------------------------------
c
c     automatically-generated wrapper program to pack arrays
c         and call set_mesh or redistribute_data
c
c-----------------------------------------------------------------------

c     include 'seq_poisson_wrap.h'

c-----------------------------------------------------------------------
```

Parallel Application Program.

```
c-----------------------------------------------------------------------
c
c     example of mesh/spectral archetype
c
c     Poisson solver
c
c     make-time parameters:
c         NX, NY = dimensions of grid
c         NPROCS = number of processes
c         NXPROCS, NYPROCS = dimensions of process grid
c
c-----------------------------------------------------------------------

c-----------------------------------------------------------------------
c
c     main program
c
c-----------------------------------------------------------------------

      program main
      implicit none
      include 'arch_uparms.h'
      include 'arch_parms.h'
      include 'par_poisson_header.h'

      processors (MAXPROCS)
      call spawn(procs)
      end

c-----------------------------------------------------------------------
c
c     process-main program
c
c-----------------------------------------------------------------------

      subroutine procmain()
      implicit none
      include 'arch_uparms.h'
      include 'arch_parms.h'
      include 'par_poisson_header.h'

      integer IUNIT,OUNIT
      parameter (IUNIT=11,OUNIT=12)
      character*(*) P_IN
      parameter (P_IN='poisson.IN')
      character*(*) P_OUT1,P_OUT2
      parameter (P_OUT1='par_poisson_',P_OUT2='.OUT')

      integer procnum, idummy(3)
```

```
      integer procnum_one, procxyz_one(3)
      integer procnum_blk, procxyz_blk(3)
      integer low(3), high(3)
      double precision uk(lclsize_dg1)
      double precision ukp1(lclsize_dg1)
      double precision F, G
      external F, G
      double precision diffmax
      integer nsteps
      integer istarts, istartms, istops, istopms, itimediff

      character*80 p_out
      character*4 cbuff1,cbuff2
      integer cblen1,cblen2

      call mytime(istarts, istartms)
c
c     read and broadcast constants
c
      call local_pos(idummy,procnum,-1)
      if (procnum .eq. IOPROC) then
          open(unit=IUNIT, file=P_IN, access='sequential',
     $         status='old', form='formatted')
          read(IUNIT, *) H
          read(IUNIT, *) TOL
          read(IUNIT, *) NCHECK
          read(IUNIT, *) MAXSTEPS
          close(unit=IUNIT)
          print*, 'procs = ', procs
          print*, 'nx_dg1 = ', nx_dg1
          print*, 'ny_dg1 = ', ny_dg1
          print*, 'nprocx_blk = ', nprocx_blk
          print*, 'nprocy_blk = ', nprocy_blk
      endif
      call broadcast(NIC,NRC,NDPC,iconst,rconst,dconst,-1)

c
c     set up grid (undistributed)
c
      call wrapper(id_dg1,id_one,DOUBLEPRECISION_T,uk,SETMESH)
      call local_pos(procxyz_one,procnum_one,id_dg1)

c
c     initialize undistributed grid
c
      if (procnum_one .eq. 1) then
          call initgrid(nx_dg1, ny_dg1, uk)
      endif

c
c     distribute
c
      call wrapper(id_dg1,id_blk,DOUBLEPRECISION_T,uk,REDISTRIBUTEDATA)
      call local_pos(procxyz_blk,procnum_blk,id_dg1)

c
c
c     perform computation
c
      call data_bounds(procxyz_blk, low, high, id_dg1)
      call computegrid(low(1),high(1),low(2),high(2),uk,ukp1,
     -    diffmax,nsteps)

c
c     redistribute to collect all data in one process again
```

```
c
      call wrapper(id_dg1,id_one,DOUBLEPRECISION_T,uk,REDISTRIBUTEDATA)

c
c     print results
c
      if (procnum_one .eq. 1) then
c         build output filename
          if (nprocx_blk .le. 9) then
              write (cbuff1, '(3i1.1)') nprocx_blk
              cblen1=1
          else
              write (cbuff1, '(3i2.2)') nprocx_blk
              cblen1=2
          endif
          if (nprocy_blk .le. 9) then
              write (cbuff2, '(3i1.1)') nprocy_blk
              cblen2=1
          else
              write (cbuff2, '(3i2.2)') nprocy_blk
              cblen2=2
          endif
          p_out = P_OUT1 // cbuff1(1:cblen1) // '_' // cbuff2(1:cblen2)
     -        // P_OUT2
          open(unit=OUNIT, file=p_out, access='sequential',
     $         status='unknown', form='formatted')
          write (OUNIT,*) 'NX, NY = ', nx_dg1, ny_dg1
          write (OUNIT,*) 'H = ', H
          write (OUNIT,*) 'tolerance = ', TOL
          call Fprint(OUNIT)
          call Gprint(OUNIT)

          if (diffmax .le. TOL) then
              write (OUNIT,*) 'convergence occurred in ',
     -            nsteps, ' steps'
              print*, 'steps = ', nsteps
          else
              write (OUNIT,*) 'no convergence in ', MAXSTEPS,
     -            ' steps; ', 'max. difference ', diffmax
              print*, 'steps = ', MAXSTEPS
          endif
          call printgrid(nx_dg1, ny_dg1, uk, OUNIT)
          close(unit=OUNIT)
      endif

      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'process ', procnum, ':  ', itimediff

      end

c-----------------------------------------------------------------------
c
c     initialize grid
c
c-----------------------------------------------------------------------

      subroutine initgrid(nx, ny, uk)
      implicit none
      include 'arch_uparms.h'
      include 'arch_parms.h'
      include 'par_poisson_header.h'

      integer nx, ny
      double precision uk(nx, ny)
```

```
      double precision F, G
      external F, G
      integer i, j

c
c     interior points
c
      do i = 2, nx-1
      do j = 2, ny-1
          uk(i,j) = F(i,j,nx,ny,H)
      enddo
      enddo
c
c     boundary points
c
      do j = 1, ny
          uk(1,j) = G(1,j,nx,ny,H)
          uk(nx,j) = G(nx,j,nx,ny,H)
      enddo
      do i = 2, nx-1
          uk(i,1) = G(i,1,nx,ny,H)
          uk(i,ny) = G(i,ny,nx,ny,H)
      enddo

      end

c---------------------------------------------------------------------
c
c     print grid data
c
c---------------------------------------------------------------------

      subroutine printgrid(nx, ny, uk, ounit)
      implicit none
      include 'arch_uparms.h'
      include 'arch_parms.h'
      include 'par_poisson_header.h'

      integer nx, ny
      double precision uk(nx, ny)
      integer ounit

      integer i, j

c     do i = 1, nx
c         if (nx .gt. 10) write (ounit,*) ' '
c         write (ounit,9999) (uk(i,j), j = 1, ny)
c     enddo
9999  format(10F8.4)
      do i = 1, nx, nx/5
          write (ounit,9999) (uk(i,j), j = 1, ny, ny/5), uk(i,ny)
      enddo
      write (ounit,9999) (uk(nx,j), j = 1, ny, ny/5), uk(nx,ny)

      end

c---------------------------------------------------------------------
c
c     do grid computation
c
c---------------------------------------------------------------------


      subroutine computegrid(ixlo,ixhi,iylo,iyhi,uk,ukp1,diffmax,nsteps)
```

```
      implicit none
      include 'arch_uparms.h'
      include 'arch_parms.h'
      include 'par_poisson_header.h'

      integer ixlo,ixhi,iylo,iyhi
      double precision uk(ixlo:ixhi,iylo:iyhi)
      double precision ukp1(ixlo:ixhi,iylo:iyhi)
      double precision diffmax
      integer nsteps

      double precision F, G
      external F, G
      double precision diff, difflocal
      integer glbstart(3), glbend(3)
      integer lclstart(3), lclend(3)
      integer ipxyz(3), iproc
      integer istart, iend, jstart, jend, kstart, kend
      integer locmaxin(3), locmaxout(3)
      logical iempty(3)
      integer i, j, k
      integer glblcl(3)
      integer istartg, jstartg, kstartg
      integer igoffset, jgoffset

c     compute loop bounds
      call local_pos(ipxyz,iproc,id_dg1)
      call pack3(2,2,1,glbstart)
      call pack3(nx_dg1-1,ny_dg1-1,1,glbend)
      call intersect(ipxyz,glbstart,glbend,lclstart,lclend,iempty,
     -    id_dg1)
      call unpack3(istart,jstart,kstart,lclstart)
      call unpack3(iend,jend,kend,lclend)
c     compute starting global indices (of local section)
      call local_to_global(ipxyz,lclstart,glblcl,id_dg1)
      call unpack3(istartg,jstartg,kstartg,glblcl)
c     compute offsets (global index = offset + local index)
      igoffset = istartg - istart
      jgoffset = jstartg - jstart

c     loop until convergence
      diffmax = TOL + 1.0

      do k = 1,MAXSTEPS

c         refresh ghost boundaries
          call boundary_exchange(uk,id_dg1)
c         compute new values
          do i = istart, iend
          do j = jstart, jend
              ukp1(i,j) = 0.25*(H*H*F(igoffset+i,jgoffset+j,
     -                  nx_dg1,ny_dg1,H)
     -            + uk(i-1,j) + uk(i,j-1)
     -            + uk(i+1,j) + uk(i,j+1) )
          enddo
          enddo
c         every NCHECK-th step, recompute convergence test
          if (mod(k,NCHECK) .eq. 0) then
              difflocal = 0.0
              do i = istart, iend
              do j = jstart, jend
                  diff = abs(ukp1(i,j) - uk(i,j))
                  if (diff .gt. difflocal) difflocal = diff
              enddo
```

```
              enddo
              call global_max_dp(difflocal,locmaxin,diffmax,locmaxout,
     -            id_dg1)
          endif
c         copy new values to old values
          do i = istart, iend
          do j = jstart, jend
              uk(i,j) = ukp1(i,j)
          enddo
          enddo

c         check for convergence
          nsteps = k
          if (diffmax .le. TOL) go to 1000

      enddo

1000  return
      end

c-----------------------------------------------------------------------
c
c     functions for Poisson equation
c
c-----------------------------------------------------------------------

      double precision function F(i,j,nx,ny,h)
      implicit none
      integer i, j, nx, ny
      double precision h

      F = 0.0
      end

c-----------------------------------------------------------------------

      subroutine Fprint(ounit)
      integer ounit
      implicit none
      write (ounit,*) 'F(i,j) = 0.0'
      end

c-----------------------------------------------------------------------

      double precision function G(i,j,nx,ny,h)
      implicit none
      integer i, j, nx, ny
      double precision h

      G = (i+j)*h
      end

c-----------------------------------------------------------------------

      subroutine Gprint(ounit)
      integer ounit
      implicit none
      write (ounit,*) 'G(i,j) = (i+j)*H'
      end

c-----------------------------------------------------------------------
c
c     automatically-generated wrapper program to pack arrays
c         and call set_mesh or redistribute_data
c
```

```
c-----------------------------------------------------------------------

      include 'par_poisson_wrap.h'

c-----------------------------------------------------------------------
```

Computational Benchmark Program.

```
c-----------------------------------------------------------------------
c
c     example of mesh/spectral archetype
c
c     Poisson solver
c
c     benchmark version
c
c     make-time parameters:
c         NX, NY = dimensions of grid
c
c     may need to adjust loops bounded by klim
c
c-----------------------------------------------------------------------

c-----------------------------------------------------------------------
c
c     main program
c
c-----------------------------------------------------------------------

      program main
      implicit none
c     include 'arch_uparms.h'
c     include 'arch_parms.h'
c     include 'bench_poisson_header.h'

c     call procmain()
c     end

c-----------------------------------------------------------------------
c
c     process-main program
c
c-----------------------------------------------------------------------

c     subroutine procmain()
c     implicit none
c     include 'arch_uparms.h'
c     include 'arch_parms.h'
      include 'bench_poisson_header.h'

      integer IUNIT,OUNIT
      parameter (IUNIT=11,OUNIT=12)
      character*(*) P_IN
      parameter (P_IN='poisson.IN')
      character*(*) P_OUT1,P_OUT2
      parameter (P_OUT1='bench_poisson',P_OUT2='.OUT')

c     integer procnum, idummy(3)
c     integer procnum_one, procxyz_one(3)
c     integer procnum_blk, procxyz_blk(3)
c     integer low(3), high(3)
c     double precision uk(lclsize_dg1)
c     double precision ukp1(lclsize_dg1)
      double precision uk(nx_dg1*ny_dg1)
```

```
      double precision ukp1(nx_dg1*ny_dg1+2)
      double precision F, G
      external F, G
      double precision diffmax
      integer nsteps
      integer istarts, istartms, istops, istopms, itimediff, k, klim

      character*80 p_out
      character*4 cbuff1,cbuff2
      integer cblen1,cblen2

c-----benchmark reading constants
c
c     read and broadcast constants
c
c     call local_pos(idummy,procnum,-1)
c     if (procnum .eq. IOPROC) then
c         print*, 'procs = ', procs
          print*, 'nx_dg1 = ', nx_dg1
          print*, 'ny_dg1 = ', ny_dg1
c         print*, 'nprocx_blk = ', nprocx_blk
c         print*, 'nprocy_blk = ', nprocy_blk

      call mytime(istarts, istartms)
      klim = 100
      do k=1,klim
              open(unit=IUNIT, file=P_IN, access='sequential',
     $            status='old', form='formatted')
              read(IUNIT, *) H
              read(IUNIT, *) TOL
              read(IUNIT, *) NCHECK
              read(IUNIT, *) MAXSTEPS
              close(unit=IUNIT)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'input: ', klim, itimediff, dble(itimediff)/dble(klim)
c     endif
c     call broadcast(NIC,NRC,NDPC,iconst,rconst,dconst,-1)

c
c     set up grid (undistributed)
c
c     call wrapper(id_dg1,id_one,DOUBLEPRECISION_T,uk,SETMESH)
c     call local_pos(procxyz_one,procnum_one,id_dg1)

c-----benchmark initialization (within initgrid)
c
c     initialize undistributed grid
c
c     if (procnum_one .eq. 1) then
          call initgrid(nx_dg1, ny_dg1, uk)
c     endif

c
c     distribute
c
c     call wrapper(id_dg1,id_blk,DOUBLEPRECISION_T,uk,REDISTRIBUTEDATA)
c     call local_pos(procxyz_blk,procnum_blk,id_dg1)

c-----benchmark computation (within computegrid)
c
c     perform computation
c
c     call data_bounds(procxyz_blk, low, high, id_dg1)
```

```
c     call computegrid(low(1),high(1),low(2),high(2),uk,ukp1,
c    -    diffmax,nsteps)
      call computegrid(1,nx_dg1,1,ny_dg1,uk,ukp1,diffmax,nsteps)

c
c     redistribute to collect all data in one process again
c
c     call wrapper(id_dg1,id_one,DOUBLEPRECISION_T,uk,REDISTRIBUTEDATA)

c
c     print results
c
c     if (procnum_one .eq. 1) then
      call mytime(istarts, istartms)
      klim = 100
      do k=1,klim
c         build output filename (dummy version)
          write (cbuff1, '(3i1.1)') 0
          cblen1=1
          write (cbuff2, '(3i1.1)') 0
          cblen2=1
          p_out = P_OUT1 // P_OUT2
          open(unit=OUNIT, file=p_out, access='sequential',
     $         status='unknown', form='formatted')
          write (OUNIT,*) 'NX, NY = ', nx_dg1, ny_dg1
          write (OUNIT,*) 'H = ', H
          write (OUNIT,*) 'tolerance = ', TOL
          call Fprint(OUNIT)
          call Gprint(OUNIT)

          if (diffmax .le. TOL) then
              write (OUNIT,*) 'convergence occurred in ',
     -            nsteps, ' steps'
c             print*, 'steps = ', nsteps
          else
              write (OUNIT,*) 'no convergence in ', MAXSTEPS,
     -            ' steps; ', 'max. difference ', diffmax
c             print*, 'steps = ', MAXSTEPS
          endif
          call printgrid(nx_dg1, ny_dg1, uk, OUNIT)
          close(unit=OUNIT)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'output: ', klim, itimediff,
     $    dble(itimediff)/dble(klim)
c     endif

c     return
      end

c--------------------------------------------------------------------------
c
c     initialize grid
c
c--------------------------------------------------------------------------

      subroutine initgrid(nx, ny, uk)
      implicit none
c     include 'arch_uparms.h'
c     include 'arch_parms.h'
      include 'bench_poisson_header.h'

      integer nx, ny
      double precision uk(nx, ny)
```

```
      double precision F, G
      external F, G
      integer i, j
      integer istarts, istartms, istops, istopms, itimediff, k, klim

c-----benchmark

      call mytime(istarts, istartms)
      klim = 1000
      do k=1,klim
c
c     interior points
c
      do i = 2, nx-1
      do j = 2, ny-1
          uk(i,j) = F(i,j,nx,ny,H)
      enddo
      enddo
c
c     boundary points
c
      do j = 1, ny
          uk(1,j) = G(1,j,nx,ny,H)
          uk(nx,j) = G(nx,j,nx,ny,H)
      enddo
      do i = 2, nx-1
          uk(i,1) = G(i,1,nx,ny,H)
          uk(i,ny) = G(i,ny,nx,ny,H)
      enddo

      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'initialization: ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

      end

c--------------------------------------------------------------------------
c
c     print grid data
c
c--------------------------------------------------------------------------

      subroutine printgrid(nx, ny, uk, ounit)
      implicit none
c     include 'arch_uparms.h'
c     include 'arch_parms.h'
      include 'bench_poisson_header.h'

      integer nx, ny
      double precision uk(nx, ny)
      integer ounit

      integer i, j

c     do i = 1, nx
c         if (nx .gt. 10) write (ounit,*) ' '
c         write (ounit,9999) (uk(i,j), j = 1, ny)
c     enddo
9999  format(10F8.4)
      do i = 1, nx, nx/5
          write (ounit,9999) (uk(i,j), j = 1, ny, ny/5), uk(i,ny)
      enddo
```

```
      write (ounit,9999) (uk(nx,j), j = 1, ny, ny/5), uk(nx,ny)

      end

c-----------------------------------------------------------------------
c
c     do grid computation
c
c-----------------------------------------------------------------------

      subroutine computegrid(ixlo,ixhi,iylo,iyhi,uk,ukp1,diffmax,nsteps)

      implicit none
c     include 'arch_uparms.h'
c     include 'arch_parms.h'
      include 'bench_poisson_header.h'

      integer ixlo,ixhi,iylo,iyhi
      double precision uk(ixlo:ixhi,iylo:iyhi)
      double precision ukp1(ixlo:ixhi,iylo:iyhi)
      double precision diffmax
      integer nsteps

      double precision F, G
      external F, G
      double precision diff, difflocal
c     integer glbstart(3), glbend(3)
c     integer lclstart(3), lclend(3)
c     integer ipxyz(3), iproc
      integer istart, iend, jstart, jend, kstart, kend
c     integer locmaxin(3), locmaxout(3)
c     logical iempty(3)
      integer i, j, k
c     integer glblcl(3)
      integer istartg, jstartg, kstartg
      integer igoffset, jgoffset
      integer istarts, istartms, istops, istopms, itimediff, k, klim

c     compute loop bounds
c     call local_pos(ipxyz,iproc,id_dg1)
c     call pack3(2,2,1,glbstart)
c     call pack3(nx_dg1-1,ny_dg1-1,1,glbend)
c     call intersect(ipxyz,glbstart,glbend,lclstart,lclend,iempty,
c    -    id_dg1)
c     call unpack3(istart,jstart,kstart,lclstart)
c     call unpack3(iend,jend,kend,lclend)
c     compute starting global indices (of local section)
c     call local_to_global(ipxyz,lclstart,glblcl,id_dg1)
c     call unpack3(istartg,jstartg,kstartg,glblcl)
c     compute offsets (global index = offset + local index)
c     igoffset = istartg - istart
c     jgoffset = jstartg - jstart

      istart=2
      jstart=2
      kstart=1
      iend=nx_dg1-1
      jend=ny_dg1-1
      kend=1
      igoffset=0
      jgoffset=0

c     loop until convergence
      diffmax = TOL + 1.0
```

```
c     do k = 1,MAXSTEPS

c         refresh ghost boundaries
c         call boundary_exchange(uk,id_dg1)

c-----    benchmark computation of new values
c         compute new values

          call mytime(istarts, istartms)
          klim = 1000
          do k=1,klim

          do i = istart, iend
          do j = jstart, jend
              ukp1(i,j) = 0.25*(H*H*F(igoffset+i,jgoffset+j,
     -                nx_dg1,ny_dg1,H)
     -            + uk(i-1,j) + uk(i,j-1)
     -            + uk(i+1,j) + uk(i,j+1) )
          enddo
          enddo

          enddo
          call mytime(istops, istopms)
          call mytimediff(istarts, istartms, istops, istopms, itimediff)
          print*, 'computation: ', klim, itimediff,
     $         dble(itimediff)/dble(klim)

c-----    benchmark convergence test
c         every NCHECK-th step, recompute convergence test
c         if (mod(k,NCHECK) .eq. 0) then

              call mytime(istarts, istartms)
              klim = 1000
              do k=1,klim

              difflocal = 0.0
              do i = istart, iend
              do j = jstart, jend
                  diff = abs(ukp1(i,j) - uk(i,j))
                  if (diff .gt. difflocal) difflocal = diff
              enddo
              enddo
c             call global_max_dp(difflocal,locmaxin,diffmax,locmaxout,
c    -            id_dg1)

              enddo
              call mytime(istops, istopms)
              call mytimediff(istarts, istartms, istops, istopms,
     $            itimediff)
              print*, 'convergence test: ', klim, itimediff,
     $            dble(itimediff)/dble(klim)

c         endif

c----     benchmark copy
c         copy new values to old values

          call mytime(istarts, istartms)
          klim = 1000
          do k=1,klim

          do i = istart, iend
          do j = jstart, jend
              uk(i,j) = ukp1(i,j)
          enddo
```

```
          enddo

          enddo
          call mytime(istops, istopms)
          call mytimediff(istarts, istartms, istops, istopms, itimediff)
          print*, 'copy: ', klim, itimediff,
     $         dble(itimediff)/dble(klim)

c         check for convergence
c         nsteps = k
c         if (diffmax .le. TOL) go to 1000

c     enddo

c1000  return
1000  continue
      end

c-----------------------------------------------------------------------
c
c     functions for Poisson equation
c
c-----------------------------------------------------------------------

      double precision function F(i,j,nx,ny,h)
      implicit none
      integer i, j, nx, ny
      double precision h

      F = 0.0
      end

c-----------------------------------------------------------------------

      subroutine Fprint(ounit)
      integer ounit
      implicit none
      write (ounit,*) 'F(i,j) = 0.0'
      end

c-----------------------------------------------------------------------

      double precision function G(i,j,nx,ny,h)
      implicit none
      integer i, j, nx, ny
      double precision h

      G = (i+j)*h
      end

c-----------------------------------------------------------------------

      subroutine Gprint(ounit)
      integer ounit
      implicit none
      write (ounit,*) 'G(i,j) = (i+j)*H'
      end

c-----------------------------------------------------------------------
c
c     automatically-generated wrapper program to pack arrays
c         and call set_mesh or redistribute_data
c
c-----------------------------------------------------------------------
```

```
c     include 'bench_poisson_wrap.h'

c-----------------------------------------------------------------------
```

Communication Benchmark Program.

```
C-----------------------------------------------------------------------
C
C       program bench_mesh_spectral
C       written by adam rifkin, adam@cs.caltech.edu, 1996
C       modified by berna massingill
C
C       calculates times for the archetype library routines
C
C       make-time parameters:
C           NX, NY = dimensions of grid
C           NPROCS = number of processes
C           NXPROCS, NYPROCS = dimensions of process grid
C
C       may also need to adjust loops bounded by klim
C
C-----------------------------------------------------------------------

      program main
      implicit none
      include 'arch_uparms.h'
      include 'arch_parms.h'
      include 'bench_mesh_spectral_header.h'

      processors (MAXPROCS)
      call spawn(procs)
      end

C-----------------------------------------------------------------------

      subroutine procmain()
      implicit none
      include 'arch_uparms.h'
      include 'arch_parms.h'
      include 'bench_mesh_spectral_header.h'

c     number of times to do communication operations
      integer NTIMES
      parameter (NTIMES=10)
c     sizes of data for broadcast operation
      integer NIC, NRC, NDPC
      parameter (NIC=2)
      parameter (NRC=2)
      parameter (NDPC=2)

      integer IUNIT,OUNIT
      parameter (IUNIT=11,OUNIT=12)

      integer procnum, procxyz(3), datasize(3)
      integer low(3), high(3)
      integer glbstart(3), glbend(3)
      integer lclstart(3), lclend(3)
      integer locals(3), globals(3)
      integer k, itemp1, itemp2, itemp3
      logical iempty(3)
      integer iconst(NIC)
      integer rconst(NRC)
      integer dconst(NDPC)
      double precision difflocal, diffmax
```

```
      integer locmaxin, locmaxout
      double precision data(lclsize_dg1)
      integer istarts, istartms, istops, istopms, itimediff, klim, k
      external readproc, writeproc

      call local_pos(procxyz,procnum,-1)
      if (procnum.eq.IOPROC) then
          print*, 'procs = ', procs
          print*, 'data sizes:'
          print*, 'nx_dg1 = ', nx_dg1
          print*, 'ny_dg1 = ', ny_dg1
          print*, 'broadcast sizes:'
          print*, 'NIC = ', NIC
          print*, 'NRC = ', NRC
          print*, 'NDPC = ', NDPC
      endif

C---- benchmark wrapper SETMESH

      call mytime(istarts, istartms)
      klim = 100000
      do k=1,klim
        call wrapper(id_dg1,id_blk,DOUBLEPRECISION_T,data,SETMESH)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'SETMESH ', procnum, ':  ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

C---- benchmark local_pos

      call mytime(istarts, istartms)
      klim = 100000
      do k=1,klim
        call local_pos(procxyz,procnum,id_dg1)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'local_pos ', procnum, ':  ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

C---- benchmark data_widths

      call mytime(istarts, istartms)
      klim = 100000
      do k=1,klim
        call data_widths(procxyz,.false.,datasize,id_dg1)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'data_widths ', procnum, ':  ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

C---- benchmark wrapper REDISTRIBUTEDATA (one to blk)

      call mytime(istarts, istartms)
      klim = NTIMES
      do k=1,klim
        call wrapper(id_dg1,id_one,DOUBLEPRECISION_T,data,SETMESH)
        call wrapper(id_dg1,id_blk,DOUBLEPRECISION_T,data,
     $      REDISTRIBUTEDATA)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'SETMESH/REDISTRIBUTEDATA (one to blk) ',
```

```
     $    procnum, ':  ', klim, itimediff, dble(itimediff)/dble(klim)

C---- benchmark wrapper REDISTRIBUTEDATA (blk to one)

      call mytime(istarts, istartms)
      klim = NTIMES
      do k=1,klim
        call wrapper(id_dg1,id_blk,DOUBLEPRECISION_T,data,SETMESH)
        call wrapper(id_dg1,id_one,DOUBLEPRECISION_T,data,
     $      REDISTRIBUTEDATA)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'SETMESH/REDISTRIBUTEDATA (blk to one) ',
     $    procnum, ':  ', klim, itimediff, dble(itimediff)/dble(klim)

C---- benchmark wrapper REDISTRIBUTEDATA (row to col)

      call mytime(istarts, istartms)
      klim = NTIMES
      do k=1,klim
        call wrapper(id_dg1,id_row,DOUBLEPRECISION_T,data,SETMESH)
        call wrapper(id_dg1,id_col,DOUBLEPRECISION_T,data,
     $      REDISTRIBUTEDATA)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'SETMESH/REDISTRIBUTEDATA (row to col) ',
     $    procnum, ':  ', klim, itimediff, dble(itimediff)/dble(klim)

C---- benchmark wrapper REDISTRIBUTEDATA (col to row)

      call mytime(istarts, istartms)
      klim = NTIMES
      do k=1,klim
        call wrapper(id_dg1,id_col,DOUBLEPRECISION_T,data,SETMESH)
        call wrapper(id_dg1,id_row,DOUBLEPRECISION_T,data,
     $      REDISTRIBUTEDATA)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'SETMESH/REDISTRIBUTEDATA (col to row) ',
     $    procnum, ':  ', klim, itimediff, dble(itimediff)/dble(klim)

C---- benchmark broadcast

      call mytime(istarts, istartms)
      klim = NTIMES
      do k=1,klim
        call broadcast(NIC,NRC,NDPC,iconst,rconst,dconst,-1)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'broadcast ', procnum, ':  ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

C---- benchmark data_bounds

      call wrapper(id_dg1,id_blk,DOUBLEPRECISION_T,data,SETMESH)
      call local_pos(procxyz,procnum,id_dg1)
      call mytime(istarts, istartms)
      klim = 100000
      do k=1,klim
        call data_bounds(procxyz, low, high, id_dg1)
      enddo
```

```
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'data_bounds ', procnum, ':  ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

C---- benchmark pack3

      call mytime(istarts, istartms)
      klim = 1000000
      do k=1,klim
        call pack3(2,2,1,glbstart)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'pack3 ', procnum, ':  ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

C------ benchmark unpack3

      call mytime(istarts, istartms)
      klim = 1000000
      do k=1,klim
        call unpack3(itemp1,itemp2,itemp3,glbstart)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'unpack3 ', procnum, ':  ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

C---- benchmark intersect

      call wrapper(id_dg1,id_blk,DOUBLEPRECISION_T,data,SETMESH)
      call local_pos(procxyz,procnum,id_dg1)
      call pack3(2,2,1,glbstart)
      call pack3(nx_dg1-1,ny_dg1-1,1,glbend)
      call mytime(istarts, istartms)
      klim = 1000000
      do k=1,klim
          call intersect(procxyz,glbstart,glbend,lclstart,lclend,
     $          iempty,id_dg1)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'intersect ', procnum, ':  ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

C---- benchmark local_to_global

      call wrapper(id_dg1,id_blk,DOUBLEPRECISION_T,data,SETMESH)
      call local_pos(procxyz,procnum,id_dg1)
      call pack3(1,1,1,locals)
      call mytime(istarts, istartms)
      klim = 1000000
      do k=1,klim
          call local_to_global(procxyz,locals,globals,id_dg1)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'local_to_global ', procnum, ':  ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

C---- benchmark boundary_exchange

      call mytime(istarts, istartms)
      klim = NTIMES
```

```
      do k=1,klim
        call boundary_exchange(data,id_dg1)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'boundary_exchange (no wrap) ', procnum, ':  ',
     $    klim, itimediff, dble(itimediff)/dble(klim)

C---- benchmark global_max_dp

      call mytime(istarts, istartms)
      klim = NTIMES
      do k=1,klim
        call global_max_dp(difflocal,locmaxin,diffmax,locmaxout,id_dg1)
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'global_max_dp ', procnum, ':  ', klim, itimediff,
     $    dble(itimediff)/dble(klim)


C---- benchmark read_mesh (no actual I/O -- benchmarked elsewhere)

      call mytime(istarts, istartms)
      klim = NTIMES
      do k=1,klim
        call wrapper(id_dg1,id_row,DOUBLEPRECISION_T,data,SETMESH)
c       if (procnum.eq.IOPROC) then
c           open(unit=IUNIT, file=fft_in, form='unformatted')
c       endif
        call read_mesh(readproc, id_dg1, IUNIT, data)
c       if (procnum.eq.IOPROC) then
c           close(unit=IUNIT)
c       endif
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'read_mesh (dummy) ', procnum, ':  ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

C---- benchmark write_mesh (no actual I/O -- benchmarked elsewhere)

      call mytime(istarts, istartms)
      klim = NTIMES
      do k=1,klim
        call wrapper(id_dg1,id_row,DOUBLEPRECISION_T,data,SETMESH)
c       if (procnum.eq.IOPROC) then
c           open(unit=OUNIT, file=fft_out, form='unformatted')
c       endif
        call write_mesh(writeproc, id_dg1, OUNIT, data)
c       if (procnum.eq.IOPROC) then
c           close(unit=OUNIT)
c       endif
      enddo
      call mytime(istops, istopms)
      call mytimediff(istarts, istartms, istops, istopms, itimediff)
      print*, 'write_mesh (dummy) ', procnum, ':  ', klim, itimediff,
     $    dble(itimediff)/dble(klim)

      end

c-----------------------------------------------------------------------
c
c
c     dummy subroutine for reading input data (one local section at
```

```
c         a time)
c
c-----------------------------------------------------------------------

      subroutine readproc(ignum, iunit, ipx, ipy, ipz, ixlo, ixhi,
     -     iylo, iyhi, izlo, izhi, nxlcl, nylcl, nzlcl, rarr)
      implicit none

      integer ignum, iunit, x, y,z
      integer ipx, ipy, ipz
      integer ixlo, ixhi, iylo, iyhi, izlo, izhi
      integer nxlcl, nylcl, nzlcl

      complex rarr(ixlo:ixhi, iylo:iyhi, izlo:izhi)

c     do x=1,nxlcl
c        do y=1,nylcl
c           do z=1,nzlcl
c              read(iunit, end=10) rarr(x, y, z)
c           enddo
c        enddo
c     enddo
10    return
      end

c-----------------------------------------------------------------------
c
c     dummy subroutine for writing input data (one local section at
c         a time)
c
c-----------------------------------------------------------------------

      subroutine writeproc(ignum, ounit, ipx, ipy, ipz, ixlo, ixhi,
     -     iylo, iyhi, izlo, izhi, nxlcl, nylcl, nzlcl, warr)
      implicit none

      integer ignum, ounit
      integer ipx, ipy, ipz, x, y, z
      integer ixlo, ixhi, iylo, iyhi, izlo, izhi
      integer nxlcl, nylcl, nzlcl

      complex warr(ixlo:ixhi, iylo:iyhi, izlo:izhi)

c     do x=1,nxlcl
c        do y=1,nylcl
c           do z=1,nzlcl
c              write(ounit) warr(x, y, z)
c           enddo
c        enddo
c     enddo
      return
      end


C-----------------------------------------------------------------------

      include 'bench_mesh_spectral_wrap.h'

C-----------------------------------------------------------------------
```